Opasraportti

LuTK - Department of Mathematical Sciences (2013 - 2014)

Tutkintorakenteet

Bachelor of Science (mathematics)

Tutkintorakenteen tila: archived
Lukuvuosi: 2013-14
Lukuvuoden alkamispäivämäärä: 01.08.2013

Compulsory general studies (vähintään 8 op)

800008Y-01: Acting as a Student Tutor, 1 op
902002Y: English 1 (Reading for Academic Purposes), 2 op
902004Y: English 2 (Scientific Communication), 2 op
800008Y: Orientation for New Students, 2 op

Compulsory
800008Y-02: Personal Study Plan, 1 op
800008Y-01: Acting as a Student Tutor, 1 op
800008Y-02: Personal Study Plan, 1 op
901004Y: Swedish, 2 - 3 op

Compulsory major studies (69 op)

The following studies are compulsory for everyone. In addition, one of the courses Euclidean topology 802352A (4 op) or Metric topology 802356A (5 op).

802354A: Basics in Algebra, 5 op
802155P: Continuity and limit, 4 op
802156P: Derivative, 4 op
802154P: Elementary functions, 3 op
806113P: Introduction to Statistics, 5 op
802151P: Introduction to mathematical deduction, 5 op
802118P: Linear Algebra I, 4 op
802119P: Linear Algebra II, 5 op
800300A: Maturity test, 0 op
800322A: Multidimensional analysis, 8 op
801195P: Probability Theory, 5 op
802355A: Rings, Fields and Polynomials, 5 op
801323A: Seminar, 6 op
802353A: Series and Integrals, 6 op
Optional major studies (vähintään 4 op)

In addition to compulsory major studies, students must choose optional studies in major subject as follows:

- students planning teachers studies at least 4 cr
- others at least 11 cr

When choosing the optional major studies, student is advised to take possible demands in the coming master program into account. Notice also that, in the teachers master degree, it is possible to replace (at most) 10 cr advanced courses with intermediate courses in mathematics.

Remark. If optional courses contains courses in statistics, these courses cannot be used in a possible minor subject in statistics. Note that some of the courses might not be lectured every year.

H325035: Optional intermediate studies in mathematics, 0 - 180 op

Electives
800329A: Topology, 8 op
800343A: Permutations, Fields and Galois' Theory, 8 op
800345A: Differential Equations I, 4 op
800346A: Differential Equations II, 4 op
801344A: Basic Course on Numerical Computation, 8 op
801387A: Basic Course on Numerical Analysis, 6 op
802362A: Introduction to computational inverse problems, 5 op
801386A: Complex Analysis II, 4 op
801390A: History of Mathematics, 6 op
801389A: Basic Geometry, 6 op
802328A: Basics in Number Theory, 5 op
802331A: Principles to Mathematical Modelling, 8 op
802360A: Introduction to inverse problems, 4 op
801385A: Complex Analysis I, 4 op
801396A: Introduction to Probability Theory II, 5 op
802363A: Metric Spaces, 6 op
801346A: Introduction to Cryptography, 4 op
802364A: Introduction to Mathematical Software, 6 op
802322A: Basics in mathematical modelling, 5 op

H326635: Optional intermediate studies in statistics, 0 - 180 op

Electives
805324A: Time series analysis, 5 op
806351A: Introduction to Independent Component Analysis, 4 op
805334A: Analysis of categorical data, 9 op
805328A: Multivariate analysis, 9 op
805333A: Robust methods, 6 op
805398A: An introduction to stochastic modelling, 8 op
805380A: Clinical biostatistics, 6 op
806330A: Analysis of Market Risk, 5 op
805309A: Statistical methods in epidemiology, 9 op
805339A: The Statistical Foundation of Econometrics, 5 - 6 op
805332A: Design of experiments, 9 op
805308A: Analysis of longitudinal data, 5 op
806357A: Statistical finance, 5 op

Minor subjects (vähintään 50 op)

Bachelor studies contains also studies in major and minor subjects. The minimum requirement is that student does either two smaller minor subjects (at least 25 cr each) or one larger minor subject (at least 60 cr).

Minor studies for students in teacher education

The choice of minor subjects defines how students qualify as teachers. Pedagogical studies for teachers forms a natural 30 cr minor subject for those students who are doing teachers studies. The other minor subject should be either physics, chemistry or computer sciences. Any other combinations should be applied separately from the Faculty of Sciences. Notice that when minimum requirements are fullfilled, one is free to choose other minor subjects (taking the study permissions into account).
Master studies in different programs might contain different requirements for major and minor studies. These requirements should be taken into account when choosing minor studies in Bachelor's degree. More information can be found in the Study Guide.

Physics as a minor subject

Chemistry as a minor subject

Computer sciences as a minor subject

Pedagogical studies

Other minor studies

Other studies

This part contains all courses which are not minor studies, such as, single courses in different subjects, extra language courses, etc.

Master's degree (Major in Mathematics and Computer Sciences)

Tutkintorakenteen tila: published

Lukuvuosi: 2013-14

Lukuvuoden alkamispäivämäärä: 01.08.2013

Compulsory advanced studies (vähintään 30 op)

Master's degree in mathematics contains advanced major studies 80 ECTS, which consists of master's thesis (30 ECTS) and other advanced studies (50 ECTS). The advanced courses can be selected from the list below (See "Optional advanced studies"). The student is encouraged to discuss of the topic of the master's thesis and course selections with the student advisor or supervisor.

Complement studies (if needed):

If needed, Bachelor’s degree is completed such that the following conditions hold:

1)  Studies in statistics at least 10 ECTS (courses 806112P Basic methods of data analysis or 805310A Statistical interference I).
2)  60 ECTS minor subject in computer sciences.

800698S: Pro gradu thesis, 30 op

Optional advanced studies (vähintään 50 op)

Choose at least 50 ECTS of advanced studies. The student is encouraged to discuss of the topic of the master's thesis and course selections with the student advisor or supervisor. Special courses might not be in the course list. In this case, please contact department's administrative officer.

H325003: Mathematics, optional advanced studies, 0 - 120 op

Electives

802653S: Lebesgue Measure and Integration Theory, 5 op
801698S: Cryptography, 5 op
Minor studies

This line of expertise trains specialists in mathematical methods of information technology for both industry and research. The emphasis is on a deep and broad grasp of mathematical methods, supported by applied courses towards the end of the studies as well as a sufficiently strong background in computer science. The graduates have found employment for example in telecommunications companies, software houses, polytechnic universities and research institutes. Suitable minor subjects include computer science (mandatory), statistics, communications engineering, economics and physics.

Other studies

Master's degree (Major in Mathematics)

Tutkintorakenteen tila: published

Lukuvuosi: 2013-14

Lukuvuoden alkamispäivämäärä: 01.08.2013
Compulsory advanced studies (vähintään 30 op)

Master's degree in mathematics contains advanced major studies 80 ECTS, which consists of master's thesis (30 ECTS) and other advanced studies (50 ECTS). The advanced courses can be selected from the list below (See "Optional advanced studies"). The student is encouraged to discuss the topic of the master's thesis with the student advisor or the supervisor. They will also help the student to choose suitable courses.

800698S: Pro gradu thesis, 30 op

Optional advanced studies (vähintään 50 op)

Choose at least 50 ECTS of advanced studies. Special courses might not be in the course list. In this case, please contact department's administrative officer.

H325003: Mathematics, optional advanced studies, 0 - 120 op

Electives
- 802653S: Lebesgue Measure and Integration Theory, 5 op
- 801698S: Cryptography, 5 op
- 802655S: Continued Fractions, 5 op
- 802644S: Introduction to Functional Analysis, 10 op
- 802636S: Information Theory, 10 op
- 802635S: Introduction to partial differential equations, 10 op
- 802652S: Hilbert Spaces, 5 op
- 800651S: Functional analysis, 10 op
- 802629S: Function estimation, 10 op
- 800674S: Fourier transform and distributions, 10 op
- 802647S: Fourier series and the discrete Fourier transform, 10 op
- 802656S: Algebraic numbers, 5 op
- 802637S: Advanced Problem Solving, 2 - 6 op
- 802645S: Number Theory A, 5 op
- 802646S: Number Theory B, 5 op
- 802631S: Modern real analysis, 10 op
- 800688S: Theory of Optimization, 10 op
- 800660S: Group Theory, 10 op
- 802633S: Statistical Pattern Recognition, 10 op
- 801643S: Topology, 10 op
- 802651S: Measure and Integration, 5 op
- 802650S: Fractal Geometry, 10 op
- 802660S: Operator theory and integral equations, 10 op

H326603: Statistics optional advanced studies, 0 - 120 op

Electives
- 805609S: Statistical methods in epidemiology, 9 op
- 805646S: Analysis of longitudinal data, 5 op
- 805679S: Time series analysis, 5 op
- 805683S: The Statistical Foundation of Econometrics, 5 - 6 op
- 805681S: Generalized Linear Models, 9 op
- 805699S: Statistical methods in epidemiology, 8 op
- 806618S: Computationally intensive statistical methods, 9 op
- 806621S: Spatial Data Analysis, 10 op
- 806628S: Statistical Finance, 5 op
- 806629S: Introduction to Sampling Methods, 4 op
- 806630S: Market Risk Analysis, 5 op
- 805651S: Stochastic processes, 10 op
- 806622S: Probability, 10 op
- 805611S: Mathematical statistics II, 10 op

Minor studies
This study line is intended, in particular, for students interested in a research career in mathematics. By selecting suitable minor subjects, student is able to work in a wide spectrum of research institutes. Suitable minor subjects are, for instance, computer sciences, statistics, economics and physics.

Other studies

Master's degree (Major in Applied Mathematics)

Tutkintorakenteen tila: published

Lukuvuosi: 2013-14

Lukuvuoden alkamispäivämäärä: 01.08.2013

Compulsory advanced studies (vähintään 30 op)

Master's degree in mathematics contains advanced major studies 80 ECTS, which consists of master's thesis (30 ECTS) and other advanced studies (50 ECTS). The advanced course can be selected from the following list (See "Optional advanced studies"). The student is encouraged to discuss the topic of the master's thesis and course selections with the student advisor or supervisor.

Complement studies

If Bachelor's degree does not include one of the following courses, student must complete the following courses (one of the courses) as a supplement studies.

- Basic Course on Numerical Computation (801344A, 8 ECTS)
- Introduction to Mathematical Software (802364A, 6 ECTS)

800698S: Pro gradu thesis, 30 op

Optional advanced studies (vähintään 50 op)

Choose at least 50 ECTS of advanced studies. Special courses might not be in the course list. In this case, please contact department's administrative officer. The student is encouraged to discuss the topic of the master's thesis and the course selections with the student advisor or supervisor.

H325003: Mathematics, optional advanced studies, 0 - 120 op

Electives

802653S: Lebesgue Measure and Integration Theory, 5 op
801698S: Cryptography, 5 op
802655S: Continued Fractions, 5 op
802644S: Introduction to Functional Analysis, 10 op
802636S: Information Theory, 10 op
802635S: Introduction to partial differential equations, 10 op
802652S: Hilbert Spaces, 5 op
800651S: Functional analysis, 10 op
802629S: Function estimation, 10 op
800674S: Fourier transform and distributions, 10 op
802656S: Algebraic numbers, 5 op
802637S: Advanced Problem Solving, 2 - 6 op
802645S: Number Theory A, 5 op
802646S: Number Theory B, 5 op
802631S: Modern real analysis, 10 op
800688S: Theory of Optimization, 10 op
800660S: Group Theory, 10 op
802633S: Statistical Pattern Recognition, 10 op
801643S: Topology, 10 op
802651S: Measure and Integration, 5 op
802650S: Fractal Geometry, 10 op
802660S: Operator theory and integral equations, 10 op
H326603: Statistics optional advanced studies, 0 - 120 op

Electives
805609S: Statistical methods in epidemiology, 9 op
805646S: Analysis of longitudinal data, 5 op
805679S: Time series analysis, 5 op
805683S: The Statistical Foundation of Econometrics, 5 - 6 op
805681S: Generalized Linear Models, 9 op
805699S: Statistical methods in epidemiology, 8 op
806618S: Computationally intensive statistical methods, 9 op
806621S: Spatial Data Analysis, 10 op
806628S: Statistical Finance, 5 op
806629S: Introduction to Sampling Methods, 4 op
806630S: Market Risk Analysis, 5 op
805651S: Stochastic processes, 10 op
806622S: Probability, 10 op
805611S: Mathematical statistics II, 10 op

Minor studies

This line of expertise trains the student in the use mathematical modeling to solve problems that arise in the natural sciences, various fields of technology and economics. The graduates have found employment as industrial mathematicians, teachers and researchers. Suitable minor subjects include physics, computer science, statistics, information technology and economics.

Other studies

Master's degree (Major in Statistics)

Tutkintorakenteen tila: published

Lukuvuosi: 2013-14

Lukuvuoden alkamispäivämäärä: 01.08.2013

Compulsory advanced studies (vähintään 63 op)

Master's degree in mathematics contains advanced major studies 80 ECTS, which consists of master's thesis (30 ECTS), mandatory advanced studies (63 or 65 ECTS, depending on the scope of Practical training) and optional advanced studies (17 or 15 ECTS, depending on the scope of practical training). The advanced course can be selected from the following list (See "Optional advanced studies"). The student is encouraged to discuss of the topic of the master's thesis and together with course selections with the student advisor or your supervisor.

Complement studies

If Bachelor's degree does not include one of the following courses, student must complete the following courses as a supplement studies.

- Statistical software (805340A, 4 ECTS)
- Basic Methods of Data Analysis (806112P, 10 ECTS)
- Statistical Inference I (805310A, 10 ECTS)
- Regression modelling (806359A, 10 ECTS)
Optional advanced studies (vähintään 15 op)

Choose at least 17 ECTS of advanced studies (or 15 ECTS cr if the scope of Practical training is 7 ECTS cr). Special courses might not be in the course list. If the course in question is not in the list, please contact departments administrative officer.

H325003: Mathematics, optional advanced studies, 0 - 120 op

_Electives_
- 802653S: Lebesgue Measure and Integration Theory, 5 op
- 801698S: Cryptography, 5 op
- 802655S: Continued Fractions, 5 op
- 802644S: Introduction to Functional Analysis, 10 op
- 802636S: Information Theory, 10 op
- 802635S: Introduction to partial differential equations, 10 op
- 802652S: Hilbert Spaces, 5 op
- 800651S: Functional analysis, 10 op
- 802629S: Function estimation, 10 op
- 800674S: Fourier transform and distributions, 10 op
- 802647S: Fourier series and the discrete Fourier transform, 10 op
- 802656S: Algebraic numbers, 5 op
- 802637S: Advanced Problem Solving, 2 - 6 op
- 802645S: Number Theory A, 5 op
- 802646S: Number Theory B, 5 op
- 802631S: Modern real analysis, 10 op
- 800688S: Theory of Optimization, 10 op
- 800660S: Group Theory, 10 op
- 802633S: Statistical Pattern Recognition, 10 op
- 801643S: Topology, 10 op
- 802651S: Measure and Integration, 5 op
- 802650S: Fractal Geometry, 10 op
- 802660S: Operator theory and integral equations, 10 op

H326603: Statistics optional advanced studies, 0 - 120 op

_Electives_
- 805609S: Statistical methods in epidemiology, 9 op
- 805646S: Analysis of longitudinal data, 5 op
- 805679S: Time series analysis, 5 op
- 805683S: The Statistical Foundation of Econometrics, 5 - 6 op
- 805681S: Generalized Linear Models, 9 op
- 805699S: Statistical methods in epidemiology, 8 op
- 806618S: Computationally intensive statistical methods, 9 op
- 806621S: Spatial Data Analysis, 10 op
- 806628S: Statistical Finance, 5 op
- 806629S: Introduction to Sampling Methods, 4 op
- 806630S: Market Risk Analysis, 5 op
- 805651S: Stochastic processes, 10 op
- 806622S: Probability, 10 op
- 805611S: Mathematical statistics II, 10 op

Minor studies

In this line of expertise, the spread of applications is very wide. Suitable minor subjects in this line are, for instance, mathematics, computer sciences or economics. Discuss about your choices with the head of this line or with student counsellor.
Other studies

Bachelor of Science (statistics)

Tutkintorakenteen tila: archived

Lukuvuosi: 2013-14

Lukuvuoden alkamispäivämäärä: 01.08.2013

Compulsory general studies (vähintään 8 op)

800008Y-01: Acting as a Student Tutor, 1 op
902002Y: English 1 (Reading for Academic Purposes), 2 op
902004Y: English 2 (Scientific Communication), 2 op
800008Y: Orientation for New Students, 2 op

Compulsory

800008Y-02: Personal Study Plan, 1 op
800008Y-01: Acting as a Student Tutor, 1 op
800008Y-02: Personal Study Plan, 1 op
901004Y: Swedish, 2 - 3 op

Compulsory major studies (69 op)

The following studies are compulsory for everyone.

802354A: Basics in Algebra, 5 op
802155P: Continuity and limit, 4 op
802156P: Derivative, 4 op
802154P: Elementary functions, 3 op
802352A: Euclidean Topology, 4 op
806113P: Introduction to Statistics, 5 op
802151P: Introduction to mathematical deduction, 5 op
802118P: Linear Algebra I, 4 op
802119P: Linear Algebra II, 5 op
800300A: Maturity test, 0 op
800322A: Multidimensional analysis, 8 op
801195P: Probability Theory, 5 op
802355A: Rings, Fields and Polynomials, 5 op
801323A: Seminar, 6 op
802353A: Series and Integrals, 6 op

Compulsory major studies

The following studies are also compulsory for students major in statistics:

806112P: Basic Methods of Data Analysis, 10 op
801396A: Introduction to Probability Theory II, 5 op
806359A: Regression modelling, 10 op
805310A: Statistical Inference I, 10 op
805340A: Statistical Software, 4 op

Optional intermediate studies in statistics (vähintään 15 op)

Other intermediate level courses in statistics (at least 15 ECTS) from the list below. Note that some of the courses are not lectured every year.
Electives

- 805324A: Time series analysis, 5 op
- 806351A: Introduction to Independent Component Analysis, 4 op
- 805334A: Analysis of categorical data, 9 op
- 805328A: Multivariate analysis, 9 op
- 805398A: An introduction to stochastic modelling, 8 op
- 805380A: Clinical biostatistics, 6 op
- 806330A: Analysis of Market Risk, 5 op
- 805309A: Statistical methods in epidemiology, 9 op
- 805339A: The Statistical Foundation of Econometrics, 5 - 6 op
- 805332A: Design of experiments, 9 op
- 805308A: Analysis of longitudinal data, 5 op
- 806357A: Statistical finance, 5 op

Minor subjects (vähintään 50 op)

Bachelor studies contains also studies in major and minor subjects. The minimum requirement is that student does either two smaller minor subjects (at least 25 cr each) OR one larger minor subject (at least 60 cr).

Remark. Master studies in different programs might contain different requirements for major and minor studies. These requirements should be taken into account when choosing minor studies in Bachelor's degree. More information can be found in the Study Guide.

Other studies

This part contains all courses which are not minor studies, such as, single courses in different subjects, extra language courses, etc.

Master's degree (Subject Teacher)

Tutkintorakenteen tila: published

Lukuvuosi: 2013-14
Lukuvuoden alkamispäivämäärä: 01.08.2013

Compulsory advanced studies (vähintään 30 op)

Master's degree (line: subject teacher) contains advanced major studies 60 ECTS, which consists of master's thesis (20 ECTS), Special course for teachers of mathematics (10 op), and other advanced studies (30 ECTS). The advanced courses can be selected from the list below (See "Optional advanced studies").

The student is encouraged to discuss of the topic of the master's thesis and together with course selections with the student advisor or your supervisor.

Note. In this line, students can replace at most 10 ECTS advanced studies with intermediate level studies.

- 800697S: Pro Gradu Thesis, 20 op
- 802632S: Special course for teachers of mathematics, 10 op

Optional advanced studies (vähintään 30 op)

Choose at least 30 ECTS of advanced studies. Special courses might not be in the course list. In this case, please contact department's administrative officer.
H325003: Mathematics, optional advanced studies, 0 - 120 op

Electives

802653S: Lebesgue Measure and Integration Theory, 5 op
801698S: Cryptography, 5 op
802655S: Continued Fractions, 5 op
802644S: Introduction to Functional Analysis, 10 op
802636S: Information Theory, 10 op
802635S: Introduction to partial differential equations, 10 op
802652S: Hilbert Spaces, 5 op
800651S: Functional analysis, 10 op
802629S: Function estimation, 10 op
800674S: Fourier transform and distributions, 10 op
802647S: Fourier series and the discrete Fourier transform, 10 op
802656S: Algebraic numbers, 5 op
802637S: Advanced Problem Solving, 2 - 6 op
802645S: Number Theory A, 5 op
802646S: Number Theory B, 5 op
802631S: Modern real analysis, 10 op
800688S: Theory of Optimization, 10 op
800660S: Group Theory, 10 op
802633S: Statistical Pattern Recognition, 10 op
801643S: Topology, 10 op
802651S: Measure and Integration, 5 op
802650S: Fractal Geometry, 10 op
802660S: Operator theory and integral equations, 10 op

H326603: Statistics optional advanced studies, 0 - 120 op

Electives

805609S: Statistical methods in epidemiology, 9 op
805646S: Analysis of longitudinal data, 5 op
805679S: Time series analysis, 5 op
805683S: The Statistical Foundation of Econometrics, 5 - 6 op
805681S: Generalized Linear Models, 9 op
805699S: Statistical methods in epidemiology, 8 op
806618S: Computationally intensive statistical methods, 9 op
806621S: Spatial Data Analysis, 10 op
806628S: Statistical Finance, 5 op
806629S: Introduction to Sampling Methods, 4 op
806630S: Market Risk Analysis, 5 op
805651S: Stochastic processes, 10 op
806622S: Probability, 10 op
805611S: Mathematical statistics II, 10 op

Minor studies

The degree programme of subject teacher is comprised of compulsory major subject studies in mathematics and studies in the secondary teaching subject (compulsory minor subject 60 ECTS), which can be e.g. physics, chemistry or information technology. The degree must also include pedagogic studies of 60 ECTS credits (KTK - Pedagogical Studies for Teachers). Part of the pedagogical studies and minor subject studies are already included to the Bachelor degree.

Compulsory minor studies

- Pedagogical studies 60 ECTS
- Second teacher's subject 60 ECTS (e.g. physics, chemistry, computer sciences)

Other studies
Opintojaksojen kuvaukset

Tutkintorakenteisiin kuuluvien opintokohteiden kuvaukset

800008Y-01: Acting as a Student Tutor, 1 op

Opiskelumuoto: General Studies
Laji: Partial credit
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

902002Y: English 1 (Reading for Academic Purposes), 2 op

Voimassaolo: 01.08.1995 -
Opiskelumuoto: Language and Communication Studies
Laji: Course
Vastuuysikkö: Language Centre
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: English

Proficiency level:

Status:
In the Faculty of Science, this course is mandatory for all degree programmes except Geography. Please consult the Faculty Study Guide to establish the language requirements for your own degree programme.

Required proficiency level:
English must have been the A1 or A2 language at school or equivalent English skills should have been acquired otherwise.

ECTS Credits:
2 ECTS credits (total work load 54 hours including classroom meetings.)

Language of instruction:
English

Timing:
Biology: 1st year spring term
Chemistry: 1st year autumn term
Geology: 1st year spring term
Information Processing Science: 1st year spring term
Mathematical Sciences: 1st year spring term
Physical Sciences: 1st year autumn term

Learning outcomes:
By the end of the course, you are expected

• to have acquired effective vocabulary learning techniques by being able to distinguish parts of words to infer meanings
• to understand and be able to construct basic grammatical structures used in formal written English
• to be able to utilize text structure and cohesion markers when reading academic texts
• to be able to apply effective reading techniques and have necessary skills to extract global and detailed information with considerable ease and speed from general texts related to Natural Sciences as well as texts/textbooks of their own field

Contents:
In this course, students improve their understanding of written academic English used in texts in Natural Sciences as well as expand their general and scientific vocabulary. Students become aware of their own role in learning and use a variety of different study methods in order to develop their own language learning strategies, which will enhance their academic English.
Mode of delivery:
Contact teaching

Learning activities and teaching methods:
Contact teaching (26 hours) and self-study 28 hours

Target group:
1st year students of Biology, Chemistry, Geology, Information Processing Science, Physics, and Mathematics

Prerequisites and co-requisites:
-

Recommended optional programme components:
In addition to this course, students are required to take 902004Y Scientific Communication.

Recommended or required reading:
Set books for substance studies; journal articles in print and on-line.

Assessment methods and criteria:
Continuous assessment takes into account active and regular participation in classroom sessions and successful completion of all homework tasks, vocabulary quizzes, and an end of course exam.

Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Biology, Geology, Information Processing: Karen Niskanen
Chemistry, Physics, Mathematics: Patrick Nesbitt

Working life cooperation:
-

Other information:
N.B. Students with grades laudatur or eximia in their A1 English school-leaving examination can be exempted from this course and will be granted the credits by the Faculty of Science.

Retake examinations: Two retake examinations are allowed on the dates set by the Extension School. See the dates and registration instructions at: http://www.oulu.fi/kielikoulutus

902004Y: English 2 (Scientific Communication), 2 op

Voimassaolo: 01.08.1995 -
Opiskelumuoto: Language and Communication Studies
Laji: Course
Vastuuysikkö: Language Centre
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: English
Leikkaavuudet:
    ay902004Y    English 2 (Scientific Communication) (OPEN UNI)    2.0 op

Proficiency level:
B2/C1 on the CEFR scales

Status:
This course is mandatory for all 2nd year students (except geographers) who will have English as their foreign language in their B.Sc. degree. This includes the students who were exempted from 'Reading for Academic Purposes'(902002Y). Please consult the faculty study guide to establish the language requirements on your own degree programme.

Required proficiency level:
Students taking this course must have had English as the A1 or A2 language at school or the equivalent English skills should have been acquired otherwise. The course 'Reading for Academic Purposes' (902002Y) is a pre-requisite, unless exempted.

ECTS Credits:
The student workload is 53 hrs work/ 2 ECTS credits.

Language of instruction:
English

Timing:
Biology: 2nd year autumn term
Chemistry: 2nd year spring term
Geology: 2nd year spring term
Learning outcomes:
By the end of the course, you are expected:
1. to have provided evidence of oral fluency in pair work communication and small group discussions.
2. to have developed effective language learning strategies through autonomous homework.
3. to have demonstrated the ability to prepare and present scientific subjects, using appropriate field-related vocabulary.
4. to have demonstrated lecture listening skills in field-related situations.

Contents:
Skills in listening, speaking, and giving presentations are practised in the course. Homework tasks include autonomous work to support the classroom learning and the task of preparing and presenting a scientific presentation.

Mode of delivery:
Contact teaching

Learning activities and teaching methods:
Contact teaching 28 hours, homework 28 hours

Target group:
2nd year students of Biology, Chemistry, Geology, Information Processing Science, Mathematics, Physics

Prerequisites and co-requisites:
-

Recommended optional programme components:
Also required: 902002Y Reading for Academic Purposes Englannin kieli 1

Recommended or required reading:
Course materials will be provided by the teacher and a copy fee will be charged.

Assessment methods and criteria:
Continuous assessment is based on regular attendance, active participation in all lessons and the successful completion of all homework tasks.

Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass / fail.

Person responsible:
Jolene Gear

Working life cooperation:
-

Other information:
Alternative method of course completion: An optional exemption test is offered twice per year. The student can only participate in the exemption exam once. See exemption exam details and schedule.

800008Y: Orientation for New Students, 2 op

Opiskelumuoto: General Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
2 ECTS

Language of instruction:
Finnish

Timing:
First year (autumn term)

Learning outcomes:
After the course, student is familiar with objectives and curriculum of the degree program. Moreover, the student is familiarized with the correct study methods and learning environment. After the course, the student is also able to search information from, for instance, university library and databases. After the course, student has planned future studies (study plan).

Contents:
The aim of the course is to familiarise the student with university studies, learning environment, provide the student with information on the history and current weight of mathematical sciences in the society as well as the objectives and curriculum of the degree programme. During the course, student makes the study plan.

**Mode of delivery:**
Face-to-face teaching (tutoring group)

**Learning activities and teaching methods:**
Group working

**Target group:**
Major students

**Prerequisites and co-requisites:**
-

**Recommended optional programme components:**
-

**Recommended or required reading:**
-

**Assessment methods and criteria:**
Taking part to the group meetings and making the Personal Study Plan. Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
Pass/Fail

**Person responsible:**
Student advisor

**Working life cooperation:**
-

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_compulsory_

**800008Y-02: Personal Study Plan, 1 op**

Opiskelumuoto: General Studies  
Laji: Partial credit  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

**800008Y-01: Acting as a Student Tutor, 1 op**

Opiskelumuoto: General Studies  
Laji: Partial credit  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

**901004Y: Swedish, 2 - 3 op**
Voimassaolo: 01.08.1995 -
Opiskelumuoto: Language and Communication Studies
Laji: Course
Vastuuysikkö: Language Centre
Opintokohteen kielet: Swedish
Leikkaavuudet:
   901035Y Second Official Language (Swedish), Oral Skills 1.0 op
   901034Y Second Official Language (Swedish), Written Skills 1.0 op
   ay901004Y Swedish (OPEN UNI) 2.0 op

Proficiency level:
B1/B2/C1 (CEFR scale)

Status:
This course is compulsory to all students except those who have at least 60 ECTS credits of Swedish studies in their degrees. The language proficiency provided by the course unit is equivalent to the language proficiency required of a state official with an academic degree working in a bilingual municipality area (Act 424/03 and Decree 481/03).

Required proficiency level:
The required starting proficiency level for students of all faculties is a grade of 7 or higher from the Swedish studies at secondary school (B-syllabus) or matriculation examination grade A - L or a passing grade from the Brush up course Swedish 901018Y.
If a student doesn't meet these requirements or his/her language skills are otherwise lacking, he/she must achieve the required proficiency level BEFORE taking this compulsory Swedish course.

ECTS Credits:
2 ECTS credits (Biochemistry 3 ECTS credits)

Language of instruction:
Swedish

Timing:
See the study guide of the Faculty of Science.

Learning outcomes:
Upon completion of the course the student should have acquired the necessary proficiency level in Swedish to be able to manage in the most common communication situations related to his/her professional work tasks. He/she should be able to use basic grammatical structures fairly well in both speech and writing. He/she should be able to use the most common situational phrases understandably in various communication situations. He/she should be able to find the main points in general academic texts and texts related to his/her field of study and relay this information to colleagues or an audience of laymen using Swedish. He/she should be able to write short texts relating to his/her field of study.

Contents:
Communicative oral and written exercises, which aim to develop the student's Swedish proficiency in areas relevant to his/her academic field and future professional tasks. The student practises oral presentation and pronunciation. Situational oral exercises done individually and in pairs and groups. Discussions in small groups. Current texts about the student's special field. Listening comprehension exercises. Written exercises relating to the student's professional field.

Mode of delivery:
Contact teaching

Learning activities and teaching methods:
2 ECTS credits: 28 hours of contact teaching (1 x 180 minutes per week) and related exercises, self-directed study. The course unit's total workload is 53 hours.
3 ECTS credits (biochemistry): 45 hours of contact teaching (2 x 90 minutes per week) and related exercises, 35 hours of self-directed study. The course unit's total workload is 80 hours.

Target group:
Students of the Faculty of Science

Prerequisites and co-requisites:
See Required Proficiency Level

Recommended optional programme components:

Recommended or required reading:
The material, which is special field-specific, authentic and up to date, is distributed during the course. Students must pay for their course material.

Assessment methods and criteria:
The course focuses on improving both oral and written language skills and requires active attendance and participation in exercises, which also require preparation time. 100% attendance is required. The course unit tests
both oral and written language skills. Students participate in the teaching in either autumn semester or spring semester.

Read more about assessment criteria at the University of Oulu webpage.

**Grading:**
Assessment is based on continuous assessment and exams. Approved completion of the course unit requires that the student achieves at least satisfactory oral and written language skills. The grades are based on continuous assessment and the course exams. Oral and written language skills are graded separately. The possible grades are satisfactory skills (CERF proficiency level B1) and good skills (CERF proficiency levels B2-C1). For more information on the proficiency levels of oral and written language skills, see Assessment Criteria (in Finnish).

**Person responsible:**
Lecturer Rauno Varonen

**Working life cooperation:**
-

**Other information:**
Teaching will begin according to the schedule

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**802354A: Basics in Algebra, 5 op**

**Voimassaolo:** 01.08.2010 -

**Opiskelumuoto:** Intermediate Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Kari Myllylä

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
- ay802354A Number Theory and Groups (OPEN UNI) 5.0 op
- 800333A Algebra I 8.0 op

**ECTS Credits:**
5 ECTS credits

**Language of instruction:**
Finnish

**Timing:**
1. year, 3. period

**Learning outcomes:**
After completing the course, student is able to
- derive and proof main results in the course
- use and apply different proof techniques
- recognize algebraic structures and the concepts
- see connections and differences between different algebraic structures

**Contents:**
The course includes basics in arithmetics and algebraic structures, such as, congruence, residue classes, prime numbers, Euclidean algorithm, the fundamental theorem of arithmetic, Euler-Fermat formula, groups and morphisms.

The course gives an understanding of algebraic terms and concepts used in mathematics and physics.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
28h lectures, 14h exercises

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
802151P Introduction to mathematical deduction

**Recommended optional programme components:**
-

**Recommended or required reading:**
Lecture notes

**Assessment methods and criteria:**
Midterm exam or final exam
**802155P: Continuity and limit, 4 op**

**Voimassaolo:** 01.08.2012 -

**Opiskelumuoto:** Basic Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
- 800119P Analysis 1 5.0 op
- 802162P Continuity and Limit 5.0 op
- 801111P Basic Methods in Mathematics I / math 10.0 op
- 800147P Basic Methods in Mathematics I / appl. 8.0 op

**ECTS Credits:**
4 cr

**Language of instruction:**
Finnish

**Timing:**
1. year, 1. period

**Learning outcomes:**
After completing the course, student is able to
- derive and proof main results of the course
- use different types of proof techniques
- define the limit of function and the continuity of function
- derive and proof the limit using different proof techniques
- deduce the continuity of functions using different proof techniques

**Contents:**
The main concept of the course are the limit of a real-valued function and the continuity of real-valued function. Interrelations between these concepts are also studied.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
28h lectures, 14h exercises

**Target group:**
Main and minor students

**Prerequisites and co-requisites:**
802151P Introduction to mathematical deduction

**Recommended optional programme components:**
- 

**Recommended or required reading:**
- 

**Assessment methods and criteria:**
Final exam

Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Maarit Järvenpää

**Working life cooperation:**
-
802156P: Derivative, 4 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Maarit Järvenpää
Opintokohteen kielet: Finnish
Leikkaavuudet:
- 800317A Analysis 2 5.0 op
- 802163P Derivative 5.0 op
- 801111P Basic Methods in Mathematics I / math 10.0 op

ECTS Credits:
4 cr
Language of instruction:
Finnish
Timing:
1. year, 2. period
Learning outcomes:
After completing the course, student is able to
- derive and proof main results of the course
- use different types of proof techniques
- use and apply the concept of derivative in different types of problems
Contents:
The course considers the concept of derivative of real-valued function and applies this concept to different types of situations.
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
28h lectures, 14 h exercises
Target group:
Major and minor students
Prerequisites and co-requisites:
802151P Introduction to mathematical deduction
802154P Elementary functions
802155P Limits and continuity

Recommended optional programme components:
-
Recommended or required reading:
-
Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible:
Maarit Järvenpää
Working life cooperation:
-

802154P: Elementary functions, 3 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Basic Studies
Laji: Course
Introduction to Real Functions

5.0 op

Basic Methods in Mathematics I / math

10.0 op

Basic Methods in Mathematics I / appl.

8.0 op

ECTS Credits:

3 cr

Language of instruction:

Finnish

Timing:

1. year, 1. period

Learning outcomes:

After completing the course, student is able to

- prove essential result in the course
- use and apply different types of proof techniques
- handle elementary functions

Contents:

Course introduces basic concepts and definitions related to real-valued functions. Definitions and proofs are essential part of the course.

Mode of delivery:

Face-to-face teaching

Learning activities and teaching methods:

21h luentoja, 10 h harjoituksia

Target group:

Major and minor students

Prerequisites and co-requisites:

802151P Introduction to mathematical deduction

Recommended optional programme components:

-

Recommended or required reading:

-

Assessment methods and criteria:

Final exam

Read more about assessment criteria at the University of Oulu webpage.

Grading:

1-5

Person responsible:

Maarit Järvenpää

Working life cooperation:

-
Introduction to Statistics  5.0 op
A Second Course in Statistics  5.0 op
Statistics for Economic Sciences  5.0 op

ECTS Credits:
5 cr
Language of instruction:
Finnish
Timing:
First year, 3. period
Learning outcomes:
On successful completion of this course, the student will be able to
- present the dataset by using graphics, tables and statistics
- apply appropriate statistical techniques for analyzing solutions to simple real-world problems
- interpret listing of some statistical software

Contents:
The course presents probabilistic techniques for studying uncertainty, and to illustrate how such techniques can be applied to make statistical analysis and interpretation of data in simple one variable settings. Topics include descriptive statistics, basics of probability theory, random variables and their distributions, sampling distributions, estimation, confidence intervals, and hypothesis testing. One aim is also to get basic knowledge from some statistical software.

Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
32 h lectures, 24 h exercises from which 16 h are normal exercises and 8 h computer exercises.

Target group:
Major and minor students
Prerequisites and co-requisites:
802151P Introduction to mathematical deduction
801195P Introduction to probability theory
802118P Linear algebra I

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible:
Hanna Heikkinen
Working life cooperation:
No

802151P: Introduction to mathematical deduction, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
ay802151P Introduction to mathematical deduction (OPEN UNI) 5.0 op

ECTS Credits:
5 ECTS
Language of instruction:
Finnish
Timing:
First period at the first semester.
Learning outcomes:
After completing the course, student
- is able to use different methods proving techniques
- is able to use basic set theoretic concepts and definitions
- is able to define and apply basic definitions related to functions

Contents:
The course in an introduction to mathematical deduction and introduces different types of proof techniques. The course covers the concepts familiar from upper secondary school studies more profound way. Main concepts in this course are basic set theory and functions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 30h, exercises 18h

Target group:
Major and minor students

Prerequisites and co-requisites:
-

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Tero Vedenjuoksu

Working life cooperation:
-

802118P: Linear Algebra I, 4 op

Voimassaolo: 16.10.2012 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Lay, David C. , 2003
Opintokohteen kielet: Finnish
Leikkaavuudet:
   802120P Introduction to Matrices 5.0 op

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
First semester, 2. period

Learning outcomes:
On successful completion of this course, the student will be able to
- solve linear systems of equations ja apply them to linear algebraic problems
- know matrices and their basic properties
- know basic properties of linear spaces

Contents:
The aim is to familiarise the student with the basics of linear algebra: systems of linear equations, vector space R^n and matrix algebra.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
35 h lectures, 21 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Midterm exams or final exam

Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Tero Vedenjuoksu

Working life cooperation:
-

802119P: Linear Algebra II, 5 op

Opiskelumuoto: Basic Studies

Laji: Course

Vastuuysikkö: Department of Mathematical Sciences

Arvostelu: 1 - 5, pass, fail

Opintokohteen oppimateriaali:
Lay, David C., 2003

Opintokohteen kielet: Finnish

Leikkaavuudet:
802320A Linear Algebra 5.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
First year, 4. period

Learning outcomes:
On successful completion of this course, the student will be able to
- basic properties of inner product spaces
- linear mappings, their matrix representation, and eigen values
- determinants and apply them to problems relating to matrices and linear mappings

Contents:
The aim of the course is to provide the student with the knowledge needed in almost all later courses in mathematics:
Abstract vector spaces and subspaces, Linear independence and bases, Inner product spaces, Linear mappings, Determinants, Eigenvalues and Eigenvectors, Hermitian matrices and quadratic forms.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
35 h lectures, 21 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802119P Linear algebra I

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Midterm exam or final exam

Read more about assessment criteria at the University of Oulu webpage.
800300A: Maturity test, 0 op

Opiskelumuoto: Intermediate Studies  
Laji: Course  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish  

ECTS Credits: 0 cr  
Language of instruction: Finnish/Swedish  
Timing: Third year  
Learning outcomes: Maturity test  
Contents: Students must take a written maturity test to demonstrate their language skills and how well they know the topic of their thesis. The maturity test is taken in the language in which the student has received his or her education in Finland. If the student has received his or her education in a language other than Finnish or Swedish, the degree programme determines the language of the maturity test. In such cases only the contents of the maturity test is evaluated, not the language.  
Mode of delivery: Maturity test written in examination room.  
Learning activities and teaching methods: Maturity test  
Target group: Major students  
Prerequisites and co-requisites: Bachelor’s degree (or similar)  
Recommended optional programme components: -  
Recommended or required reading: -  
Assessment methods and criteria: Maturity test  
Read more about assessment criteria at the University of Oulu webpage.  
Grading: Pass/Fail  
Person responsible: Supervisor of thesis  
Working life cooperation: -

800322A: Multidimensional analysis, 8 op

Opiskelumuoto: Intermediate Studies  
Laji: Course  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Pekka Salmi  
Opintokohteen kielet: Finnish
Leikkaavuudet:
800328A Calculus of several variables 5.0 op
802351A Vector Calculus 5.0 op

ECTS Credits:
8 cr
Language of instruction:
Finnish
Timing:
Second year, periods 1-2
Learning outcomes:
On successful completion of this course, the student will be able to
- differentiate multivariate functions
- apply the derivative to minimization problems
- define and use multidimensional integrals
Contents:
The course deals with multidimensional real calculus. The topology of $\mathbb{R}^n$ is reviewed, after which differential and integral calculus is derived for vector-valued functions of multiple arguments are derived.
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
56 h lectures, 28 h exercises
Target group:
Major and minor students
Prerequisites and co-requisites:
Linear algebra I
Linear algebra II
Euclidean topology
Series and integrals
Recommended optional programme components:
-
Recommended or required reading:
Lecture notes
Assessment methods and criteria:
Midterm exams or final exam
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible:
Maarit Järvenpää
Working life cooperation:
No

801195P: Probability Theory, 5 op

Voimassaalo: 01.01.2011 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Tuominen, P., , 1993
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits
Language of instruction:
Finnish (possible also in English)
Timing:
First year, 2. period

**Learning outcomes:**
On successful completion of this course, the student will be able to
- solve simple practical problems associated with probability
- solve simple theoretical problems associated with probability
- derive the basic properties of probability, starting from the axioms

**Contents:**
The course is an introduction to Probability. After review of high school curriculum material, the axiomatic approach to Probability is introduced. The most important concepts are the probability space, conditional probability, independence, a random variable as well as its distribution and expected value.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
32 h lectures, 16 h exercises

**Target group:**
Major students

**Prerequisites and co-requisites:**
802151P Introduction to mathematical deduction
802154P Elementary functions

**Recommended optional programme components:**
-

**Recommended or required reading:**
-

**Assessment methods and criteria:**
Midterm exams or final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Lasse Holmström

**Working life cooperation:**
-

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802355A: Rings, Fields and Polynomials, 5 op

**Voimassaolo:** 01.08.2010 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Department of Mathematical Sciences
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Kari Myllylä
**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
- 800333A  Algebra I  8.0 op

**ECTS Credits:**
5 ECTS credits

**Language of instruction:**
Finnish

**Timing:**
Second year, 1. period

**Learning outcomes:**
After completing the course, student is able to
- derive and proof main results in the course
- use and apply different proof techniques
- recognize algebraic structures and the concepts
- see connections and differences between different algebraic structures

**Contents:**
The course introduces algebraic structures, such as rings, polynomial rings, ideals, integral domains, fields, finite fields, field extensions and quotient field. The course gives an understanding of algebraic terms and concepts used in mathematics and physics.

Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
28h lectures, 14h exercises
Target group:
Major students
Prerequisites and co-requisites:
802354A Number theory and groups
Recommended optional programme components:
- 
Recommended or required reading:
Lecture notes
Assessment methods and criteria:
Midterm exam or final exam
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible:
Kari Myllylä
Working life cooperation:
-

801323A: Seminar, 6 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
800331A Proseminar 10.0 op

ECTS Credits:
6 cr
Language of instruction:
Finnish (also English)
Timing:
2.-3. year of studies
Learning outcomes:
After completing the Bachelor's thesis, student
- is able to form a clear and logical
- is able to concentrate to important and essential details in the subject of thesis
- gain experience presenting mathematical concept and research studies.
Contents:
Proseminar (Bachelor's thesis) is a small mathematical study based on literature. Student is familiarized to write mathematical texts and obtain information using literature. Thesis includes a oral presentation from the subject of the thesis.
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
Seminars and own work
Target group:
Major students
Prerequisites and co-requisites:
Compulsory basic and intermediate studies.
Recommended optional programme components:
Maturity test is written from the topic of Bachelor's thesis.
Recommended or required reading:
Assessment methods and criteria:
Opinnäytetyö
Read more about assessment criteria at the University of Oulu webpage.
Grading:
Pass/Fail
Person responsible:
Maarit Järvenpää
Working life cooperation:

802353A: Series and Integrals, 6 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettaja: Peter Hästö
Opintokohteen kielet: Finnish
Leikkaavuudet:
  800318A Analysis 3  5.0 op
  802164P Series and Integral  5.0 op

ECTS Credits:
6 ECTS credits
Language of instruction:
Finnish (possible also in English)
Timing:
First year, 4. period
Learning outcomes:
After completing the course, student is able to
  • operate with real series
  • separate the concept of continuity and uniform continuity
  • define and calculate Riemann integrals
  • derive and operate function sequences and function series
  • calculate derivate and integrate function series

Contents:
The course is a continuum for the courses Limits and continuity and Derivative. Basic topological methods (presented in Euclidean Topology) are heavily used in proofs and methods involving continuous functions. The goal is the same as in the prerequisite courses, that is, to develop mathematical thinking and extend the knowledge of mathematical analysis.

Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
30h exercises, 14h exercises
Target group:
Major and minor students
Prerequisites and co-requisites:
802154P Elementary functions
802155P Limit and continuity
802156P Derivative
802352A Euclidean topology

Recommended optional programme components:

Recommended or required reading:
Lecture notes
Assessment methods and criteria:
Midterm exams or final exam
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible:
Peter Hästö
Working life cooperation:
-

H325035: Optional intermediate studies in mathematics, 0 - 180 op
Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Ei opintojaksokuvauksia.

Electives

800329A: Topology, 8 op
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Mahmoud Filali
Opintokohteen oppimateriaali:
Vala K., Suominen K., 1990
Opintokohteen kielet: Finnish

ECTS Credits:
8 cr
Language of instruction:
English (also Finnish)
Timing:
Second year or later. Fall/spring term
Learning outcomes:
On successful completion of this course, the student will be able to follow more advanced topology and analysis.
Contents:
The course presents the very basics of topology that mathematics students should know. It starts with elementary set theory, then it goes on covering metric spaces including Baire's theorem; topological spaces and convergence in topological spaces; separation axioms including Urysohn's lemma and Tietze extension theorem; compact spaces including Tyconoff theorem; and ends with connected spaces.
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
56 hours lecture, 28 h exercises
Target group:
Major and minor students
Prerequisites and co-requisites: 
Compulsory basic and intermediate studies in mathematics.

Recommended optional programme components:

- 

Recommended or required reading:
S. Willard: General Topology;
K. Suominen & K. Vala: Topologia;

Assessment methods and criteria:
Final exam, or mid-term exams
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mahmoud Filali

Working life cooperation:

800343A: Permutations, Fields and Galois' Theory, 8 op

Opiskeluomoin: Intermediate Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Niemenmaa Markku
Opintokohteen oppimateriaali:
Herstein, I. N., , 1996
Opintokohteen kielet: Finnish

Leikkaavuudet:

- 800323A Field extensions 5.0 op
- 802333A Permutations, Fields and Galois Theory 10.0 op

ECTS Credits:
8 cr

Language of instruction:
Finnish

Timing:
2. year or later. Periods 3-4 (Spring term)

Learning outcomes:
On successful completion of this course, the student will be able to
- compute with permutations and deal with their applications
- solve equations of third and fourth degree
- work with the structures of different finite fields

Contents:
The aim is to introduce three main topics which are related to each other: Elementary number theory: division algorithm, greatest common divisor, prime numbers and congruences. Group theory: group axioms, subgroups. Lagrange's theorem, homomorphisms and factor groups. Commutative ring theory: fields, polynomial rings, quotient rings and finite fields.

Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
56 h lectures, 28 h exercises

Target group:
Major- and minor students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics.

Recommended optional programme components:
-

Recommended or required reading:

Assessment methods and criteria:
Final exam, mid-term exams
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Markku Niemenmaa

Working life cooperation:
-

800345A: Differential Equations I, 4 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Boyce, William E., , 2005
Nagle, R. Kent, , 1996
Zill, Dennis G., , 2001
Opintokohteen kielet: Finnish
Leikkaavuudet:
800320A Differential equations 5.0 op

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
2. year or later, 3. period

Learning outcomes:
On successful completion of this course, the student will be able to
- recognize the concerning differential equation and choose the proper method and solve it
- notice the conditions that guarantee the uniqueness of the solution
- understand what implicit solution means

Contents:
The course consist ordinary differential equations. First order differential equations like separable, homogeneous, linear, exact and those that can be transform to them with suitable substitutions are studied and solved by algebraic methods (for example separation of variables). Iterative methods and numerical methods are applied in some cases to obtained an approximate solution or a numerical solution. Higher order linear differential equations with constant coefficients that appear in applications are considered and also second order linear differential equations with continuous coefficients. The basis of how to solve finite
systems of differential equations is given. Power series method is applied to solve some second order linear differential equations like Legendre equation.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
30 h lectures, 16 h exercises

**Target group:**
Major- and minor students

**Prerequisites and co-requisites:**
Compulsory basic and intermediate studies in mathematics.

**Recommended optional programme components:**

**Recommended or required reading:**

**Assessment methods and criteria:**
Final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Martti Kumpulainen

**Working life cooperation:**

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800346A: Differential Equations II, 4 op

**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Department of Mathematical Sciences
**Arvostelu:** 1 - 5, pass, fail
**Opintokohteen oppimateriaali:**
Nagle, R. Kent, , 1996
Folland, Gerald B., , 1992
Zill, Dennis G., , 2001
**Opintokohteen kielet:** Finnish
**Leikkaavuudet:**

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**ECTS Credits:**
4 cr

**Language of instruction:**
Finnish

**Timing:**
2. year or later, 4. period

**Learning outcomes:**
On successful completion of this course, the student will be able to
- apply method of Frobenius to solve second order linear differential equations
- proof the basic properties of Bessel functions, Legendre polynomials and Hermite polynomials
- calculate the Fourier-series of a given piecewise continuous function
- apply integral transformations to solve some integral equations and ordinary differential equations with constant coefficients
- recognize heat and wave equations and choose the proper method to solve them

Contents:
The course consist second order ordinary differential equation that are important in applications and partial differential equations like heat and wave equations. Method of Frobenius is introduced to solve second order ordinary differential equation. Some special functions (like Gamma function and Bessel functions) are considered and also orthogonal polynomials (Legendre polynomials and Hermite polynomials). The basics how to calculate Fourier-series for a piecewise continuous function is given. Last, basics of integral transformations (Laplace-transformation and Fourier-transformation) are studied, and how to apply them and the method of separation of variable in some cases to heat and wave equations.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
30 h lectures, 16 h exercises.

Target group:
Major and minor students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics

Recommended optional programme components:

Recommended or required reading:

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Martti Kumpulainen

Working life cooperation:

801344A: Basic Course on Numerical Computation, 8 op

Voimassaolo: 01.03.2011 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Erkki Laitinen
Opintokohteen oppimateriaali:
Opintokohteen kielet: Finnish

ECTS Credits:
8 cr

Language of instruction:
**Learning outcomes:**
On successful completion of this course, the student will be able to
- program using Fortran the basic numerical problems
- exploit the libraries of the University's IT center for solving numerical problems

**Contents:**
The lecture course is focused to methods how to program and solve numerical problems by computer. The lectures consist of following topics: Fortran95 programming language related to numeric, basics of Unix operating system, numerical and graphical libraries in solving numerical problems.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
20h lectures, 40h computer exercises and practical work

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
Basics in computer programming

**Recommended optional programme components:**
-

**Recommended or required reading:**
Available Fortran Manuals.

**Assessment methods and criteria:**
Exam, Practical work
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Erkki Laitinen

**Working life cooperation:**
-

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**801387A: Basic Course on Numerical Analysis, 6 op**

**Voimassaolo:** 01.03.2011 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Department of Mathematical Sciences
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Erkki Laitinen
**Opintokohteen oppimateriaali:**
Atkinson, Kendall, , 1993
**Opintokohteen kielet:** Finnish

**ECTS Credits:**
6 cr

**Learning outcomes:**
On successful completion of this course, the student will be able to
- implement efficient numerical algorithms for solving basic numerical problems
- approximate the error of numerical results

**Contents:**
The lecture course is focused on numerical methods, which can be used for solving numerically mathematical problems which analytical solution is unknown or complicated to construct. The lectures consist of following topics: Computer arithmetic, nonlinear equations, systems of linear equations, interpolation, integration, derivation and differential equations.

**Assessment methods and criteria:**
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Person responsible:**
Erkki Laitinen

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**802362A: Introduction to computational inverse problems, 5 op**

- **Voimassaolo:** 01.08.2010 -
- **Opiskelumuoto:** Intermediate Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opettajat:** Mikko Orispää
- **Opintokohteen kielet:** Finnish

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**801386A: Complex Analysis II, 4 op**

- **Opiskelumuoto:** Intermediate Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen oppimateriaali:**
  - Lang, Serge, , 1999
  - Spiegel, Murray R., , 1964
- **Opintokohteen kielet:** Finnish

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**ECTS Credits:**
4 cr

**Learning outcomes:**
On successful completion of this course, the student will be able to
- derive and prove core results of complex analysis
- apply theory of complex analysis to many structures of analysis

**Contents:**
The course deals with fundamental results on complex analysis such as Cauchy integral theorem and Cauchy integral formulas. As application some important corollaries of them will be proved such as Liouville Theorem, Fundamental theorem of algebra and Maximum principle. Further, after brief introduction to power series the presentation of analytic functions by using power series will be studied. After Laurent representation of complex functions theory of residues will be considered and as application this theory will be used to calculate certain type of definite integrals.

**Assessment methods and criteria:**
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Person responsible:**
Jorma Arhippainen

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**801390A: History of Mathematics, 6 op**

- **Opiskelumuoto:** Intermediate Studies
- **Laji:** Course
Contents:
The aim of the course is to provide the student a general conception of the history of mathematics. The main emphasis is on the calculations. Contents: Egyptian and Babylonian mathematics; Euclid and the Elements, Archimedes and Apollonius; Roman era; India and China; the islamic world; medieval mathematics; the rise of algebra; Descartes, Fermat; Newton and Leibniz, the beginning of calculus.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

801389A: Basic Geometry, 6 op

Learning outcomes:
On successful completion of this course, the student will be able to
- prove simple geometric claims
- solve simple geometric problems with the help of ruler and compass
- solve basic applied problems of school geometry

Contents:
School geometry (801389A) The course presents the core material in Finnish junior high school and high school geometry courses. It is mainly meant for those students who study to become mathematics, physics and chemistry teachers. The first part of this course is classic Euclidean plane geometry and the second part is solid geometry. Students become familiar with geometric proof and how to solve simple geometric problems with the help of ruler and compass. Geometric results are used to solve problems. The second part considers spatial geometry and starts with how lines and planes can situate in ordinary three dimensional space. Basic geometric properties of solids like cube, ball and cone are considered and methods how to calculate their surface aries and volumes are presented.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Martti Kumpulainen

802328A: Basics in Number Theory, 5 op
**Voimassaolo:** 01.06.2011 -  
**Opiskelumuoto:** Intermediate Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Tapani Matala-aho  
**Opintokohteen oppimateriaali:**  
Hardy, G. H., , 1979  
Rosen, Kenneth H., , 1993  
**Opintokohteen kielet:** Finnish  

**ECTS Credits:** 5 cr  
**Language of instruction:** Finnish  
**Timing:** 2.-3. year of studies. Timing varies.  

**Learning outcomes:**  
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.  

**Contents:**  
In our lectures we consider arithmetical properties of the common numbers involved in studying mathematics and in particular number theory. Also the methods will get a special interest. Examples of the numbers under the research will be binomials, continued fractions, sums of powers and some numbers sharing a name with the mathematicians Bernoulli, Euler, Fermat, Fibonacci, Heron, Lucas, Mersenne, Neper, Pythagoras, Stirling, Wilson and Wolstenholme. From the tools we mention congruences of rational numbers and polynomials, difference operators, generating series, irrationality considerations, matrix presentations, recurrences and telescopes.  

**Mode of delivery:**  
Face-to-face teaching  

**Learning activities and teaching methods:**  
36h lectures, 18h exercises  

**Target group:** Major and minor students  

**Prerequisites and co-requisites:**  
802354A Lukuteoria ja ryhmät,  
802355A Rings, fields and polynomials  
802118P Linear algebra I  
802119P Linear algebra II  
802352A Euclidean topology  
802353A Series and integrals  

**Recommended optional programme components:** -  

**Recommended or required reading:**  
Lecture notes,  
G.H. Hardy ja E.M. Wright: An Introduction to the Theory of Numbers;  
Kenneth H. Rosen: Elementary number theory and its applications.  

**Assessment methods and criteria:**
Mid-term exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Tapani Matala-aho

**Working life cooperation:**
-

**802331A: Principles to Mathematical Modelling, 8 op**

**Voimassaolo:** 01.08.2009 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Department of Mathematical Sciences
**Arvostelu:** 1 - 5, pass, fail
**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

**802360A: Introduction to inverse problems, 4 op**

**Voimassaolo:** 01.08.2010 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Department of Mathematical Sciences
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Sari Lasanen
**Opintokohteen kielet:** Finnish

**ECTS Credits:**
4 cr

**Language of instruction:**
Finnish. Alternatively, a book examination in English.

**Learning outcomes:**
Upon completion, the student will be able to
- recognise several inverse problems
- describe typical properties of inverse problems
- solve simple inverse problems with accurate and inaccurate data

**Contents:**
1. Examples of inverse problems and their typical properties
2. Well-posed and ill-posed problems
3. Least squares solutions
4. Tikhonov regularization
5. Statistical inverse problems

**Learning activities and teaching methods:**
Lectures 4x45 min / week. Exercises 2x45 min /week.

**Target group:**
Suitable for major and minor students.

**Prerequisites and co-requisites:**
- 802118P Linear Algebra I
- 802119P Linear Algebra II
Also recommended:
- 800322A Multidimensional Analysis (or Analysis II)
- 801396A Introduction to Probability Theory II
- 802352A Euclidian Topology
- 800345A Differential Equations I

**Assessment methods and criteria:**

Exam.
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Other information:**

This course does not contain numerical programming tasks. Computer-aided computations are contained in a separate course 802362A Introduction to Computational Inverse Problems.

**801396A: Introduction to Probability Theory II, 5 op**

**Opiskelumuoto:** Intermediate Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen oppimateriaali:**

Tuominen, P., 1993

Spiegel, Murray R., 1964

**Opintokohteen kielet:** Finnish

**ECTS Credits:**

4 cr

**Learning outcomes:**

On successful completion of this course, the student will be able to
- know the basic properties of algebraic and topological structure of complex numbers
- know the basic properties of complex functions
- be able to apply theory of complex numbers to different fields of pure and applied mathematics

**Contents:**

The course deals basic theory of complex numbers. After a brief introduction to algebraic properties of complex numbers, such basic results as polar coordinate representation, De Moivre formulas and topology on complex plane will be considered. For the complex functions the concepts of limit, continuity and derivate will be studied. Some basic properties of analytic functions will be considered and Cauchy-Riemann formulas will be proved. Finally basic theory of pathintegral of complex functions will be studied.

**Assessment methods and criteria:**

Read more about [assessment criteria](#) at the University of Oulu webpage.

**Person responsible:**

Jorma Arhippainen
Finnish

**Timing:**
2. year, Fall semester

**Learning outcomes:**
On successful completion of this course, the student will be able to
- understand probability theory deeper than before
- apply various stochastic models
- derive the basic results associated with the new concepts introduced

**Contents:**
The course is a direct continuation for the course Probability Theory I. The new concepts include for
instance the moments of a distribution, the probability generating function, the Law of Large Numbers, the
Central Limit Theorem as well as two-dimensional distributions.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
24h lectures, 12h exercises

**Target group:**
Major- and minor students. Recommended for students aiming to Master's degree with major in statistics or
major in mathematics and computer sciences.

**Prerequisites and co-requisites:**
801195P Introduction to probability I
802352A Euclidean topology
802353A Series and integrals

**Assessment methods and criteria:**
Final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Kenneth Nordström.

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802363A: Metric Spaces, 6 op

**Voimassaolo:** 01.08.2010 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Department of Mathematical Sciences
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Mahmoud Filali
**Opintokohteen kielet:** Finnish

**ECTS Credits:**
5 cr

**Language of instruction:**
English (also in Finnish)

**Timing:**
2.-3. year studies. Timing varies.

**Learning outcomes:**
After completing the course, student is able to participate fully for more advanced courses in topology and
analysis.

**Contents:**
Course includes basic definitions and results in metric spaces. Keywords are: interior, closure, convergence in metric spaces, continuity in metric spaces, Baire's theorem, compactness, contraction, implicit function theorem. Course takes known and classical results in real analysis and generalizes them to metric spaces.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
28h lectures, 14h exercises

**Target group:**
Major studies

**Recommended optional programme components:**
-

**Recommended or required reading:**
Lecture notes

**Assessment methods and criteria:**
Final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Mahmoud Filali

**Working life cooperation:**
-

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**801346A: Introduction to Cryptography, 4 op**

**Opiskelumuoto:** Intermediate Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Tapani Matala-aho

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
802336A Introduction to Cryptography 5.0 op

**ECTS Credits:**
4 cr

**Language of instruction:**
Finnish

**Timing:**
2. year or later, Fall term (1. or 2. period)

**Learning outcomes:**
After completing the course, student
- knows the principles of some traditional symmetric key methods
- knows how public key methods (RSA, discrete logarithm, knapsack) work
- is familiar with the possibility to use and apply number theory in cryptography

**Contents:**
The course considers some traditional symmetric key methods (affine system, matrix cryptography) and three public key methods, namely RSA, discrete logarithm and knapsack.

**Mode of delivery:**
Face-to-face teaching
Learning activities and teaching methods:
27 h lectures, 15 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics.

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Tapani Matala-aho

802364A: Introduction to Mathematical Software, 6 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Markus Harju
Opintokohteen kielet: Finnish

ECTS Credits:
6 cr

Language of instruction:
English

Timing:
2.-3. year of studies. Timing varies.

Learning outcomes:
After completing the course, student is able to use mathematical software (Mathematica, Matlab and R-software) in solving different types of mathematical problems.

Contents:
The course introduces mathematical softwares (Mathematica, Matlab and R-software) for students such that they are able to solve different types of mathematical problems using these programs. Student should have at least compulsory basic and intermediat studies in mathematics.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises (computer class)

Target group:
Major and minor students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics (1. and 2. studies in mathematics).

Recommended optional programme components: -
Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Home work
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mikko Orispää

Working life cooperation:

802322A: Basics in mathematical modelling, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Erkki Laitinen
Opintokohteen kielet: Finnish

H326635: Optional intermediate studies in statistics, 0 - 180 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Electives

805324A: Time series analysis, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C., , 1993
Lütkepohl, Helmut , , 1991
Hamilton, James D., , 1994
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply computer programs to fit time series models. Furthermore, a student learns to read scientific articles about time series.

**Contents:**

The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH). Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

**Recommended or required reading:**


**Assessment methods and criteria:**

Read more about [assessment criteria](#) at the University of Oulu webpage.

**Person responsible:**

Jussi Klemelä

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**806351A: Introduction to Independent Component Analysis, 4 op**

**Opiskelumuoto:** Intermediate Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish

**Assessment methods and criteria:**

Read more about [assessment criteria](#) at the University of Oulu webpage.

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**805334A: Analysis of categorical data, 9 op**

**Voi massaolo:** - 28.02.2011  
**Opiskelumuoto:** Intermediate Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish

**ECTS Credits:**

9 cr  

**Learning outcomes:**

A student who has successfully completed the course is supposed to  
- be familiar with generalized linear models and to be able to use them when studying discrete data  
- be able to model the behaviour of ordinal dependent variables  
- be able to make use of so-called mixed models while studying discrete or ordinal data

**Contents:**

The course deals with the analysis of contingency tables and with models for qualitative and ordinal dependent variables. Models for truncated dependent variables are also briefly touched. A majority of these models can be interpreted as generalised linear models (GLIM). This is why the essentials of the GLIM-theory and the corresponding phraseology is presented. So-called generalised mixed linear models (including random effects) and the estimation of their parameters by the GEE and the ML methods are also discussed. The course can be taken either as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of exercises in the computer lab.

**Assessment methods and criteria:**
Person responsible:
Markku Rahiala

805328A: Multivariate analysis, 9 op
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

805333A: Robust methods, 6 op
Voimassaolo: - 31.07.2007
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

805398A: An introduction to stochastic modelling, 8 op
Voimassaolo: - 01.09.2012
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805380A: Clinical biostatistics, 6 op
Voimassaolo: - 01.09.2012
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

806330A: Analysis of Market Risk, 5 op
Opiskelumuoto: Intermediate Studies  
Laji: Course  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Jussi Klemelä  
Opintokohteen kielet: Finnish  

Leikkaavuudet:  
806630S Market Risk Analysis 5.0 op  

ECTS Credits:  
5 cr  

Language of instruction:  
Finnish  

Timing:  
3. year of studies or later. Timing varies.  

Learning outcomes:  
The student knows how to estimate the unconditional value-at-risk using empirical quantiles, parametric modeling, semiparametric modeling, and extreme value theory. The student knows also how to estimate the conditional value-at-risk using GARCH models. The student can read scientific articles about risk management.  

Contents:  
The course is an introduction to the quantitative risk management of a portfolio of stocks. The course introduces various risk measures, extreme value theory, and modeling of financial time series. The course covers:  
- conditional and unconditional loss distribution,  
- Value-at-Risk and other risk measures, standard methods of estimating  
- Value-at-Risk: multivariate normal modeling, historical simulation/empirical quantiles, and the Monte Carlo method,  
- modeling of distributions: multivariate distributions, normal mixture distributions, spherical and elliptical distributions, and dimension reduction,  
- modeling of financial time series: ARMA models, GARCH models, and volatility models, copulas and measures of dependence,  
- extreme value theory: block maxima and threshold exceedance methods.  

Mode of delivery:  
Face-to-face teaching  

Learning activities and teaching methods:  
Besides lectures, there are voluntary exercises.  

Target group:  
students of mathematical sciences, students of finance and economics  

Prerequisites and co-requisites:  
806113P Introduction to Statistics  

Recommended optional programme components:  
-  

Recommended or required reading:  

Assessment methods and criteria:  
Final exam  
Read more about assessment criteria at the University of Oulu webpage.  

Grading:  
1-5  

Person responsible:  

805309A: Statistical methods in epidemiology, 9 op

Voimassaolo: 01.06.2009 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lääärä Esa
Opintokohteen oppimateriaali:
Santos Silva, Isabel dos , , 1999
Clayton, David , , 1993
Rothman, Kenneth J. , , 1998
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805339A: The Statistical Foundation of Econometrics, 5 - 6 op

Voimassaolo: 01.06.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Hayashi, Fumio , , 2000
Gourieroux, Christian , , 1995
Gourieroux, Christian , , 1995
Harvey, Andrew C. , , 1990
Opintokohteen kielet: Finnish
Leikkaavuudet:

ECTS Credits:
5/6 cr

Learning outcomes:
The course familiarizes students with applications of statistical models when inferences are made on economic phenomena. The principles of statistical inference on economic phenomena are the same as those of general statistical inference but there are some special issues that make the inference different in economics than in other application areas of statistics. After finishing the course, a student can apply both linear regression and nonlinear regression and a student is able to apply the generalized method of moments as well as the method of instrumental variables. A student can diagnose the validity of the assumptions of the linear regression model and tune his inferences accordingly.

Contents:
The course starts with the study of the linear regression model, and covers asymptotic inference related to
the linear regression model, tests of the parameter restrictions and tests of a structural change. Besides
linear regression, also nonlinear regression and the generalized method of moments is covered, as well as
inference based on instrumental variables and problems stemming from measurement errors.
Inference under heteroscedasticity and autocorrelated disturbances is included. The basic theory of time
series analysis (cointegration and autoregressive conditional heteroscedasticity) and the basic theory of
panel data is included.

Recommended or required reading:
William H. Greene: Econometric Analysis (Prentice Hall)

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä

805332A: Design of experiments, 9 op
Voimassaolo: - 31.07.2007
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

805308A: Analysis of longitudinal data, 5 op
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Peter J. Diggle et al., , 2002
Hsiao, Cheng , , 2003
McCulloch, Charles E. , , 2001
Fitzmaurice, Garrett M. , , 2004
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
A student who has succesfully completed the course is supposed to
- be familiar with so-called mixed models for both discrete and continuous dependent variables
- be able to make use of these mixed models while studying longitudinal data

Contents:
The purpose of the course is to teach the students, how one can simultaneously study dependencies
between observed variables and variations between individuals in the panel. Linear and non-linear mixed
models, variograms and so-called growth curve models are introduced as central inferential tools for these
studies. Model diagnostics, dynamic ARX-type models and the GMM estimation principle also get a lot of
attention. A major part of the course deals with modelling continuous dependent variables, but cases of
qualitative, ordinal and count dependent variables are covered as well. The course can be taken either
as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of
excercises in the computer lab.

Assessment methods and criteria:
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Person responsible:**
Markku RAhiala

### 806357A: Statistical finance, 5 op

- **Voimassaolo:** 01.08.2010 -
- **Opiskelumuoto:** Intermediate Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opettajat:** Jussi Klemelä
- **Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

### 800698S: Pro gradu thesis, 30 op

- **Opiskelumuoto:** Advanced Studies
- **Laji:** Diploma thesis
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen kielet:** Finnish

**ECTS Credits:**
- 30 cr

**Language of instruction:**
- Finnish (also English)

**Learning outcomes:**
After writing the Master's degree, student has written an analytical and logical study of a problem or theory in a field of mathematics, applied mathematics or statistics. Completing the thesis successfully, student is able to write scientific articles and texts in mathematics.

**Contents:**
The scope of the Master's thesis is 20 cr for Teacher students and 30 cr in other disciplines. In Master's thesis, the student engages in researching a specific mathematical area or problem in the field of mathematics, applied mathematics or statistics.

**Mode of delivery:**
- Thesis

**Learning activities and teaching methods:**
- Own work, meetings with the supervisor

**Target group:**
- Major students

**Prerequisites and co-requisites:**
- Bachelor's degree (or equivalent), 20-50 cr advanced studies

**Recommended optional programme components:**
- 

**Recommended or required reading:**
- 

**Assessment methods and criteria:**
- Thesis

Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
- 1-5

**Person responsible:**
- Professors and other teaching personnel

**Working life cooperation:**
-
H325003: Mathematics, optional advanced studies, 0 - 120 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Electives

802653S: Lebesgue Measure and Integration Theory, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikael Lindström
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

801698S: Cryptography, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen oppimateriaali:
Trappe, Wade; Washington, Lawrence C., , 2005
Menezes, Alfred J.; van Oorschot, Paul C.; Vanstone, Scott A. , , 1997
Opintokohteen kielet: Finnish

Learning outcomes:
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

Contents:
In our lectures we study mathematical basics of encrypting, key exchange and signature systems. As examples, we mention elementary group and number theory used in primality tests and factoring, complexity estimates of computations-in particular in finite fields, repeated squaring and discrete logarithm in finite cyclic groups- applied in multiplicative groups of finite fields and addition groups of elliptic curves. Deduction of addition formulae in projective and affine Weierstrass elliptic curves. Diffie-Hellman key exchange, ElGamal encrypting and signature systems in finite cyclic groups applied in finite fields or in elliptic curves defined over finite fields. DSA, ECDSA, Massey-Omura. Some algorithms and tests: AKS, Fermat, Lenstra , Lucas, Miller-Rabin, Pohlig-Hellman, Pollard's p-1 and rho, pseudoprimes, quadratic sieve, Solovay-Strassen.
**Assessment methods and criteria:**
Read more about assessment criteria at the University of Oulu webpage.

**802655S: Continued Fractions, 5 op**

- **Voimassaolo:** 01.01.2011 -
- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen kielet:** Finnish

**Language of instruction:**
FI/EN

**Recommended or required reading:**
Kenneth H. Rosen: Elementary number theory and its applications.
Lisa Lorentzen and Haakon Waadeland: Continued Fractions with Applications (1992).
Oskar Perron: Die Lehre von den Kettenbruchen (1913).

Course material: http://cc.oulu.fi/~tma/OPETUS.html

**802644S: Introduction to Functional Analysis, 10 op**

- **Voimassaolo:** 01.08.2009 -
- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opettajat:** Mahmoud Filali
- **Opintokohteen kielet:** Finnish

**Learning outcomes:**
If we think of functional analysis as infinite dimensional linear algebra, then the course offers the tools and the ways to handle this infinite dimension. After completing the course successfully, the student will be able to follow almost any material on functional analysis.

**Contents:**
After recalling some basic definitions on linear algebra and giving the basic definitions concerning normed spaces, we present the uniform boundedness principle and the open mapping theorem. In this first part of the course, the relative compactness of the unit ball in a normed space is studied under the norm topology. Hahn-Banach Theorem is presented in its various forms: algebraic, analytic and geometric, and followed by Krein-Milman Theorem. We end up with the weak topology on normed spaces and the weak* topology on Banach duals. The relative compactness of the unit ball is studied with respect to these two topologies.

**Assessment methods and criteria:**
Read more about assessment criteria at the University of Oulu webpage.

**Person responsible:**
Mahmoud Filali

**802636S: Information Theory, 10 op**

- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail  
Opettajat: Lasse Holmström  
Opintokohteen oppimateriaali:  
Ash, Robert, , 1990 
Cover, Thomas M.; Joy, Thomas A., , 2006 
Gallager, Robert G., , 1968 
MacKay, David J. C., , 2003  
Opintokohteen kielet: Finnish

ECTS Credits:  
10 cr

Learning outcomes:  
On successful completion of this course, the student will be able to  
- explain the basic concepts and results of information theory  
- solve mathematical information theoretic problems  
- derive the central results of the theory

Contents:  
The course is an introduction Claude Shannon's mathematical theory of communication. The focus is on the information content of an information source, compression of information, coding, transmission of coded information through an information channel as well as decoding of the received message.

Assessment methods and criteria:  
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:  
Lasse Holmström

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802635S: Introduction to partial differential equations, 10 op

Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Valeriy Serov  
Opintokohteen oppimateriaali:  
Colton, David, , 1988 
Kress, Rainer, , 1999 
Folland, Gerald B., , 1995  
Opintokohteen kielet: Finnish

ECTS Credits:  
10 cr

Learning outcomes:  
On successful completion of this course, the student will be able to  
- solve linear and quasi-linear partial differential equations of first order using the method of characteristics  
- apply the method of separation of variables to solve initial-boundary value problems for heat, wave and Laplace equations  
- verify that a given function is a fundamental solution of a partial differential operator  
- use single and double layer potentials to solve boundary value problems for Laplacian

Contents:  
Linear and nonlinear equations of the first order, trigonometric Fourier series, Laplace equation in $\mathbb{R}^n$ and in bounded domains, potential theory, Green's function, Heat equation in $\mathbb{R}^n$ and in bounded domains, Wave equation in $\mathbb{R}^n$ and in bounded domains, d'Alembert formula for any dimensions, Fourier method.

Assessment methods and criteria:  
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:  

802652S: Hilbert Spaces, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
800624S Analysis III 10.0 op

ECTS Credits:
5 ECTS credits

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

800651S: Functional analysis, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish (English if neede)

Timing:
4-5 year of studies. Timig varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results in functional analysis.
- apply the results and methods of the course in various problems both in pure and applied mathematics.

Contents:
The course presents the theory of Banach and Hilbert spaces, Banach fixed point theorem, basic theory of
operators, Baire category theorem, principle of uniform boundedness, open mapping theorem, closed
graph theorem, Hahn-Banach theorem, compact operators and their spectrum.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 24h exercises

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies.

Recommended optional programme components:

Recommended or required reading:
Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mikael Lindström

Working life cooperation:
-

802629S: Function estimation, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström

Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods

Learning outcomes:
Upon completing the course the student will be able to
- characterise the basic features non-parametric function estimation methods
- apply such estimation methods to practical problems
- derive some of the basic results of non-parametric function estimation for kernel estimators

Contents:
The course focuses on the theory and practice of non-parametric function estimation with a special
emphasis on kernel methods. The particular functions considered are a probability density function and a
regression function.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical
background.

Prerequisites and co-requisites:
Calculus in one and several dimensions. Probability theory I. Probability theory II or Random variables and
distributions.

Recommended optional programme components:
No

Recommended or required reading:
Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the homework problems he/she has solved during the course. This is agreed in the beginning of the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

800674S: Fourier transform and distributions, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov

Opintokohteen oppimateriaali:
Stein, Elias M.; Shakarchi R., 2003
Taylor, Michael E., 1996
Grafakos Loukas, 2004
Stakgold, Ivar, 1998

Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
English

Timing:
4.-5. year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- calculate the Fourier transform of a given integrable function on the line
- perform basic operations, such as differentiation, convolution and Fourier transformation, on distributions
- use Fourier transform to find, and provide estimates for, fundamental solutions of partial differential operators
- formulate direct and inverse scattering problems for the Schrödinger operator

Contents:

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Euclidean topology, Series and integrals, Multidimensional analysis, Complex analysis I and II, and Linear algebra I and II.

**Recommended optional programme components:**
- 

**Recommended or required reading:**
Luentomoniste
L. Grafakos: Classical and Modern Fourier Analysis, Pearson Education, 2004;

**Assessment methods and criteria:**
Final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Valeriy Serov

**Working life cooperation:**
- 

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**802647S: Fourier series and the discrete Fourier transform, 10 op**

**Voimassaolo:** 01.01.2010 -
**Opiskelumuoto:** Advanced Studies
**Laji:** Course
**Vastuuysikkö:** Department of Mathematical Sciences
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Valeriy Serov

**Opintokohteen kielet:** English

Ei opintojaksokuvauksia.

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**802656S: Algebraic numbers, 5 op**

**Voimassaolo:** 01.01.2012 -
**Opiskelumuoto:** Advanced Studies
**Laji:** Course
**Vastuuysikkö:** Department of Mathematical Sciences
**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen kielet:** Finnish

**Language of instruction:**
FI/EN

**Learning outcomes:**
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding.
When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

**Contents:**
First we revise some basics of rings and fields which are needed to proceed ahead field extensions. In particular, divisibility in an integral domain is carefully studied yielding to applications in the theory of polynomial algebra and algebraic integers. The theory of algebraic numbers is strongly based on polynomial algebra, where the properties of zeros and divisibility of polynomials are considered. The definition of an algebraic number will be generalized to the algebraic elements of field extensions going forward to algebraic fields. Considered as most important algebraic fields we get number fields which are finitely generated subfields of the field $A$ of all complex algebraic numbers. In particular, we study quadratic number fields. Further, we shall consider the divisibility and factorization of algebraic integers with some applications to Diophantine equations.

**Prerequisites and co-requisites:**
Algebra I and II, Linear algebra I and II, Basics in Number Theory (Number theory I)

**Recommended or required reading:**
I.N. Stewart and D.O. Tall: Algebraic number theory.
Daniel Marcus: Number fields.
J.B. Fraleigh: Abstract algebra.
Michael Artin: Algebra.

Course material: http://cc.oulu.fi/~tma/OPETUS.html

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802637S: Advanced Problem Solving, 2 - 6 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Peter Hästö  
**Opintokohteen kiele:** English

**Assessment methods and criteria:**
Read more about [assessment criteria](http://cc.oulu.fi/~tma/OPETUS.html) at the University of Oulu webpage.

802645S: Number Theory A, 5 op

**Voimassaolo:** 01.08.2009 -  
**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Tapani Matala-aho  
**Opintokohteen kiele:** Finnish

Ei opintojakosokuvauksia.

802646S: Number Theory B, 5 op

**Voimassaolo:** 01.08.2009 -  
**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Tapani Matala-aho  
**Opintokohteen kiele:** Finnish
802631S: Modern real analysis, 10 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish

**Learning outcomes:**  
On successful completion of this course, the student will be able to  
- derive and prove basic results of modern real analysis.  
- apply the results and methods of modern real analysis in different topics of mathematics, like in the theory of partial differential equations.

**Contents:**  
The course presents Lebesgue spaces (Hölder’s and Minkowski’s inequalities, completeness, dual spaces), the Vitali covering theorem, the Hardy-Littlewood maximal function, approximation with smooth functions using convolution, Lebesgue’s density theorem, Sobolev’s inequalities.

**Assessment methods and criteria:**  
Read more about [assessment criteria](#) at the University of Oulu webpage.

800688S: Theory of Optimization, 10 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Erkki Laitinen  
**Opintokohteen oppimateriaali:**  
Luenberger, David G., 1984  
Peressini, Anthony L., 1988  
**Opintokohteen kielet:** Finnish

**Learning outcomes:**  
On successful completion of this course, the student will be able to  
- identify the correct methods for solving the conventional optimization problems  
- implement the most typical numerical algorithms for solving linear and nonlinear optimization problems

**Contents:**  
The lecture course is focused to methods, which can apply for solving essential optimization problems of technical and economical sciences. The lectures consist of following topics: Linear programming, convex sets and functions and nonlinear convex optimization. The topics are considered theoretically and also numerical algorithms for problem solution are presented.

**Mode of delivery:**  
Face-to-face teaching
Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Euclidean topology, Series and integrals, and Linear algebra I and II

Recommended optional programme components:

Recommended or required reading:

Assessment methods and criteria:
Mid-term exam or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Erkki Laitinen

Working life cooperation:

800660S: Group Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Niemenmaa Markku
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
4-5 year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- use different proving techniques related to the theory
- prove the Sylow theorems and deal with their applications
- prove important results in the theory of finite solvable groups

Contents:
Aim: To provide the student with the basics of group theory and its development during the past hundred years. Basics of group theory, permutations, studies on the arithmetical

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 56 h, exercises 28 h.

Target group:
Major students
Prerequisites and co-requisites:
802355A Number theory and groups
802355A Rings, Fields and polynomials
800343A Permutations, fields and Galois' theory

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Mid-term exam or final exam.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Markku Niemenmaa

Working life cooperation:
-

802633S: Statistical Pattern Recognition, 10 op

Opiskeluomotto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen oppimateriaali:
Duda, Richard O.,, 2001
Theodoridis, Sergios,, 2002
Webb, A. R, , 2002
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods.

Learning outcomes:
Upon completing the course the student will
-be familiar with the most common classifiers used in pattern recognition
-be able to apply pattern recognition methods to practical problems
-be able derive some of the basic mathematical results of pattern recognition theory

Contents:
The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

**Prerequisites and co-requisites:**
Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

**Recommended or required reading:**
Lecture notes.
Optional reading:

**Assessment methods and criteria:**
Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

**Grading:**
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

**Person responsible:**
Lasse Holmström

**Working life cooperation:**
No

**Other information:**
No

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**801643S: Topology, 10 op**

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Mahmoud Filali

**Opintokohteen kielet:** Finnish

**ECTS Credits:**
10 cr

**Language of instruction:**
English (also Finnish)

**Timing:**
3.-5. year of studies. Timing varies.

**Learning outcomes:**
After completion of the course, the student should be able to follow more advanced courses or seminars on abstract harmonic analysis.

**Contents:**
This is an advanced course, aimed to final year students and to postgraduate students. The course covers topological groups and their uniform structures; subgroups, Quotient groups and product groups; and invariant pseudo-metrics on groups. The last part of the course presents some basics on compact semigroups with some examples such as Ellis group and semigroup compactifications

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
56h lectures, 28h exercises

**Target group:**
Major students
Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics, 800329A Topologia I

Recommended optional programme components:
- 

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Mid-term exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mahmoud Filai

802651S: Measure and Integration, 5 op
Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802650S: Fractal Geometry, 10 op
Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Esa Järvenpää
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802660S: Operator theory and integral equations, 10 op
Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen kielet: English

Ei opintojaksokuvauksia.
Electives

805609S: Statistical methods in epidemiology, 9 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen oppimateriaali:
Santos Silva, Isabel dos, 1999
Clayton, David, 1993
Rothman, Kenneth J., 1998
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805646S: Analysis of longitudinal data, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Peter J. Diggle et al., 2002
Hsiao, Cheng, 2003
McCulloch, Charles E., 2001
Fitzmaurice, Garrett M., 2004
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
A student who has succesfully completed the course is supposed to
- be familiar with so-called mixed models for both discrete and continuous dependent variables
- be able to make use of these mixed models while studying longitudinal data

Contents:
The purpose of the course is to teach the students, how one can simultaneously study dependencies between observed variables and variations between individuals in the panel. Linear and non-linear mixed models, variograms and so-called growth curve models are introduced as central inferential tools for these studies. Model diagnostics, dynamic ARX-type models and the GMM estimation principle also get a lot of attention. A major part of the course deals with modelling continuous dependent variables, but cases of
qualitative, ordinal and count dependent variables are covered as well. The course can be taken either as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of exercises in the computer lab.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä

805679S: Time series analysis, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C. , , 1993
Lütkepohl, Helmut , , 1991
Hamilton, James D. , , 1994
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply computer programs to fit time series models. Furthermore, a student learns to read scientific articles about time series.

Contents:
The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH). Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

Recommended or required reading:

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä

805683S: The Statistical Foundation of Econometrics, 5 - 6 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C. , , 1990
The statistical foundations of econometrics

**ECTS Credits:**
5/6 cr

**Language of instruction:**
Finnish

**Learning outcomes:**
The course familiarizes students with applications of statistical models when inferences are made on economic phenomena. The principles of statistical inference on economic phenomena are the same as those of general statistical inference but there are some special issues that make the inference different in economics than in other application areas of statistics. After finishing the course, a student can apply both linear regression and nonlinear regression and a student is able to apply the generalized method of moments as well as the method of instrumental variables. A student can diagnose the validity of the assumptions of the linear regression model and tune his inferences accordingly.

**Contents:**
The course starts with the study of the linear regression model, and covers asymptotic inference related to the linear regression model, tests of the parameter restrictions and tests of a structural change. Besides linear regression, also nonlinear regression and the generalized method of moments is covered, as well as inference based on instrumental variables and problems stemming from measurement errors. Inference under heteroscedasticity and autocorrelated disturbances is included. The basic theory of time series analysis (cointegration and autoregressive conditional heteroscedasticity) and the basic theory of panel data is included.

**Recommended or required reading:**
William H. Greene: Econometric Analysis (Prentice Hall)

**Assessment methods and criteria:**
Read more about assessment criteria at the University of Oulu webpage.

**Person responsible:**
Jussi Klemelä.
806618S: Computationally intensive statistical methods, 9 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806621S: Spatial Data Analysis, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806628S: Statistical Finance, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettaja: Jussi Klemelä
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806629S: Introduction to Sampling Methods, 4 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettaja: Läära Esa
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806630S: Market Risk Analysis, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettaja: Jussi Klemelä
Opintokohteen kielet: Finnish
Leikkaavuudet:

806330A Analysis of Market Risk 5.0 op
ECTS Credits: 5 cr

Language of instruction: Finnish

Timing: 3. year of studies or later. Timing varies.

Learning outcomes:
The student knows how to estimate the unconditional value-at-risk using empirical quantiles, parametric modeling, semiparametric modeling, and extreme value theory. The student knows also how to estimate the conditional value-at-risk using GARCH models. The student can read scientific articles about risk management.

Contents:
The course is an introduction to the quantitative risk management of a portfolio of stocks. The course introduces various risk measures, extreme value theory, and modeling of financial time series. The course covers:
- conditional and unconditional loss distribution,
- Value-at-Risk and other risk measures, standard methods of estimating
- Value-at-Risk: multivariate normal modeling, historical simulation/empirical quantiles, and the Monte Carlo method,
- modeling of distributions: multivariate distributions, normal mixture distributions, spherical and elliptical distributions, and dimension reduction,
- modeling of financial time series: ARMA models, GARCH models, and volatility models, copulas and measures of dependence,
- extreme value theory: block maxima and threshold exceedance methods.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises.

Target group:
students of mathematical sciences, students of finance and economics

Prerequisites and co-requisites:
806113P Introduction to Statistics

Recommended optional programme components:
-

Recommended or required reading:

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
Home page of the course is http://cc.oulu.fi/~jklemela/marketrisk/

805651S: Stochastic processes, 10 op
806622S: Probability, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

805611S: Mathematical statistics II, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Opettajat: Jussi Klemelä

Opintokohteen oppimateriaali:
Lehmann, E. L. , 2001
Migon, H. S. , 1999

Leikkaavuudet:
805627S  Theory of Statistical Inference  5.0 op

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

800698S: Pro gradu thesis, 30 op

Opiskelumuoto: Advanced Studies
Laji: Diploma thesis
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
30 cr
Language of instruction:
Finnish (also English)

Learning outcomes:
After writing the Master's degree, student has written an analytical and logical study of a problem or theory in a field of mathematics, applied mathematics or statistics. Completing the thesis successfully, student is able to write scientific articles and texts in mathematics.

Contents:
The scope of the Master's thesis is 20 cr for Teacher students and 30 cr in other disciplines. In Master's thesis, the student engages in researching a specific mathematical area or problem in the field of mathematics, applied mathematics or statistics.
Mode of delivery:
Thesis

Learning activities and teaching methods:
Own work, meetings with the supervisor

Target group:
Major students

Prerequisites and co-requisites:
Bachelor's degree (or equivalent), 20-50 cr advanced studies

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Thesis
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Professors and other teaching personnel

Working life cooperation:
-

H325003: Mathematics, optional advanced studies, 0 - 120 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Electives

802653S: Lebesgue Measure and Integration Theory, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikael Lindström
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

801698S: Cryptography, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen oppimateriaali:
Trappe, Wade; Washington, Lawrence C., , 2005
Learning outcomes:
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

Contents:
In our lectures we study mathematical basics of encrypting, key exchange and signature systems. As examples, we mention elementary group and number theory used in primality tests and factoring, complexity estimates of computations-in particular in finite fields, repeated squaring and discrete logarithm in finite cyclic groups- applied in multiplicative groups of finite fields and addition groups of elliptic curves. Deduction of addition formulae in projective and affine Weierstrass elliptic curves. Diffie-Hellman key exchange, ElGamal encrypting and signature systems in finite cyclic groups applied in finite fields or in elliptic curves defined over finite fields. DSA, ECDSA, Massey-Omura. Some algorithms and tests: AKS, Fermat, Lenstra, Lucas, Miller-Rabin, Pohlig-Hellman, Pollard's p-1 and rho, pseudoprimes, quadratic sieve, Solovay-Grassen.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802655S: Continued Fractions, 5 op

Voimassaolo: 01.01.2011 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Language of instruction:
FI/EN

Recommended or required reading:
Kenneth H. Rosen: Elementary number theory and its applications.
Lisa Lorentzen and Haakon Waadeland: Continued Fractions with Applications (1992).
Oskar Perron: Die Lehre von den Kettenbruchen (1913).

Course material: http://cc.oulu.fi/~tma/OPETUS.html

802644S: Introduction to Functional Analysis, 10 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettaja: Mahmoud Filali
Opintokohteen kielet: Finnish

Learning outcomes:
If we think of functional analysis as infinite dimensional linear algebra, then the course offers the tools and the ways to handle this infinite dimension. After completing the course successfully, the student will be able to follow almost any material on functional analysis.

Contents:
After recalling some basic definitions on linear algebra and giving the basic definitions concerning normed spaces, we present the uniform boundedness principle and the open mapping theorem. In this first part of the course, the relative compactness of the unit ball in a normed space is studied under the norm topology. Hahn-Banach Theorem is presented in its various forms: algebraic, analytic and geometric, and followed by Krein-Milman Theorem. We end up with the weak topology on normed spaces and the weak* topology on Banach duals. The relative compactness of the unit ball is studied with respect to these two topologies.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Mahmoud Filali

802636S: Information Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen oppimateriaali:
Ash, Robert, , 1990
Cover, Thomas M.; Joy, Thomas A., , 2006
Gallager, Robert G., , 1968
MacKay, David J. C., , 2003
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Learning outcomes:
On successful completion of this course, the student will be able to
- explain the basic concepts and results of information theory
- solve mathematical information theoretic problems
- derive the central results of the theory

Contents:
The course is an introduction Claude Shannon's mathematical theory of communication. The focus is on the information content of an information source, compression of information, coding, transmission of coded information through an information channel as well as decoding of the received message.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Lasse Holmström

802635S: Introduction to partial differential equations, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen oppimateriaali:
**Colton, David**, , 1988
**Kress, Rainer**, , 1999
**Folland, Gerald B.**, , 1995

**Opintokohteen kielet**: Finnish

**ECTS Credits:**
10 cr

**Learning outcomes:**
On successful completion of this course, the student will be able to
- solve linear and quasi-linear partial differential equations of first order using the method of characteristics
- apply the method of separation of variables to solve initial-boundary value problems for heat, wave and Laplace equations
- verify that a given function is a fundamental solution of a partial differential operator
- use single and double layer potentials to solve boundary value problems for Laplacian

**Contents:**
Linear and nonlinear equations of the first order, trigonometric Fourier series, Laplace equation in $\mathbb{R}^n$ and in bounded domains, potential theory, Green's function, Heat equation in $\mathbb{R}^n$ and in bounded domains, Wave equation in $\mathbb{R}^n$ and in bounded domans, d'Alembert formula for any dimensions, Fourier method.

**Assessment methods and criteria:**
Read more about [assessment criteria] at the University of Oulu webpage.

**Person responsible:**
Valeriy Serov

802652S: Hilbert Spaces, 5 op

**Voimassaolo**: 01.08.2010 -
**Opiskelumuoto**: Advanced Studies
**Laji**: Course
**Vastuuysikkö**: Department of Mathematical Sciences
**Arvostelu**: 1 - 5, pass, fail
**Opintokohteen kielet**: Finnish

**Leikkaavuudet:**
- 800624S Analysis III 10.0 op

**ECTS Credits:**
5 ECTS credits

**Assessment methods and criteria:**
Read more about [assessment criteria] at the University of Oulu webpage.

800651S: Functional analysis, 10 op

**Opiskelumuoto**: Advanced Studies
**Laji**: Course
**Vastuuysikkö**: Department of Mathematical Sciences
**Arvostelu**: 1 - 5, pass, fail
**Opintokohteen kielet**: Finnish

**ECTS Credits:**
10 cr

**Language of instruction:**
Finnish (English if neede)

**Timing:**
4-5 year of studies. Timing varies.
Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results in functional analysis.
- apply the results and methods of the course in various problems both in pure and applied mathematics.

Contents:
The course presents the theory of Banach and Hilbert spaces, Banach fixed point theorem, basic theory of operators, Baire category theorem, principle of uniform boundedness, open mapping theorem, closed graph theorem, Hahn-Banach theorem, compact operators and their spectrum.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 24h exercises

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies.

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mikael Lindström

Working life cooperation:
-

802629S: Function estimation, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods

Learning outcomes:
Upon completing the course the student will be able to
- characterise the basic features non-parametric function estimation methods
- apply such estimation methods to practical problems
- derive some of the basic results of non-parametric function estimation for kernel estimators

Contents:
The course focuses on the theory and practice of non-parametric function estimation with a special emphasis on kernel methods. The particular functions considered are a probability density function and a regression function.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions. Probability theory I. Probability theory II or Random variables and distributions.

Recommended optional programme components:
No

Recommended or required reading:
Lecture notes written by the instructor.

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the homework problems he/she has solved during the course. This is agreed in the beginning of the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

800674S: Fourier transform and distributions, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov

Opintokohteen oppimateriaali:
Stein, Elias M.; Shakarchi R., , 2003
Taylor, Michael E., , 1996
Grafakos Loukas, , 2004
Stakgold, Ivar , , 1998

Opintokohteen kieleet: Finnish

ECTS Credits:
10 cr

Language of instruction:
English
Timing:
4.-5. year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- calculate the Fourier transform of a given integrable function on the line
- perform basic operations, such as differentiation, convolution and Fourier transformation, on distributions
- use Fourier transform to find, and provide estimates for, fundamental solutions of partial differential operators
- formulate direct and inverse scattering problems for the Schrödinger operator

Contents:

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Euclidean topology, Series and integrals, Multidimensional analysis, Complex analysis I and II, and Linear algebra I and II.

Recommended optional programme components:
-

Recommended or required reading:
Luentomoniste
L. Grafakos: Classical and Modern Fourier Analysis, Pearson Education, 2004;

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Valeriy Serov

Working life cooperation:
-

802647S: Fourier series and the discrete Fourier transform, 10 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen kielet: English

Ei opintojaksokuvauksia.
Learning outcomes:
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed: For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

Contents:
First we revise some basics of rings and field which are needed to proceed ahead field extensions. In particular, divisibility in an integral domain is carefully studied yielding to applications in the theory of polynomial algebra and algebraic integers. The theory of algebraic numbers is strongly based on polynomial algebra, where the properties of zeros and divisibility of polynomials are considered. The definition of an algebraic number will be generalized to the algebraic elements of field extensions going forward to algebraic fields. Considered as most important algebraic fields we get number fields which are finitely generated subfields of the field of all complex algebraic numbers. In particular, we study quadratic number fields. Further, we shall consider the divisibility and factorization of algebraic integers with some applications to Diophantine equations.

Prerequisites and co-requisites:
Algebra I and II, Linear algebra I and II, Basics in Number Theory (Number theory I)

Recommended or required reading:
I.N. Stewart and D.O. Tall: Algebraic number theory.
Daniel Marcus: Number fields.
J.B. Fraleigh: Abstract algebra.
Michael Artin: Algebra.

Course material: http://cc.oulu.fi/~tma/OPETUS.html

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.
802645S: Number Theory A, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802646S: Number Theory B, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802631S: Modern real analysis, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results of modern real analysis.
- apply the results and methods of modern real analysis in different topics of mathematics, like in the theory of partial differential equations.

Contents:
The course presents Lebesgue spaces (Hölder’s and Minkowski’s inequalities, completeness, dual spaces), the Vitali covering theorem, the Hardy-Littlewood maximal function, approximation with smooth functions using convolution, Lebesgue’s density theorem, Sobolev’s inequalities.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

800688S: Theory of Optimization, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Erkki Laitinen
Opintokohteen oppimateriaali:
Luenberger, David G., , 1984
Peressini, Anthony L., , 1988
Opintokohteen kielet: Finnish
Leikkaavuudet:
802666S  Linear Optimization  5.0 op

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
4.-5. year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- identify the correct methods for solving the conventional optimization problems
- implement the most typical numerical algorithms for solving linear and nonlinear optimization problems

Contents:
The lecture course is focused to methods, which can apply for solving essential optimization problems of
technical and economical sciences. The lectures consist of following topics: Linear programming, convex
sets and functions and nonlinear convex optimization. The topics are considered theoretically and also
numerical algorithms for problem solution are presented.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Euclidean topology, Series and integrals, and Linear algebra I and II

Recommended optional programme components:
-

Recommended or required reading:

Assessment methods and criteria:
Mid-term exam or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Erkki Laitinen

Working life cooperation:
-

800660S: Group Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Niemenmäki Markku
Opintokohteen kielet: Finnish
ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
4-5 year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- use different proving techniques related to the theory
- prove the Sylow theorems and deal with their applications
- prove important results in the theory of finite solvable groups

Contents:
Aim: To provide the student with the basics of group theory and its development during the past hundred
years. Basics of group theory, permutations, studies on the arithmetical

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 56 h, exercises 28 h.

Target group:
Major students

Prerequisites and co-requisites:
802355A Number theory and groups
802355A Rings, Fields and polynomials
800343A Permutations, fields and Galois' theory

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Mid-term exam or final exam.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Markku Niemennmaa

Working life cooperation:
-

802633S: Statistical Pattern Recognition, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen oppimateriaali:
Duda, Richard O., , 2001
Theodoridis, Sergios , , 2002
Webb, A. R , , 2002
Opintokohteen kielet: Finnish
ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods.

Learning outcomes:
Upon completing the course the student will
- be familiar with the most common classifiers used in pattern recognition
- be able to apply pattern recognition methods to practical problems
- be able derive some of the basic mathematical results of pattern recognition theory

Contents:
The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

Recommended or required reading:
Lecture notes.
Optional reading:

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No
ECTS Credits:  
10 cr  
Language of instruction:  
English (also Finnish)  
Timing:  
3.-5. year of studies. Timing varies.  
Learning outcomes:  
After completion of the course, the student should be able to follow more advanced courses or seminars on abstract harmonic analysis.  
Contents:  
This is an advanced course, aimed to final year students and to postgraduate students. The course covers topological groups and their uniform structures; subgroups, Quotient groups and product groups; and invariant pseudo-metrics on groups. The last part of the course presents some basics on compact semigroups with some examples such as Ellis group and semigroup compactifications  
Mode of delivery:  
Face-to-face teaching  
Learning activities and teaching methods:  
56h lectures, 28h exercises  
Target group:  
Major students  
Prerequisites and co-requisites:  
Compulsory basic and intermediate studies in mathematics, 800329A Topologia I  
Recommended optional programme components:  
-  
Recommended or required reading:  
Lecture notes  
Assessment methods and criteria:  
Mid-term exams or final exam  
Read more about assessment criteria at the University of Oulu webpage.  
Grading:  
1-5  
Person responsible:  
Mahmoud Filai  

802651S: Measure and Integration, 5 op  
Voimassaolo: 01.08.2010 -  
Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish  
Assessment methods and criteria:  
Read more about assessment criteria at the University of Oulu webpage.  

802650S: Fractal Geometry, 10 op  
Voimassaolo: 01.01.2010 -  
Opiskelumuoto: Advanced Studies
802660S: Operator theory and integral equations, 10 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Esa Järvenpää
Opintokohteen kiele: English

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

H326603: Statistics optional advanced studies, 0 - 120 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kiele: Finnish

Ei opintojaksokuvauksia.

Electives

805609S: Statistical methods in epidemiology, 9 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärå Esa
Opintokohteen oppimateriaali:
Santos Silva, Isabel dos, 1999
Clayton, David, 1993
Rothman, Kenneth J., 1998
Opintokohteen kiele: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805646S: Analysis of longitudinal data, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
ECTS Credits:
5 cr

Learning outcomes:
A student who has successfully completed the course is supposed to
- be familiar with so-called mixed models for both discrete and continuous dependent variables
- be able to make use of these mixed models while studying longitudinal data

Contents:
The purpose of the course is to teach the students, how one can simultaneously study dependencies between observed variables and variations between individuals in the panel. Linear and non-linear mixed models, variograms and so-called growth curve models are introduced as central inferential tools for these studies. Model diagnostics, dynamic ARX-type models and the GMM estimation principle also get a lot of attention. A major part of the course deals with modelling continuous dependent variables, but cases of qualitative, ordinal and count dependent variables are covered as well. The course can be taken either as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of exercises in the computer lab

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä

805679S: Time series analysis, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C. , , 1993
Lütkepohl, Helmut , , 1991
Hamilton, James D. , , 1994
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply computer programs to fit time series models. Furthermore, a student learns to read scientific articles about time series.

Contents:
The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram.
Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH). Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

**Recommended or required reading:**
A. Harvey: Time Series Models, Philip Allan (2. painos)
H. Lutkepohl: Introduction to Multiple Time Series Analysis, Springer (2. painos)
J. Hamilton: Time Series, Princeton University Press
The MIT Press.

**Assessment methods and criteria:**
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Person responsible:**
Jussi Klemelä

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**805683S: The Statistical Foundation of Econometrics, 5 - 6 op**

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuksikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Jussi Klemelä

**Opintokohteen oppimateriaali:**
Harvey, Andrew C., , 1990
Hayashi, Fumio , , 2000
Gourieroux, Christian , , 1995
Gourieroux, Christian , , 1995

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
805339A The statistical foundations of econometrics 5.0 op

**ECTS Credits:**
5/6 cr

**Language of instruction:**
Finnish

**Learning outcomes:**
The course familiarizes students with applications of statistical models when inferences are made on economic phenomena. The principles of statistical inference on economic phenomena are the same as those of general statistical inference but there are some special issues that make the inference different in economics than in other application areas of statistics. After finishing the course, a student can apply both linear regression and nonlinear regression and a student is able to apply the generalized method of moments as well as the method of instrumental variables. A student can diagnose the validity of the assumptions of the linear regression model and tune his inferences accordingly.

**Contents:**
The course starts with the study of the linear regression model, and covers asymptotic inference related to the linear regression model, tests of the parameter restrictions and tests of a structural change. Besides linear regression, also nonlinear regression and the generalized method of moments is covered, as well as inference based on instrumental variables and problems stemming from measurement errors. Inference under heteroscedasticity and autocorrelated disturbances is included. The basic theory of time series analysis (cointegration and autoregressive conditional heteroscedasticity) and the basic theory of panel data is included.

**Recommended or required reading:**
William H. Greene: Econometric Analysis (Prentice Hall)

**Assessment methods and criteria:**
Read more about [assessment criteria](#) at the University of Oulu webpage.
Person responsible:
Jussi Klemelä.

805681S: Generalized Linear Models, 9 op

Opiskelu穆oto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

805699S: Statistical methods in epidemiology, 8 op

Opiskelu穆oto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806618S: Computationally intensive statistical methods, 9 op

Opiskelu穆oto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806621S: Spatial Data Analysis, 10 op

Opiskelu穆oto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806628S: Statistical Finance, 5 op

Voimassaolo: 01.08.2009 -
Opiskelu穆oto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.
806629S: Introduction to Sampling Methods, 4 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lääärä Esa
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806630S: Market Risk Analysis, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen kielet: Finnish
Leikkaavuudet:

806330A Analysis of Market Risk 5.0 op

ECTS Credits:
5 cr
Language of instruction:
Finnish
Timing:
3. year of studies or later. Timing varies.
Learning outcomes:
The student knows how to estimate the unconditional value-at-risk using empirical quantiles, parametric modeling, semiparametric modeling, and extreme value theory. The student knows also how to estimate the conditional value-at-risk using GARCH models. The student can read scientific articles about risk management.

Contents:
The course is an introduction to the quantitative risk management of a portfolio of stocks. The course introduces various risk measures, extreme value theory, and modeling of financial time series. The course covers:

- conditional and unconditional loss distribution,
- Value-at-Risk and other risk measures, standard methods of estimating
- Value-at-Risk: multivariate normal modeling, historical simulation/empirical quantiles, and the Monte Carlo method,
- modeling of distributions: multivariate distributions, normal mixtures, and spherical and elliptical distributions, and dimension reduction,
- modeling of financial time series: ARMA models, GARCH models, and volatility models, copulas and measures of dependence,
- extreme value theory: block maxima and threshold exceedance methods.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises.

Target group:
students of mathematical sciences, students of finance and economics

**Prerequisites and co-requisites:**
806113P Introduction to Statistics

**Recommended optional programme components:**
- 

**Recommended or required reading:**

**Assessment methods and criteria:**
Final exam
Read more about [assessment criteria](http://cc.oulu.fi/~jklemla/marketrisk/) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Jussi Klemelä

**Working life cooperation:**
-

**Other information:**
Home page of the course is [http://cc.oulu.fi/~jklemla/marketrisk/](http://cc.oulu.fi/~jklemla/marketrisk/)

### 805651S: Stochastic processes, 10 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish  

Ei opintojaksokuvauksia.

### 806622S: Probability, 10 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish  

Ei opintojaksokuvauksia.

### 805611S: Mathematical statistics II, 10 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Jussi Klemelä  
**Opintokohteen oppimateriaali:**  
Lehmann, E. L., 2001  
Migon, H. S., 1999  
**Opintokohteen kielet:** Finnish  
**Leikkaavuudet:**
**Assessment methods and criteria:**
Read more about assessment criteria at the University of Oulu webpage.

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### 800698S: Pro gradu thesis, 30 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Diploma thesis  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kiele:** Finnish

**ECTS Credits:**
30 cr

**Language of instruction:**
Finnish (also English)

**Learning outcomes:**
After writing the Master's degree, student has written an analytical and logical study of a problem or theory in a field of mathematics, applied mathematics or statistics. Completing the thesis successfully, student is able to write scientific articles and texts in mathematics.

**Contents:**
The scope of the Master's thesis is 20 cr for Teacher students and 30 cr in other disciplines. In Master's thesis, the student engages in researching a specific mathematical area or problem in the field of mathematics, applied mathematics or statistics.

**Mode of delivery:**
Thesis

**Learning activities and teaching methods:**
Own work, meetings with the supervisor

**Target group:**
Major students

**Prerequisites and co-requisites:**
Bachelor's degree (or equivalent), 20-50 cr advanced studies

**Recommended optional programme components:**
-

**Recommended or required reading:**
-

**Assessment methods and criteria:**
Thesis  
Read more about assessment criteria at the University of Oulu webpage.  
**Grading:**
1-5

**Person responsible:**
Professors and other teaching personnel

**Working life cooperation:**
-

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### H325003: Mathematics, optional advanced studies, 0 - 120 op

**Voimassaolo:** 01.08.2010 -  
**Opiskelumuoto:** Advanced Studies  
**Laji:** Study module  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kiele:** Finnish

Ei opintojaksokuvauksia.

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*Electives*
**802653S: Lebesgue Measure and Integration Theory, 5 op**

*Voimassaolo:* 01.08.2010 -  
*Opiskelumuoto:* Advanced Studies  
*Laji:* Course  
*Vastuuysikkö:* Department of Mathematical Sciences  
*Arvostelu:* 1 - 5, pass, fail  
*Opettajat:* Mikael Lindström  
*Opintokohteen kielet:* Finnish

**Assessment methods and criteria:**  
Read more about [assessment criteria](#) at the University of Oulu webpage.

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**801698S: Cryptography, 5 op**

*Opiskelumuoto:* Advanced Studies  
*Laji:* Course  
*Vastuuysikkö:* Department of Mathematical Sciences  
*Arvostelu:* 1 - 5, pass, fail  
*Opettajat:* Tapani Matala-aho  
*Opintokohteen oppimateriaali:*  
Trappe, Wade; Washington, Lawrence C., , 2005  
Menezes, Alfred J.; van Oorschot, Paul C.; Vanstone, Scott A., , 1997  
*Opintokohteen kielet:* Finnish

**Learning outcomes:**  
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed: For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

**Contents:**  
In our lectures we study mathematical basics of encrypting, key exchange and signature systems. As examples, we mention elementary group and number theory used in primality tests and factoring, complexity estimates of computations-in particular in finite fields, repeated squaring and discrete logarithm in finite cyclic groups- applied in multiplicative groups of finite fields and addition groups of elliptic curves. Deduction of addition formulae in projective and affine Weierstrass elliptic curves. Diffie-Hellman key exchange, ElGamal encrypting and signature systems in finite cyclic groups applied in finite fields or in elliptic curves defined over finite fields. DSA, ECDSA, Massey-Omura. Some algorithms and tests: AKS, Fermat, Lenstra, Lucas, Miller-Rabin, Pohlig-Hellman, Pollard’s p-1 and rho, pseudoprimes, quadratic sieve, Solovay-Srassen.

**Assessment methods and criteria:**  
Read more about [assessment criteria](#) at the University of Oulu webpage.

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**802655S: Continued Fractions, 5 op**

*Voimassaolo:* 01.01.2011 -  
*Opiskelumuoto:* Advanced Studies  
*Laji:* Course  
*Vastuuysikkö:* Department of Mathematical Sciences  
*Arvostelu:* 1 - 5, pass, fail  
*Opintokohteen kielet:* Finnish
Language of instruction:
FI/EN

Recommended or required reading:
Kenneth H. Rosen: Elementary number theory and its applications.
Lisa Lorentzen and Haakon Waadeland: Continued Fractions with Applications (1992).
Oskar Perron: Die Lehre von den Kettenbruchen (1913).

Course material: http://cc.oulu.fi/~tma/OPETUS.html

802644S: Introduction to Functional Analysis, 10 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Mahmoud Filali
Opintokohteen kielet: Finnish

Learning outcomes:
If we think of functional analysis as infinite dimensional linear algebra, then the course offers the tools and the ways to handle this infinite dimension. After completing the course successfully, the student will be able to follow almost any material on functional analysis.

Contents:
After recalling some basic definitions on linear algebra and giving the basic definitions concerning normed spaces, we present the uniform boundedness principle and the open mapping theorem. In this first part of the course, the relative compactness of the unit ball in a normed space is studied under the norm topology. Hahn-Banach Theorem is presented in its various forms: algebraic, analytic and geometric, and followed by Krein-Milman Theorem. We end up with the weak topology on normed spaces and the weak* topology on Banach duals. The relative compactness of the unit ball is studied with respect to these two topologies.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Mahmoud Filali

802636S: Information Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen oppimateriaali:
Ash, Robert , , 1990
Cover, Thomas M.; Joy, Thomas A., , 2006
Gallager, Robert G., , 1968
MacKay, David J. C., , 2003
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr
Learning outcomes:
On successful completion of this course, the student will be able to
- explain the basic concepts and results of information theory
- solve mathematical information theoretic problems
- derive the central results of the theory

Contents:
The course is an introduction Claude Shannon's mathematical theory of communication. The focus is on
the information content of an information source, compression of information, coding, transmission of
coded information through an information channel as well as decoding of the received message.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Lasse Holmström

802635S: Introduction to partial differential equations, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen oppimateriaali:
Colton, David, , 1988
Kress, Rainer, , 1999
Folland, Gerald B. , , 1995
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Learning outcomes:
On successful completion of this course, the student will be able to
- solve linear and quasi-linear partial differential equations of first order using the method of characteristics
- apply the method of separation of variables to solve initial-boundary value problems for heat, wave and
  Laplace equations
- verify that a given function is a fundamental solution of a partial differential operator
- use single and double layer potentials to solve boundary value problems for Laplacian

Contents:
Linear and nonlinear equations of the first order, trigonometric Fourier series, Laplace equation in R^n and
in bounded domains, potential theory, Green's function, Heat equation in R^n and in bounded domains,
Wave equation in R^n and in bounded domans, d'Alembert formula for any dimensions, Fourier method.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Valeriy Serov

802652S: Hilbert Spaces, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
800624S  Analysis III  10.0 op

ECTS Credits:
5 ECTS credits

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

800651S: Functional analysis, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish (English if neede)

Timing:
4-5 year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results in functional analysis.
- apply the results and methods of the course in various problems both in pure and applied mathematics.

Contents:
The course presents the theory of Banach and Hilbert spaces, Banach fixed point theorem, basic theory of
operators, Baire category theorem, principle of uniform boundedness, open mapping theorem, closed
graph theorem, Hahn-Banach theorem, compact operators and their spectrum.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 24h exercises

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies.

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes
K. Astala, P. Piironen, H.-O. Tylli, Funktionaalanalyysin peruskurssi, Helsingin yliopisto, luentomoniste
2008.

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5
802629S: Function estimation, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods

Learning outcomes:
Upon completing the course the student will be able to
- characterise the basic features non-parametric function estimation methods
- apply such estimation methods to practical problems
- derive some of the basic results of non-parametric function estimation for kernel estimators

Contents:
The course focuses on the theory and practice of non-parametric function estimation with a special emphasis on kernel methods. The particular functions considered are a probability density function and a regression function.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions. Probability theory I. Probability theory II or Random variables and distributions.

Recommended optional programme components:
No

Recommended or required reading:
Lecture notes written by the instructor.

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the homework problems he/she has solved during the course. This is agreed in the beginning of the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström
800674S: Fourier transform and distributions, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen oppimateriaali:
Stein, Elias M.; Shakarchi R., , 2003
Taylor, Michael E., , 1996
Grafakos Loukas, , 2004
Stakgold, Ivar , , 1998
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
English

Timing:
4.-5. year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- calculate the Fourier transform of a given integrable function on the line
- perform basic operations, such as differentiation, convolution and Fourier transformation, on distributions
- use Fourier transform to find, and provide estimates for, fundamental solutions of partial differential operators
- formulate direct and inverse scattering problems for the Schrödinger operator

Contents:

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Euclidean topology, Series and integrals, Multidimensional analysis, Complex analysis I and II, and Linear algebra I and II.

Recommended optional programme components:
-

Recommended or required reading:
- Luentomoniste
L. Grafakos: Classical and Modern Fourier Analysis, Pearson Education, 2004; 

**Assessment methods and criteria:**
Final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Valeriy Serov

**Working life cooperation:**
-

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**802647S: Fourier series and the discrete Fourier transform, 10 op**

**Voimassaolo:** 01.01.2010 -

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Valeriy Serov

**Opintokohteen kielten:** English

Ei opintojaksokuvauksia.

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**802656S: Algebraic numbers, 5 op**

**Voimassaolo:** 01.01.2012 -

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen kielten:** Finnish

**Language of instruction:**
FI/EN

**Learning outcomes:**
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed: For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

**Contents:**
First we revise some basics of rings and fields which are needed to proceed ahead field extensions. In particular, divisibility in an integral domain is carefully studied yielding to applications in the theory of polynomial algebra and algebraic integers. The theory of algebraic numbers is strongly based on polynomial algebra, where the properties of zeros and divisibility of polynomials are considered. The definition of an algebraic number will be generalized to the algebraic elements of field extensions going forward to algebraic fields. Considered as most important algebraic fields we get number fields which are finitely generated subfields of the field $\mathbb{A}$ of all complex algebraic numbers. In particular, we study quadratic number fields.
Further, we shall consider the divisibility and factorization of algebraic integers with some applications to Diophantine equations.

**Prerequisites and co-requisites:**
Algebra I and II, Linear algebra I and II, Basics in Number Theory (Number theory I)

**Recommended or required reading:**
I.N. Stewart and D.O. Tall: Algebraic number theory.
Daniel Marcus: Number fields.
J.B. Fraleigh: Abstract algebra.
Michael Artin: Algebra.

Course material: [http://cc.oulu.fi/~tma/OPETUS.html](http://cc.oulu.fi/~tma/OPETUS.html)

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**802637S: Advanced Problem Solving, 2 - 6 op**

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Peter Hästö

**Opintokohteen kielet:** English

**Assessment methods and criteria:**
Read more about [assessment criteria](http://cc.oulu.fi/~tma/OPETUS.html) at the University of Oulu webpage.

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**802645S: Number Theory A, 5 op**

**Voimassaolo:** 01.08.2009 -

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Tapani Matala-aho

**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

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**802646S: Number Theory B, 5 op**

**Voimassaolo:** 01.08.2009 -

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Tapani Matala-aho

**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

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**802631S: Modern real analysis, 10 op**

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences
Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results of modern real analysis.
- apply the results and methods of modern real analysis in different topics of mathematics, like in the theory of partial differential equations.

Contents:
The course presents Lebesgue spaces (Hölder’s and Minkowski’s inequalities, completeness, dual spaces), the Vitali covering theorem, the Hardy-Littlewood maximal function, approximation with smooth functions using convolution, Lebesgue’s density theorem, Sobolev’s inequalities.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

800688S: Theory of Optimization, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Erkki Laitinen
Opintokohteen oppimateriaali:
Luenberger, David G., , 1984
Peressini, Anthony L. , , 1988
Opintokohteen kielet: Finnish
Leikkaavuudet:
802666S Linear Optimization 5.0 op

ECTS Credits:
10 cr
Language of instruction:
Finnish
Timing:
4.-5. year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- identify the correct methods for solving the conventional optimization problems
- implement the most typical numerical algorithms for solving linear and nonlinear optimization problems

Contents:
The lecture course is focused to methods, which can apply for solving essential optimization problems of technical and economical sciences. The lectures consist of following topics: Linear programming, convex sets and functions and nonlinear convex optimization. The topics are considered theoretically and also numerical algorithms for problem solution are presented.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Euclidean topology, Series and integrals, and Linear algebra I and II
Recommended optional programme components:

- 

Recommended or required reading:

Assessment methods and criteria:
Mid-term exam or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Erkki Laitinen

Working life cooperation:
- 

800660S: Group Theory, 10 op

Opiskelumuoto: Advanced Studies

Laji: Course

Vastuuysikkö: Department of Mathematical Sciences

Arvostelu: 1 - 5, pass, fail

Opettajat: Niemenmaa Markku

Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
4-5 year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- use different proving techniques related to the theory
- prove the Sylow theorems and deal with their applications
- prove important results in the theory of finite solvable groups

Contents:
Aim: To provide the student with the basics of group theory and its development during the past hundred years. Basics of group theory, permutations, studies on the arithmetical

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 56 h, exercises 28 h.

Target group:
Major students

Prerequisites and co-requisites:
802355A Number theory and groups
802355A Rings, Fields and polynomials
800343A Permutations, fields and Galois' theory

Recommended optional programme components:
-
Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Mid-term exam or final exam.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Markku Niemenmaa

Working life cooperation:

802633S: Statistical Pattern Recognition, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen oppimateriaali:
Duda, Richard O. , , 2001
Theodoridis, Sergios , , 2002
Webb, A. R., 2002
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods.

Learning outcomes:
Upon completing the course the student will
-be familiar with the most common classifiers used in pattern recognition
-be able to apply pattern recognition methods to practical problems
-be able derive some of the basic mathematical results of pattern recognition theory

Contents:
The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

Recommended or required reading:
Lecture notes.
Optional reading:

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

801643S: Topology, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Mahmoud Filali
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
English (also Finnish)

Timing:
3.-5. year of studies. Timing varies.

Learning outcomes:
After completion of the course, the student should be able to follow more advanced courses or seminars on abstract harmonic analysis.

Contents:
This is an advanced course, aimed to final year students and to postgraduate students. The course covers topological groups and their uniform structures; subgroups, Quotient groups and product groups; and invariant pseudo-metrics on groups. The last part of the course presents some basics on compact semigroups with some examples such as Ellis group and semigroup compactifications

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics, 800329A Topologia I

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes
Assessment methods and criteria:
Mid-term exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mahmoud Filai

802651S: Measure and Integration, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802650S: Fractal Geometry, 10 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Esa Järvenpää
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802660S: Operator theory and integral equations, 10 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen kielet: English

Ei opintojaksokuvauksia.

H326603: Statistics optional advanced studies, 0 - 120 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Electives

805609S: Statistical methods in epidemiology, 9 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärää Esa
Opintokohteen oppimateriaali:
Santos Silva, Isabel dos, 1999
Clayton, David, 1993
Rothman, Kenneth J., 1998
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805646S: Analysis of longitudinal data, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Peter J. Diggle et al., 2002
Hsiao, Cheng, 2003
McCulloch, Charles E., 2001
Fitzmaurice, Garrett M., 2004
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
A student who has successfully completed the course is supposed to
- be familiar with so-called mixed models for both discrete and continuous dependent variables
- be able to make use of these mixed models while studying longitudinal data

Contents:
The purpose of the course is to teach the students, how one can simultaneously study dependencies between observed variables and variations between individuals in the panel. Linear and non-linear mixed models, variograms and so-called growth curve models are introduced as central inferential tools for these studies. Model diagnostics, dynamic ARX-type models and the GMM estimation principle also get a lot of attention. A major part of the course deals with modelling continuous dependent variables, but cases of qualitative, ordinal and count dependent variables are covered as well. The course can be taken either as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of exercises in the computer lab

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä
805679S: Time series analysis, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C., , 1993
Lütkepohl, Helmut , , 1991
Hamilton, James D., , 1994
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply computer programs to fit time series models. Furthermore, a student learns to read scientific articles about time series.

Contents:
The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH). Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

Recommended or required reading:

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä

805683S: The Statistical Foundation of Econometrics, 5 - 6 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C., , 1990
Hayashi, Fumio , , 2000
Gourieroux, Christian , , 1995
Gourieroux, Christian , , 1995
Opintokohteen kielet: Finnish

Leikkaavuudet:
805339A The statistical foundations of econometrics 5.0 op

ECTS Credits:
Learning outcomes:
The course familiarizes students with applications of statistical models when inferences are made on economic phenomena. The principles of statistical inference on economic phenomena are the same as those of general statistical inference but there are some special issues that make the inference different in economics than in other application areas of statistics. After finishing the course, a student can apply both linear regression and nonlinear regression and a student is able to apply the generalized method of moments as well as the method of instrumental variables. A student can diagnose the validity of the assumptions of the linear regression model and tune his inferences accordingly.

Contents:
The course starts with the study of the linear regression model, and covers asymptotic inference related to the linear regression model, tests of the parameter restrictions and tests of a structural change. Besides linear regression, also nonlinear regression and the generalized method of moments is covered, as well as inference based on instrumental variables and problems stemming from measurement errors. Inference under heteroscedasticity and autocorrelated disturbances is included. The basic theory of time series analysis (cointegration and autoregressive conditional heteroscedasticity) and the basic theory of panel data is included.

Recommended or required reading:
William H. Greene: Econometric Analysis (Prentice Hall)

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä.
806621S: Spatial Data Analysis, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806628S: Statistical Finance, 5 op

Voimassaolo: 01.08.2009 - 
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806629S: Introduction to Sampling Methods, 4 op

Voimassaolo: 01.01.2010 - 
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lääärä Esa
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806630S: Market Risk Analysis, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen kielet: Finnish
Leikkaavuudet: 
806330A Analysis of Market Risk 5.0 op

ECTS Credits: 
5 cr
Language of instruction: 
Finnish
Timing: 
3. year of studies or later. Timing varies.
Learning outcomes:
The student knows how to estimate the unconditional value-at-risk using empirical quantiles, parametric modeling, semiparametric modeling, and extreme value theory. The student knows also how to estimate the conditional value-at-risk using GARCH models. The student can read scientific articles about risk management.

Contents:
The course is an introduction to the quantitative risk management of a portfolio of stocks. The course introduces various risk measures, extreme value theory, and modeling of financial time series. The course covers:
- conditional and unconditional loss distribution,
- Value-at-Risk and other risk measures, standard methods of estimating
- Value-at-Risk: multivariate normal modeling, historical simulation/empirical quantiles, and the Monte Carlo method,
- modeling of distributions: multivariate distributions, normal mixed distributions, spherical and elliptical distributions, and dimension reduction,
- modeling of financial time series: ARMA models, GARCH models, and volatility models, copulas and measures of dependence,
- extreme value theory: block maxima and threshold exceedance methods.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises.

Target group:
students of mathematical sciences, students of finance and economics

Prerequisites and co-requisites:
806113P Introduction to Statistics

Recommended optional programme components:
-

Recommended or required reading:

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
Home page of the course is http://cc.oulu.fi/~jklmela/marketrisk/

805651S: Stochastic processes, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksoikuvauksia.
806622S: Probability, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksojakoauksia.

805611S: Mathematical statistics II, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Lehmann, E. L. , , 2001
Migon, H. S. , , 1999
Opintokohteen kielet: Finnish
Leikkaavuudet:
805627S Theory of Statistical Inference 5.0 op

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805611S: Mathematical statistics II, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Lehmann, E. L. , , 2001
Migon, H. S. , , 1999
Opintokohteen kielet: Finnish
Leikkaavuudet:
805627S Theory of Statistical Inference 5.0 op

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805644S: Maturity test, 0 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksojakoauksia.
806624S: Practical training/consulting, 5 - 7 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jari Päkkilä
Opintokohteen kielet: Finnish
Voidaan suorittaa useasti: Kyllä

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805620S: Pro Gradu seminar, 8 op

Voimassaolo: 01.09.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr
Language of instruction:
Finnish
Timing:
4.-5. year of studies.
Learning outcomes:
After successful completion of the Pro gradu -seminar the student is able to conduct a small scale statistical investigation and report it both in written form and orally.

Contents:
Under supervision of the leader of the seminar each student conducts a small-scale statistical investigation on a given empirical topic and material, makes a written report from it and presents it orally in seminar sessions. The written report is the M.Sc. thesis, when statistics is the major subject of the student.

Mode of delivery:
Face-to-face teaching, seminars
Learning activities and teaching methods:
Seminars and meetings in two years
Target group:
Major students in statistics
Prerequisites and co-requisites:
Compulsory basic and intermediate studies in statistics
Recommended optional programme components:
-
Recommended or required reading:
-
Assessment methods and criteria:
Participation into seminar sessions, seminar presentation and written paper.
Read more about assessment criteria at the University of Oulu webpage.
Grading:
Fail/Pass
Person responsible:
Esa Läärá
Working life cooperation:
805642S: Pro gradu thesis, 30 op

Opiskelumuoto: Advanced Studies
Laji: Diploma thesis
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

806631S: Random variables and distributions, 10 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärää Esa
Opintokohteen kielet: Finnish
Leikkaavuudet:

805628S Probability Distributions 5.0 op

Ei opintojaksokuvausia.

H325003: Mathematics, optional advanced studies, 0 - 120 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvausia.

Electives

802653S: Lebesgue Measure and Integration Theory, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikael Lindström
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.
**801698S: Cryptography, 5 op**

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Tapani Matala-aho  
**Opintokohteen oppimateriaali:**  
Trappe, Wade; Washington, Lawrence C., , 2005  
Menezes, Alfred J.; van Oorschot, Paul C.; Vanstone, Scott A., , 1997  
**Opintokohteen kielet:** Finnish

**Learning outcomes:**
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

**Contents:**
In our lectures we study mathematical basics of encrypting, key exchange and signature systems. As examples, we mention elementary group and number theory used in primality tests and factoring, complexity estimates of computations-in particular in finite fields, repeated squaring and discrete logarithm in finite cyclic groups- applied in multiplicative groups of finite fields and addition groups of elliptic curves. Deduction of addition formulae in projective and affine Weierstrass elliptic curves. Diffie-Hellman key exchange, ElGamal encrypting and signature systems in finite cyclic groups applied in finite fields or in elliptic curves defined over finite fields. DSA, ECDSA, Massey-Omura. Some algorithms and tests: AKS, Fermat, Lenstra , Lucas, Miller-Rabin, Pohlig-Hellman, Pollard's p-1 and rho, pseudoprimes, quadratic sieve, Solovay-Rasssen.

**Assessment methods and criteria:**
Read more about [assessment criteria](#) at the University of Oulu webpage.

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**802655S: Continued Fractions, 5 op**

**Voimassaolo:** 01.01.2011 -  
**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish

**Language of instruction:**
FI/EN

**Recommended or required reading:**
Kenneth H. Rosen: Elementary number theory and its applications.  
Lisa Lorentzen and Haakon Waadeland: Continued Fractions with Applications (1992).  
Oskar Perron: Die Lehre von den Kettenbruchen (1913).

Course material: [http://cc.oulu.fi/~tma/OPETUS.html](http://cc.oulu.fi/~tma/OPETUS.html)

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**802644S: Introduction to Functional Analysis, 10 op**

**Voimassaolo:** 01.08.2009 -  
**Opiskelumuoto:** Advanced Studies
Learning outcomes:
If we think of functional analysis as infinite dimensional linear algebra, then the course offers the tools and the ways to handle this infinite dimension. After completing the course successfully, the student will be able to follow almost any material on functional analysis.

Contents:
After recalling some basic definitions on linear algebra and giving the basic definitions concerning normed spaces, we present the uniform boundedness principle and the open mapping theorem. In this first part of the course, the relative compactness of the unit ball in a normed space is studied under the norm topology. Hahn-Banach Theorem is presented in its various forms: algebraic, analytic and geometric, and followed by Krein-Milman Theorem. We end up with the weak topology on normed spaces and the weak* topology on Banach duals. The relative compactness of the unit ball is studied with respect to these two topologies.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Mahmoud Filali
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen oppimateriaali:
Colton, David, , 1988
Kress, Rainer, , 1999
Folland, Gerald B. , , 1995
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Learning outcomes:
On successful completion of this course, the student will be able to
- solve linear and quasi-linear partial differential equations of first order using the method of characteristics
- apply the method of separation of variables to solve initial-boundary value problems for heat, wave and Laplace equations
- verify that a given function is a fundamental solution of a partial differential operator
- use single and double layer potentials to solve boundary value problems for Laplacian

Contents:
Linear and nonlinear equations of the first order, trigonometric Fourier series, Laplace equation in $\mathbb{R}^n$ and in bounded domains, potential theory, Green's function, Heat equation in $\mathbb{R}^n$ and in bounded domains, Wave equation in $\mathbb{R}^n$ and in bounded domains, d'Alembert formula for any dimensions, Fourier method.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Valeriy Serov

802652S: Hilbert Spaces, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
800624S Analysis III 10.0 op

ECTS Credits:
5 ECTS credits

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

800651S: Functional analysis, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
ECTS Credits:
10 cr

Language of instruction:
Finnish (English if needed)

Timing:
4-5 year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results in functional analysis.
- apply the results and methods of the course in various problems both in pure and applied mathematics.

Contents:
The course presents the theory of Banach and Hilbert spaces, Banach fixed point theorem, basic theory of
operators, Baire category theorem, principle of uniform boundedness, open mapping theorem, closed
graph theorem, Hahn-Banach theorem, compact operators and their spectrum.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 24h exercises

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies.

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes
K. Astala, P. Piiroinen, H.-O. Tylli, Funktionaalianalyysin peruskurssi, Helsingin yliopisto, luentomoniste
2008.

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mikael Lindström

Working life cooperation:
-

802629S: Function estimation, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettaja: Lasse Holmström
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr
Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods

Learning outcomes:
Upon completing the course the student will be able to
- characterise the basic features non-parametric function estimation methods
- apply such estimation methods to practical problems
- derive some of the basic results of non-parametric function estimation for kernel estimators

Contents:
The course focuses on the theory and practice of non-parametric function estimation with a special emphasis on kernel methods. The particular functions considered are a probability density function and a regression function.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions. Probability theory I. Probability theory II or Random variables and distributions.

Recommended optional programme components:
No

Recommended or required reading:
Lecture notes written by the instructor.

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the homework problems he/she has solved during the course. This is agreed in the beginning of the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

800674S: Fourier transform and distributions, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen oppimateriaali:
Stein, Elias M.; Shakarchi R., , 2003
Taylor, Michael E., , 1996
Grafakos Loukas, , 2004
Stakgold, Ivar , , 1998
ECTS Credits: 
10 cr
Language of instruction: 
English
Timing: 
4.-5. year of studies. Timing varies.
Learning outcomes: 
On successful completion of this course, the student will be able to 
- calculate the Fourier transform of a given integrable function on the line 
- perform basic operations, such as differentiation, convolution and Fourier transformation, on distributions 
- use Fourier transform to find, and provide estimates for, fundamental solutions of partial differential operators 
- formulate direct and inverse scattering problems for the Schrödinger operator
Contents: 
Mode of delivery: 
Face-to-face teaching
Learning activities and teaching methods: 
56h lectures, 28h exercises
Target group: 
Major students
Prerequisites and co-requisites: 
Euclidean topology, Series and integrals, Multidimensional analysis, Complex analysis I and II, and Linear algebra I and II.
Recommended optional programme components: 
-
Recommended or required reading: 
Luentomoniste
L. Grafakos: Classical and Modern Fourier Analysis, Pearson Education, 2004;
Assessment methods and criteria: 
Final exam
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible: 
Valeriy Serov
Working life cooperation: 
-

802647S: Fourier series and the discrete Fourier transform, 10 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
802656S: Algebraic numbers, 5 op

**Voimassaolo:** 01.01.2012 -  
**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish

**Language of instruction:**  
FI/EN

**Learning outcomes:**
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

**Contents:**
First we revise some basics of rings and fields which are needed to proceed ahead field extensions. In particular, divisibility in an integral domain is carefully studied yielding to applications in the theory of polynomial algebra and algebraic integers. The theory of algebraic numbers is strongly based on polynomial algebra, where the properties of zeros and divisibility of polynomials are considered. The definition of an algebraic number will be generalized to the algebraic elements of field extensions going forward to algebraic fields. Considered as most important algebraic fields we get number fields which are finitely generated subfields of the field \( \mathbb{A} \) of all complex algebraic numbers. In particular, we study quadratic number fields. Further, we shall consider the divisibility and factorization of algebraic integers with some applications to Diophantine equations.

**Prerequisites and co-requisites:**
Algebra I and II, Linear algebra I and II, Basics in Number Theory (Number theory I)

**Recommended or required reading:**
I.N. Stewart and D.O. Tall: Algebraic number theory.  
Daniel Marcus: Number fields.  
J.B. Fraleigh: Abstract algebra.  
Michael Artin: Algebra.

Course material: http://cc.oulu.fi/~tma/OPETUS.html

802637S: Advanced Problem Solving, 2 - 6 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail
Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results of modern real analysis.
- apply the results and methods of modern real analysis in different topics of mathematics, like in the theory of partial differential equations.

Contents:
The course presents Lebesgue spaces (Hölder’s and Minkowski’s inequalities, completeness, dual spaces), the Vitali covering theorem, the Hardy-Littlewood maximal function, approximation with smooth functions using convolution, Lebesgue’s density theorem, Sobolev’s inequalities.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Erkki Laitinen  
**Opintokohteen oppimateriaali:**  
Luenberger, David G., 1984  
Peressini, Anthony L., 1988  
**Opintokohteen kielet:** Finnish  
**Leikkaavuudet:**  
802666S   Linear Optimization   5.0 op  

**ECTS Credits:**  
10 cr  
**Language of instruction:**  
Finnish  
**Timing:**  
4.-5. year of studies. Timing varies.  
**Learning outcomes:**  
On successful completion of this course, the student will be able to  
- identify the correct methods for solving the conventional optimization problems  
- implement the most typical numerical algorithms for solving linear and nonlinear optimization problems  

**Contents:**  
The lecture course is focused to methods, which can apply for solving essential optimization problems of technical and economical sciences. The lectures consist of following topics: Linear programming, convex sets and functions and nonlinear convex optimization. The topics are considered theoretically and also numerical algorithms for problem solution are presented.  

**Mode of delivery:**  
Face-to-face teaching  
**Learning activities and teaching methods:**  
56h lectures, 28h exercises  
**Target group:**  
Major students  
**Prerequisites and co-requisites:**  
Euclidean topology, Series and integrals, and Linear algebra I and II  
**Recommended optional programme components:**  
-  
**Recommended or required reading:**  
**Assessment methods and criteria:**  
Mid-term exam or final exam  
Read more about [assessment criteria](#) at the University of Oulu webpage.  
**Grading:**  
1-5  
**Person responsible:**  
Erkki Laitinen  
**Working life cooperation:**  
-  

800660S: Group Theory, 10 op
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Niemenmaa Markku
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
4-5 year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- use different proving techniques related to the theory
- prove the Sylow theorems and deal with their applications
- prove important results in the theory of finite solvable groups

Contents:
Aim: To provide the student with the basics of group theory and its development during the past hundred years. Basics of group theory, permutations, studies on the arithmetical

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 56 h, exercises 28 h.

Target group:
Major students

Prerequisites and co-requisites:
802355A Number theory and groups
802355A Rings, Fields and polynomials
800343A Permutations, fields and Galois' theory

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Mid-term exam or final exam.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Markku Niemenmaa

Working life cooperation:
-

802633S: Statistical Pattern Recognition, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen oppimateriaali:
Duda, Richard O. , , 2001
Theodoridis, Sergios , , 2002
Webb, A. R , , 2002
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods.

Learning outcomes:
Upon completing the course the student will
- be familiar with the most common classifiers used in pattern recognition
- be able to apply pattern recognition methods to practical problems
- be able derive some of the basic mathematical results of pattern recognition theory

Contents:
The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

Recommended or required reading:
Lecture notes. 
Optional reading:

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

801643S: Topology, 10 op
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Mahmoud Filali
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
English (also Finnish)

Timing:
3.-5. year of studies. Timing varies.

Learning outcomes:
After completion of the course, the student should be able to follow more advanced courses or seminars on abstract harmonic analysis.

Contents:
This is an advanced course, aimed to final year students and to postgraduate students. The course covers topological groups and their uniform structures; subgroups, Quotient groups and product groups; and invariant pseudo-metrics on groups. The last part of the course presents some basics on compact semigroups with some examples such as Ellis group and semigroup compactifications

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics, 800329A Topologia I

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Mid-term exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mahmoud Filai

802651S: Measure and Integration, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802650S: Fractal Geometry, 10 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Esa Järvenpää
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802660S: Operator theory and integral equations, 10 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen kielet: English

Ei opintojaksokuvauksia.

H326603: Statistics optional advanced studies, 0 - 120 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Electives

805609S: Statistical methods in epidemiology, 9 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen oppimateriaali:
Santos Silva, Isabel dos , , 1999
Clayton, David , , 1993
Rothman, Kenneth J. , , 1998
Opintokohteen kielet: Finnish
805646S: Analysis of longitudinal data, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Peter J. Diggle et al., , 2002
Hsiao, Cheng , , 2003
McCulloch, Charles E. , , 2001
Fitzmaurice, Garrett M. , , 2004
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
A student who has successfully completed the course is supposed to
- be familiar with so-called mixed models for both discrete and continuous dependent variables
- be able to make use of these mixed models while studying longitudinal data

Contents:
The purpose of the course is to teach the students, how one can simultaneously study dependencies
between observed variables and variations between individuals in the panel. Linear and non-linear mixed
models, variograms and so-called growth curve models are introduced as central inferential tools for these
studies. Model diagnostics, dynamic ARX-type models and the GMM estimation principle also get a lot of
attention. A major part of the course deals with modelling continuous dependent variables, but cases of
qualitative, ordinal and count dependent variables are covered as well. The course can be taken either
as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of
exercises in the computer lab

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä

805679S: Time series analysis, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C. , , 1993
Lütkepohl, Helmut , , 1991
Hamilton, James D. , , 1994
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply computer programs to fit time series models. Furthermore, a student learns to read scientific articles about time series.

Contents:
The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH). Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

Recommended or required reading:

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä

805683S: The Statistical Foundation of Econometrics, 5 - 6 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C. , , 1990
Hayashi, Fumio , , 2000
Gourieroux, Christian , , 1995
Gourieroux, Christian , , 1995
Opintokohteen kielet: Finnish
Leikkaavuudet:
805339A The statistical foundations of econometrics 5.0 op

ECTS Credits:
5/6 cr

Language of instruction:
Finnish

Learning outcomes:
The course familiarizes students with applications of statistical models when inferences are made on economic phenomena. The principles of statistical inference on economic phenomena are the same as those of general statistical inference but there are some special issues that make the inference different in economics than in other application areas of statistics. After finishing the course, a student can apply both linear regression and nonlinear regression and a student is able to apply the generalized method of moments as well as the method of instrumental variables. A student can diagnose the validity of the assumptions of the linear regression model and tune his inferences accordingly.

Contents:
The course starts with the study of the linear regression model, and covers asymptotic inference related to the linear regression model, tests of the parameter restrictions and tests of a structural change. Besides linear regression, also nonlinear regression and the generalized method of moments is covered, as well as inference based on instrumental variables and problems stemming from measurement errors.
Inference under heteroscedasticity and autocorrelated disturbances is included. The basic theory of time series analysis (cointegration and autoregressive conditional heteroscedasticity) and the basic theory of panel data is included.

**Recommended or required reading:**
William H. Greene: Econometric Analysis (Prentice Hall)

**Assessment methods and criteria:**
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Person responsible:**
Jussi Klemelä.

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**805681S: Generalized Linear Models, 9 op**

- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

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**805699S: Statistical methods in epidemiology, 8 op**

- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

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**806618S: Computationally intensive statistical methods, 9 op**

- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

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**806621S: Spatial Data Analysis, 10 op**

- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

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**806628S: Statistical Finance, 5 op**

- **Voimassaolo:** 01.08.2009 -
- **Opiskelumuoto:** Advanced Studies
Introduction to Sampling Methods, 4 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies

Market Risk Analysis, 5 op

Opiskelumuoto: Advanced Studies

Learning outcomes:
The student knows how to estimate the unconditional value-at-risk using empirical quantiles, parametric modeling, semiparametric modeling, and extreme value theory. The student knows also how to estimate the conditional value-at-risk using GARCH models. The student can read scientific articles about risk management.

Contents:
The course is an introduction to the quantitative risk management of a portfolio of stocks. The course introduces various risk measures, extreme value theory, and modeling of financial time series. The course covers:

- conditional and unconditional loss distribution,
- Value-at-Risk and other risk measures, standard methods of estimating,
- Value-at-Risk: multivariate normal modeling, historical simulation/empirical quantiles, and the Monte Carlo method,
- modeling of distributions: multivariate distributions, normal mixture distributions, spherical and elliptical distributions, and dimension reduction,
- modeling of financial time series: ARMA models, GARCH models, and volatility models, copulas and measures of dependence,
• extreme value theory: block maxima and threshold exceedance methods.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
Besides lectures, there are voluntary exercises.

**Target group:**
students of mathematical sciences, students of finance and economics

**Prerequisites and co-requisites:**
806113P Introduction to Statistics

**Recommended optional programme components:**

**Recommended or required reading:**

**Assessment methods and criteria:**
Final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Jussi Klemelä

**Working life cooperation:**
-

**Other information:**
Home page of the course is [http://cc.oulu.fi/~jklemela/marketrisk/](http://cc.oulu.fi/~jklemela/marketrisk/)

**805651S: Stochastic processes, 10 op**

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

**806622S: Probability, 10 op**

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

**805611S: Mathematical statistics II, 10 op**

**Opiskelumuoto:** Advanced Studies

**Laji:** Course
800008Y-01: Acting as a Student Tutor, 1 op

Opiskelumuoto: General Studies
Laji: Partial credit

902002Y: English 1 (Reading for Academic Purposes), 2 op

Voimassaolo: 01.08.1995 -

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Learning outcomes:
By the end of the course, you are expected

- to have acquired effective vocabulary learning techniques by being able to distinguish parts of words to infer meanings
- to understand and be able to construct basic grammatical structures used in formal written English
- to be able to utilize text structure and cohesion markers when reading academic texts
to be able to apply effective reading techniques and have necessary skills to extract global and detailed information with considerable ease and speed from general texts related to Natural Sciences as well as texts/textbooks of their own field.

Contents:
In this course, students improve their understanding of written academic English used in texts in Natural Sciences as well as expand their general and scientific vocabulary. Students become aware of their own role in learning and use a variety of different study methods in order to develop their own language learning strategies, which will enhance their academic English.

Mode of delivery:
Contact teaching

Learning activities and teaching methods:
Contact teaching (26 hours) and self-study 28 hours

Target group:
1st year students of Biology, Chemistry, Geology, Information Processing Science, Physics, and Mathematics

Prerequisites and co-requisites:
- 

Recommended optional programme components:
In addition to this course, students are required to take 902004Y Scientific Communication.

Recommended or required reading:
Set books for substance studies; journal articles in print and on-line.

Assessment methods and criteria:
Continuous assessment takes into account active and regular participation in classroom sessions and successful completion of all homework tasks, vocabulary quizzes, and an end of course exam.

Assessment criteria:
Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Biology, Geology, Information Processing: Karen Niskanen
Chemistry, Physics, Mathematics: Patrick Nesbitt

Working life cooperation:
-

Other information:
N.B. Students with grades laudatur or eximia in their A1 English school-leaving examination can be exempted from this course and will be granted the credits by the Faculty of Science.

Retake examinations: Two retake examinations are allowed on the dates set by the Extension School. See the dates and registration instructions at: http://www.oulu.fi/kielikoulutus

902004Y: English 2 (Scientific Communication), 2 op

Voimassaolo: 01.08.1995 -
Opiskelumuoto: Language and Communication Studies
Laji: Course
Vastauyksikkö: Language Centre
Arvostelu: 1 - 5, pass, fail
Opintokohteenv kielet: English

Leikkaavuudet:
ay902004Y English 2 (Scientific Communication) (OPEN UNI) 2.0 op

Proficiency level:
B2/C1 on the CEFR scales

Status:
This course is mandatory for all 2nd year students (except geographers) who will have English as their foreign language in their B.Sc. degree. This includes the students who were exempted from ‘Reading for Academic Purposes’(902002Y). Please consult the faculty study guide to establish the language requirements on your own degree programme.

Required proficiency level:
Students taking this course must have had English as the A1 or A2 language at school or the equivalent English skills should have been acquired otherwise. The course ‘Reading for Academic Purposes’ (902002Y) is a pre-requisite, unless exempted.

ECTS Credits:
The student workload is 53 hrs work/ 2 ECTS credits.
Language of instruction: English
Timing:
Biology: 2nd year autumn term
Chemistry: 2nd year spring term
Geology: 2nd year spring term
Information Processing Science: 2nd year autumn term
Mathematics: 2nd year spring term
Physics: 2nd year autumn term
Learning outcomes:
By the end of the course, you are expected:
1. to have provided evidence of oral fluency in pair work communication and small group discussions.
2. to have developed effective language learning strategies through autonomous homework.
3. to have demonstrated the ability to prepare and present scientific subjects, using appropriate field-related vocabulary.
4. to have demonstrated lecture listening skills in field-related situations.
Contents:
Skills in listening, speaking, and giving presentations are practised in the course. Homework tasks include autonomous work to support the classroom learning and the task of preparing and presenting a scientific presentation.
Mode of delivery:
Contact teaching
Learning activities and teaching methods:
Contact teaching 28 hours, homework 28 hours
Target group:
2nd year students of Biology, Chemistry, Geology, Information Processing Science, Mathematics, Physics
Prerequisites and co-requisites:
Recommended optional programme components:
Also required: 902002Y Reading for Academic Purposes Englannin kieli 1
Recommended or required reading:
Course materials will be provided by the teacher and a copy fee will be charged.
Assessment methods and criteria:
Continuous assessment is based on regular attendance, active participation in all lessons and the successful completion of all homework tasks.
Read more about assessment criteria at the University of Oulu webpage.
Grading:
Pass / fail.
Person responsible:
Jolene Gear
Working life cooperation:
Alternative method of course completion: An optional exemption test is offered twice per year. The student can only participate in the exemption exam once. See exemption exam details and schedule.
After the course, student is familiar with objectives and curriculum of the degree program. Moreover, the student is familiarized with the correct study methods and learning environment. After the course, the student is also able to search information from, for instance, university library and databases. After the course, student has planned future studies (study plan).

**Contents:**
The aim of the course is to familiarise the student with university studies, learning environment, provide the student with information on the history and current weight of mathematical sciences in the society as well as the objectives and curriculum of the degree programme. During the course, student makes the study plan.

**Mode of delivery:**
Face-to-face teaching (tutoring group)

**Learning activities and teaching methods:**
Group working

**Target group:**
Major students

**Prerequisites and co-requisites:**
-

**Recommended optional programme components:**
-

**Recommended or required reading:**
-

**Assessment methods and criteria:**
Taking part to the group meetings and making the Personal Study Plan.

Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
Pass/Fail

**Person responsible:**
Student advisor

**Working life cooperation:**
-

*Compulsory*

**800008Y-02: Personal Study Plan, 1 op**

Opiskelumuoto: General Studies  
Laji: Partial credit  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

**800008Y-01: Acting as a Student Tutor, 1 op**

Opiskelumuoto: General Studies  
Laji: Partial credit  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

**800008Y-02: Personal Study Plan, 1 op**

Opiskelumuoto: General Studies  
Laji: Partial credit  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish
901004Y: Swedish, 2 - 3 op

Voimassaolo: 01.08.1995 -
Opiskelumuoto: Language and Communication Studies
Laji: Course
Vastuuysikkö: Language Centre
Opintokohteen kielet: Swedish
Leikkaavuudet:
- 901035Y Second Official Language (Swedish), Oral Skills 1.0 op
- 901034Y Second Official Language (Swedish), Written Skills 1.0 op
- ay901004Y Swedish (OPEN UNI) 2.0 op

Proficiency level:
B1/B2/C1 (CEFR scale)

Status:
This course is compulsory to all students except those who have at least 60 ECTS credits of Swedish studies in their degrees. The language proficiency provided by the course unit is equivalent to the language proficiency required of a state official with an academic degree working in a bilingual municipality area (Act 424/03 and Decree 481/03).

Required proficiency level:
The required starting proficiency level for students of all faculties is a grade of 7 or higher from the Swedish studies at secondary school (B-syllabus) or matriculation examination grade A - L or a passing grade from the Brush up course in Swedish 901018Y.

If a student doesn't meet these requirements or his/her language skills are otherwise lacking, he/she must achieve the required proficiency level BEFORE taking this compulsory Swedish course

ECTS Credits:
2 ECTS credits (Biochemistry 3 ECTS credits)

Language of instruction:
Swedish

Timing:
See the study guide of the Faculty of Science.

Learning outcomes:
Upon completion of the course the student should have acquired the necessary proficiency level in Swedish to be able to manage in the most common communication situations related to his/her professional work tasks. He/she should be able to use basic grammatical structures fairly well in both speech and writing. He/she should be able to use the most common situational phrases understandably in various communication situations. He/she should be able to find the main points in general academic texts and texts related to his/her field of study and relay this information to colleagues or an audience of laymen using Swedish. He/she should be able to write short texts relating to his/her field of study.

Contents:
Communicative oral and written exercises, which aim to develop the student's Swedish proficiency in areas relevant to his/her academic field and future professional tasks. The student practises oral presentation and pronunciation. Situational oral exercises done individually and in pairs and groups. Discussions in small groups. Current texts about the student's special field. Listening comprehension exercises. Written exercises relating to the student's professional field.

Mode of delivery:
Contact teaching

Learning activities and teaching methods:
2 ECTS credits: 28 hours of contact teaching (1 x 180 minutes per week) and related exercises, self-directed study.
The course unit's total workload is 53 hours.
3 ECTS credits (biochemistry): 45 hours of contact teaching (2 x 90 minutes per week) and related exercises, 35 hours of self-directed study. The course unit's total workload is 80 hours.

Target group:
Students of the Faculty of Science

Prerequisites and co-requisites:
See Required Porficiency Level

Recommended optional programme components:
-

Recommended or required reading:
The material, which is special field-specific, authentic and up to date, is distributed during the course. Students must pay for their course material.

**Assessment methods and criteria:**
The course focuses on improving both oral and written language skills and requires active attendance and participation in exercises, which also require preparation time. 100% attendance is required. The course unit tests both oral and written language skills. Students participate in the teaching in either autumn semester or spring semester.

Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
Assessment is based on continuous assessment and exams. Approved completion of the course unit requires that the student achieves at least satisfactory oral and written language skills. The grades are based on continuous assessment and the course exams. Oral and written language skills are graded separately. The possible grades are satisfactory skills (CERF proficiency level B1) and good skills (CERF proficiency levels B2-C1). For more information on the proficiency levels of oral and written language skills, see Assessment Criteria (in Finnish).

**Person responsible:**
Lecturer Rauno Varonen

**Working life cooperation:**
-

**Other information:**
Teaching will begin according to the schedule

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802354A: Basics in Algebra, 5 op

**Voimassaolo:** 01.08.2010 -
**Opiskelumuoto:** Intermediate Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Kari Myllylä

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
- ay802354A Number Theory and Groups (OPEN UNI) 5.0 op
- 800333A Algebra I 8.0 op

**ECTS Credits:**
5 ECTS credits

**Language of instruction:**
Finnish

**Timing:**
1. year, 3. period

**Learning outcomes:**
After completing the course, student is able to
- derive and proof main results in the course
- use and apply different proof techniques
- recognize algebraic structures and the concepts
- see connections and differences between different algebraic structures

**Contents:**
The course includes basics in arithmetics and algebraic structures, such as, congruence, residue classes, prime numbers, Euclidean algorithm, the fundamental theorem of arithmetic, Euler-Fermat formula, groups and morphisms. The course gives an understanding of algebraic terms and concepts used in mathematics and physics.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
28h lectures, 14h exercises

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
802151P Introduction to mathematical deduction

**Recommended optional programme components:**
Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Midterm exam or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Kari Myllylä

Working life cooperation:

802155P: Continuity and limit, 4 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Leikkaavuudet:
800119P Analysis 1  5.0 op
802162P Continuity and Limit  5.0 op
801111P Basic Methods in Mathematics I / math  10.0 op
800147P Basic Methods in Mathematics I / appl.  8.0 op

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
1. year, 1. period

Learning outcomes:
After completing the course, student is able to
- derive and proof main results of the course
- use different types of proof techniques
- define the limit of function and the continuity of function
- derive and proof the limit using different proof techniques
- deduce the continuity of functions using different proof techniques

Contents:
The main concept of the course are the limit of a real-valued function and the continuity of real-valued function. Interrelations between these concepts are also studied.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises

Target group:
Main and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5
Person responsible:
Maarit Järvenpää
Working life cooperation:
-

802156P: Derivative, 4 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Maarit Järvenpää
Opintokohteen kielet: Finnish

Leikkaavuudet:
800317A Analysis 2 5.0 op
802163P Derivative 5.0 op
801111P Basic Methods in Mathematics I / math 10.0 op

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
1. year, 2. period

Learning outcomes:
After completing the course, student is able to
- derive and proof main results of the course
- use different types of proof techniques
- use and apply the concept of derivative in different types of problems

Contents:
The course considers the concept of derivative of real-valued function and applies this concept to different types of situations.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction
802154P Elementary functions
802155P Limits and continuity

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Maarit Järvenpää
Working life cooperation:
-

802154P: Elementary functions, 3 op
**Voimassaolo:** 01.08.2012 -  
**Opiskelumuoto:** Basic Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Maarit Järvenpää  
**Opintokohteen kielet:** Finnish  

**Leikkaavuudet:**  
802161P Introduction to Real Functions 5.0 op  
801111P Basic Methods in Mathematics I / math 10.0 op  
800147P Basic Methods in Mathematics I / appl. 8.0 op  

**ECTS Credits:**  
3 cr  

**Language of instruction:**  
Finnish  

**Timing:**  
1. year, 1. period  

**Learning outcomes:**  
After completing the course, student is able to  
- prove essential result in the course  
- use and apply different types of proof techniques  
- handle elementary functions  

**Contents:**  
Course introduces basic concepts and definitions related to real-valued functions. Definitions and proofs are essential part of the course.  

**Mode of delivery:**  
Face-to-face teaching  

**Learning activities and teaching methods:**  
21h luentoja, 10 h harjoituksia  

**Target group:**  
Major and minor students  

**Prerequisites and co-requisites:**  
802151P Introduction to mathematical deduction  

**Recommended optional programme components:**  
-  

**Recommended or required reading:**  
-  

**Assessment methods and criteria:**  
Final exam  
Read more about assessment criteria at the University of Oulu webpage.  

**Grading:**  
1-5  

**Person responsible:**  
Maarit Järvenpää  

**Working life cooperation:**  
-  

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**802352A: Euclidean Topology, 4 op**  

**Voimassaolo:** 01.08.2010 -  
**Opiskelumuoto:** Intermediate Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Maarit Järvenpää  
**Opintokohteen kielet:** Finnish  

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Learning outcomes:
After the course student is able to
- define elementary topological concepts (open and closed sets, accumulation point, etc)
- handle sequences of real numbers
- proof fundamental theorems related to continuous functions

Contents:
The courses goal is to expand students knowledge and understanding of continuous functions. Course considers basic topology of n-dimensional Euclidean space. Important concepts are, for instance, open and closed sets, compactness and completeness.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802154P Elementary functions
802155P Limit and continuity
802156P Derivative

Recommended optional programme components:

Recommended or required reading:

Assessment methods and criteria:
Midterm exam or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Maarit Järvenpää

Working life cooperation:

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806113P: Introduction to Statistics, 5 op

Voimassaolo: 01.01.2011 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Hanna Heikkinen, Läärä Esa
Opintokohteen oppimateriaali:
Wild, Christopher J. , , 2000
Grönroos, Matti (2) , , 2003
Opintokohteen kielet: Finnish

Leikkaavuudet:
806118P Introduction to Statistics 5.0 op
806119P A Second Course in Statistics 5.0 op
806116P Statistics for Economic Sciences 5.0 op
ECTS Credits:
5 cr

Language of instruction:
Finnish

Timing:
First year, 3. period

Learning outcomes:
On successful completion of this course, the student will be able to
- present the dataset by using graphics, tables and statistics
- apply appropriate statistical techniques for analyzing solutions to simple real-world problems
- interpret listing of some statistical software

Contents:
The course presents probabilistic techniques for studying uncertainty, and to illustrate how such techniques can be applied to make statistical analysis and interpretation of data in simple one variable settings. Topics include descriptive statistics, basics of probability theory, random variables and their distributions, sampling distributions, estimation, confidence intervals, and hypothesis testing. One aim is also to get basic knowledge from some statistical software.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
32 h lectures, 24 h exercises from which 16 h are normal exercises and 8 h computer exercises.

Target group:
Major and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction
801195P Introduction to probability theory
802118P Linear algebra I

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Hanna Heikkinen

Working life cooperation:
No

802151P: Introduction to mathematical deduction, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Leikkaavuudet:
ay802151P Introduction to mathematical deduction (OPEN UNI) 5.0 op

ECTS Credits:
5 ECTS

Language of instruction:
Finnish

Timing:
First period at the first semester.

Learning outcomes:
After completing the course, student
- is able to use different methods proving techniques
- is able to use basic set theoretic concepts and definitions
- is able to define and apply basic definitions related to functions
Contents:
The course in an introduction to mathematical deduction and introduces different types of proof techniques. The course covers the concepts familiar from upper secondary school studies more profoundly. Main concepts in this course are basic set theory and functions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 30h, exercises 18h

Target group:
Major and minor students

Prerequisites and co-requisites:

- 

Recommended optional programme components:

- 

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Tero Vedenjuoksu

Working life cooperation:

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802118P: Linear Algebra I, 4 op

Voimassaolo: 16.10.2012 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Lay, David C., , 2003
Opintokohteen kielet: Finnish
Leikkaavuudet:
802120P Introduction to Matrices 5.0 op

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
First semester, 2. period

Learning outcomes:
On successful completion of this course, the student will be able to
- solve linear systems of equations and apply them to linear algebraic problems
- know matrices and their basic properties
- know basic properties of linear spaces

Contents:
The aim is to familiarise the student with the basics of linear algebra: systems of linear equations, vector space $\mathbb{R}^n$ and matrix algebra.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
35 h lectures, 21 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Midterm exams or final exam

Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Tero Vedenjuoksu

Working life cooperation:
-

802119P: Linear Algebra II, 5 op

Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Lay, David C. , , 2003
Opintokohteen kielet: Finnish

Leikkaavuudet:
802320A Linear Algebra 5.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
First year, 4. period

Learning outcomes:
On successful completion of this course, the student will be able to
- basic properties of inner product spaces
- linear mappings, their matrix representation, and eigen values
- determinants and apply them to problems relating to matrices and linear mappings

Contents:
The aim of the course is to provide the student with the knowledge needed in almost all later courses in mathematics:
Abstract vector spaces and subspaces, Linear independence and bases, Inner product spaces, Linear mappings,
Determinants, Eigenvalues and Eigenvectors, Hermitian matrices and quadratic forms.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
35 h lectures, 21 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802119P Linear algebra I

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Midterm exam or final exam

Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Esa Järvenpää
Working life cooperation:

800300A: Maturity test, 0 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
0 cr
Language of instruction:
Finnish/Swedish
Timing:
Third year
Learning outcomes:
Maturity test
Contents:
Students must take a written maturity test to demonstrate their language skills and how well they know the topic of their thesis. The maturity test is taken in the language in which the student has received his or her education in Finland. If the student has received his or her education in a language other than Finnish or Swedish, the degree programme determines the language of the maturity test. In such cases only the contents of the maturity test is evaluated, not the language.
Mode of delivery:
Maturity test written in examination room.
Learning activities and teaching methods:
Maturity test
Target group:
Major students
Prerequisites and co-requisites:
Bachelor's degree (or similar)
Recommended optional programme components:
-
Recommended or required reading:
-
Assessment methods and criteria:
Maturity test
Read more about assessment criteria at the University of Oulu webpage.
Grading:
Pass/Fail
Person responsible:
Supervisor of thesis
Working life cooperation:
-

800322A: Multidimensional analysis, 8 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Pekka Salmi
Opintokohteen kielet: Finnish
Leikkaavuudet:
800328A  Calculus of several variables  5.0 op
802351A  Vector Calculus  5.0 op
ECTS Credits:
8 cr
Language of instruction:
Finnish
Timing:
Second year, periods 1-2
Learning outcomes:
On successful completion of this course, the student will be able to
- differentiate multivariate functions
- apply the derivative to minimization problems
- define and use multidimensional integrals
Contents:
The course deals with multidimensional real calculus. The topology of $\mathbb{R}^n$ is reviewed, after which differential and integral calculus is derived for vector-valued functions of multiple arguments are derived.
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
56 h lectures, 28 h exercises
Target group:
Major and minor students
Prerequisites and co-requisites:
Linear algebra I
Linear algebra II
Euclidean topology
Series and integrals
Recommended optional programme components:
-
Recommended or required reading:
Lecture notes
Assessment methods and criteria:
Midterm exams or final exam
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible:
Maarit Järvenpää
Working life cooperation:
No

801195P: Probability Theory, 5 op
Voimassaolo: 01.01.2011 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Tuominen, P., 1993
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits
Language of instruction:
Finnish (possible also in English)
Timing:
First year, 2. period
Learning outcomes:
On successful completion of this course, the student will be able to
- solve simple practical problems associated with probability
- solve simple theoretical problems associated with probability
- derive the basic properties of probability, starting from the axioms

Contents:
The course is an introduction to Probability. After review of high school curriculum material, the axiomatic approach to Probability is introduced. The most important concepts are the probability space, conditional probability, independence, a random variable as well as its distribution and expected value.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
32 h lectures, 16 h exercises

Target group:
Major students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction
802154P Elementary functions

Recommended optional programme components:

Recommended or required reading:

Assessment methods and criteria:
Midterm exams or final exam

Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Lasse Holmström

Working life cooperation:

802355A: Rings, Fields and Polynomials, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Kari Myllylää
Opintokohteen kielet: Finnish
Leikkaavuudet:
800333A Algebra I 8.0 op

ECTS Credits:
5 ECTS credits
Language of instruction:
Finnish
Timing:
Second year, 1. period

Learning outcomes:
After completing the course, student is able to
  • derive and proof main results in the course
  • use and apply different proof techniques
  • recognize algebraic structures and the concepts
  • see connections and differences between different algebraic structures

Contents:
The course introduces algebraic structures, such as rings, polynomial rings, ideals, integral domains, fields, finite fields, field extensions and quotient field. The course gives an understanding of algebraic terms and concepts used in mathematics and physics.
Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises

Target group:
Major students

Prerequisites and co-requisites:
802354A Number theory and groups

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Midterm exam or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Kari Myllylä

Working life cooperation:
-

801323A: Seminar, 6 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
  800331A Proseminar 10.0 op

ECTS Credits:
6 cr

Language of instruction:
Finnish (also English)

Timing:
2.-3. year of studies

Learning outcomes:
After completing the Bachelor's thesis, student
- is able to form a clear and logical
- is able to concentrate to important and essential details in the subject of thesis
- gain experience presenting mathematical concept and research studies.

Contents:
Proseminar (Bachelor's thesis) is a small mathematical study based on literature. Student is familiarized to write mathematical texts and obtain information using literature. Thesis includes a oral presentation from the subject of the thesis.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Seminars and own work

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies.

Recommended optional programme components:
Maturity test is written from the topic of Bachelor's thesis.

Recommended or required reading:
-

Assessment methods and criteria:
Opinnäytetyö
802353A: Series and Integrals, 6 op

Voimassaolo: 01.08.2010 -
Opiskelumoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Peter Hästö
Opintokohteen kielet: Finnish
Leikkaavuudet:
   800318A   Analysis 3   5.0 op
   802164P   Series and Integral  5.0 op

ECTS Credits:
6 ECTS credits
Language of instruction:
Finnish (possible also in English)
Timing:
First year, 4. period
Learning outcomes:
After completing the course, student is able to
   • operate with real series
   • separate the concept of continuity and uniform continuity
   • define and calculate Riemann integrals
   • derive and operate function sequences and function series
   • calculate derivate and integrate function series

Contents:
The course is a continuum for the courses Limits and continuity and Derivative. Basic topological methods (presented in Euclidean Topology) are heavily used in proofs and methods involving continuous functions. The goal is the same as in the prerequisite courses, that is, to develop mathematical thinking and extend the knowledge of mathematical analysis.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
30h exercises, 14h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802154P Elementary functions
802155P Limit and continuity
802156P Derivative
802352A Euclidean topology

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Midterm exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
806112P: Basic Methods of Data Analysis, 10 op

Opiskelumuoto: Basic Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jari Päkkilä
Opintokohteen oppimateriaali:
Armitage, P., , 2002
Opintokohteen kielet: Finnish
Leikkaavuudet:
805305A Introduction to Regression and Analysis of Variance 5.0 op

ECTS Credits:
10 cr
Language of instruction:
Finnish
Timing:
2. year, periods 1-2
Learning outcomes:
On successful completion of this course, the student will be able to
- analyze continuous and categorical response in the most common experimental and observational studies
- critically evaluate chosen model
- use some statistical software

Contents:
Skills for performing statistical analyses and inferences on the basis of data obtained in common experimental and observational studies are expanded and deepened. Topics included are e.g. (1) principles of collection, description, and modelling of, and inference on statistical data; (2) basic methods of analysing continuous outcome variables, like comparison of groups, analysis of variance, regression analysis, residuals and model diagnostics, nonparametric methods, treatment of correlated and lifetime (censored) observations; (3) and basic methods of analysing binary, categorical and count data.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 42h exercises

Target group:
Major and minor students.

Prerequisites and co-requisites:
Todennäköisyyslaskennan peruskurssi
806113P Introduction to statistics
802118P Linear algebra I
802154P Elementary functions
802155P Limits and continuity
802156P Derivative

Recommended optional programme components:
To be completed before 805310A Statistical inference I, 806359A Regression modelling and other studies in statistics.

Recommended or required reading:
Lecture notes,

Assessment methods and criteria:
Mid-term exam or final exam. Mid-term exam requires active participation into the course exercises.
801396A: Introduction to Probability Theory II, 5 op

Opiskelumuoto: Intermediate Studies

Laji: Course

Vastuuysikkö: Department of Mathematical Sciences

Arvostelu: 1 - 5, pass, fail

Opintokohteen oppimateriaali:
Tuominen, P., , 1993

Opintokohteen kielet: Finnish

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
2. year, Fall semester

Learning outcomes:
On successful completion of this course, the student will be able to
- understand probability theory deeper than before
- apply various stochastic models
- derive the basic results associated with the new concepts introduced

Contents:
The course is a direct continuation for the course Probability Theory I. The new concepts include for instance the moments of a distribution, the probability generating function, the Law of Large Numbers, the Central Limit Theorem as well as two-dimensional distributions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
24h lectures, 12h exercises

Target group:
Major- and minor students. Recommended for students aiming to Master's degree with major in statistics or major in mathematics and computer sciences.

Prerequisites and co-requisites:
801195P Introduction to probability I
802352A Euclidean topology
802353A Series and integrals

Assessment methods and criteria:
Final exam

Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Kenneth Nordström.

806359A: Regression modelling, 10 op

Voitmassoalo: 01.08.2012 -

Opiskelumuoto: Intermediate Studies

Laji: Course

Vastuuysikkö: Department of Mathematical Sciences

Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish

Leikkaavuudet:
- 805351A Linear Regression 5.0 op
- 805352A Generalized Linear Models 5.0 op

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
2. year, periods 2-3

Learning outcomes:
After successful completion of the course the student is able to describe the basic concepts and assumptions of generalized linear models, as well as main principles of regression modelling, and is also able to apply these methods in the analysis of experimental or observational data.

Contents:
Generalized linear regression models for continuous, binary and count responses; model formulation, selection of variables and interpretation of parameters; fitting of models, estimation of parameters and prediction by the method of maximum likelihood; model criticism and diagnostics; use of R environment and SAS software in modelling.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (56 h), calculation and computation practicals (28 h), independent work.

Target group:
Major and minor students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics (core studies), 801396A Introduction to probability II, 806112P Basic methods of data-analysis, and 805310A Statistical inference I

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Esa Läärä

Working life cooperation:
-

805310A: Statistical Inference I, 10 op

Opiskelumuoto: Intermediate Studies

Laji: Course

Vastuuysikkö: Department of Mathematical Sciences

Arvostelu: 1 - 5, pass, fail

Opintokohteen oppimateriaali:
Pawitan, Yudi, , 2001
Sprott, D. A., , 2000
Kalbfleisch, J. G., , 1985

Opintokohteen kielet: Finnish

Leikkaavuudet:
- 805349A Likelihood Inference 5.0 op
- 805350A Estimation and Test Theory 5.0 op

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
2. or 3. year spring semester (periods 3-4).

**Learning outcomes:**
After successful completion of the course the student is able to describe the main principles of frequentist statistical inference, derive likelihood functions and from these compute point and interval estimates, test statistics and P-values for models with few parameters, as well as to interpret results such obtained.

**Contents:**
Statistical model and observed data; likelihood function, log-likelihood, score and information; construction and properties of point and interval estimates; likelihood ratio, score and Wald statistics and their asymptotic sampling distributions; jackknife and bootstrap methods; elements of Bayesian inference; Use of R environment in inferential tasks.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
Lectures (56 h), calculation and computation practicals (28 h), and independent work.

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
Introduction to propability I
Basic methods of data-analysis

**Recommended optional programme components:**
Requirement for further studies in statistics.

**Assessment methods and criteria:**
Mid-term exams or final exam
Read more about [assessment criteria](https://www.oulu.fi) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Hyon-Jung Kim-Ollila

**Working life cooperation:**
-

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**805340A: Statistical Software, 4 op**

**Opiskelumuoto:** Intermediate Studies

**Laji:** Course

**Vastuuysikkö:** Department of Mathematical Sciences

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
805353A Statistical Software 5.0 op

**ECTS Credits:**
4 cr

**Language of instruction:**
English

**Timing:**
3. year studies. Fall semester. Timing varies.

**Learning outcomes:**
After successful completion of the course the student can use independently major statistical software needed in data analysis.

**Contents:**
The course covers R, SAS and SPSS, and their most important tools for data management, statistical computation, graphics and programming will be introduced and proficiency for their fluent use is acquired.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
34 h lectures and computer class exercises.

**Target group:**
Major and minor students
Prerequisites and co-requisites:
Basic methods of data-analysis

Recommended optional programme components:
- 

Recommended or required reading:
- 

Assessment methods and criteria:
Home work
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Hyon-Jung Kim-Ollila

Working life cooperation:
- 

**H326635: Optional intermediate studies in statistics, 0 - 180 op**

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

**Electives**

**805324A: Time series analysis, 5 op**

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C. , , 1993
Lütkepohl, Helmut , , 1991
Hamilton, James D. , , 1994
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply computer programs to fit time series models. Furthermore, a student learns to read scientific articles about time series.

Contents:
The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH). Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

Recommended or required reading:

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä

806351A: Introduction to Independent Component Analysis, 4 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805334A: Analysis of categorical data, 9 op

Voimassaolo: - 28.02.2011
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
9 cr

Learning outcomes:
A student who has successfully completed the course is supposed to
- be familiar with generalized linear models and to be able to use them when studying discrete data
- be able to model the behaviour of ordinal dependent variables
- be able to make use of so-called mixed models while studying discrete or ordinal data

Contents:
The course deals with the analysis of contingency tables and with models for qualitative and ordinal dependent variables. Models for truncated dependent variables are also briefly touched. A majority of these models can be interpreted as generalised linear models (GLIM). This is why the essentials of the GLIM-theory and the corresponding phraseology is presented. So-called generalised mixed linear models (including random effects) and the estimation of their parameters by the GEE and the ML methods are also discussed. The course can be taken either as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of exercises in the computer lab.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Markku Rahiala

805328A: Multivariate analysis, 9 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
805333A: Robust methods, 6 op

Voimassaolo: - 31.07.2007
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

805398A: An introduction to stochastic modelling, 8 op

Voimassaolo: - 01.09.2012
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805380A: Clinical biostatistics, 6 op

Voimassaolo: - 01.09.2012
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

806330A: Analysis of Market Risk, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen kielet: Finnish

Leikkaavuudet:
806630S Market Risk Analysis 5.0 op

ECTS Credits:
5 cr
Language of instruction: Finnish

Timing:
3. year of studies or later. Timing varies.

Learning outcomes:
The student knows how to estimate the unconditional value-at-risk using empirical quantiles, parametric modeling, semiparametric modeling, and extreme value theory. The student knows also how to estimate the conditional value-at-risk using GARCH models. The student can read scientific articles about risk management.

Contents:
The course is an introduction to the quantitative risk management of a portfolio of stocks. The course introduces various risk measures, extreme value theory, and modeling of financial time series. The course covers:
- conditional and unconditional loss distribution,
- Value-at-Risk and other risk measures, standard methods of estimating
- Value-at-Risk: multivariate normal modeling, historical simulation/empirical quantiles, and the Monte Carlo method,
- modeling of distributions: multivariate distributions, normal mixture distributions, spherical and elliptical distributions, and dimension reduction,
- modeling of financial time series: ARMA models, GARCH models, and volatility models, copulas and measures of dependence,
- extreme value theory: block maxima and threshold exceedance methods.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises.

Target group:
students of mathematical sciences, students of finance and economics

Prerequisites and co-requisites:
806113P Introduction to Statistics

Recommended optional programme components:

Recommended or required reading:

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Jussi Klemelä

Working life cooperation:

Other information:
Home page of the course is http://cc.oulu.fi/~jklemela/marketrisk/

805309A: Statistical methods in epidemiology, 9 op

Voimassaolo: 01.06.2009 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintojakson oppimateriaali:
Santos Silva, Isabel dos, , 1999
Clayton, David, , 1993
Rothman, Kenneth J., , 1998
Opintojakson kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805339A: The Statistical Foundation of Econometrics, 5 - 6 op

Voimassaolo: 01.06.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintojakson oppimateriaali:
Hayashi, Fumio, , 2000
Gourieroux, Christian, , 1995
Gourieroux, Christian, , 1995
Harvey, Andrew C., , 1990
Opintojakson kielet: Finnish
Leikkaavuudet:
805683S Econometrics 5.0 op

ECTS Credits:
5/6 cr

Learning outcomes:
The course familiarizes students with applications of statistical models when inferences are made on economic phenomena. The principles of statistical inference on economic phenomena are the same as those of general statistical inference but there are some special issues that make the inference different in economics than in other application areas of statistics. After finishing the course, a student can apply both linear regression and nonlinear regression and a student is able to apply the generalized method of moments as well as the method of instrumental variables. A student can diagnose the validity of the assumptions of the linear regression model and tune his inferences accordingly.

Contents:
The course starts with the study of the linear regression model, and covers asymptotic inference related to the linear regression model, tests of the parameter restrictions and tests of a structural change. Besides linear regression, also nonlinear regression and the generalized method of moments is covered, as well as inference based on instrumental variables and problems stemming from measurement errors. Inference under heteroscedasticity and autocorrelated disturbances is included. The basic theory of time series analysis (cointegration and autoregressive conditional heteroscedasticity) and the basic theory of panel data is included.

Recommended or required reading:
William H. Greene: Econometric Analysis (Prentice Hall)

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä
805332A: Design of experiments, 9 op

Voimassaolo: 31.07.2007
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

805308A: Analysis of longitudinal data, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Peter J. Diggle et al., , 2002
Hsiao, Cheng , , 2003
McCulloch, Charles E. , , 2001
Fitzmaurice, Garrett M. , , 2004
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr
Learning outcomes:
A student who has successfully completed the course is supposed to
- be familiar with so-called mixed models for both discrete and continuous dependent variables
- be able to make use of these mixed models while studying longitudinal data

Contents:
The purpose of the course is to teach the students, how one can simultaneously study dependencies
between observed variables and variations between individuals in the panel. Linear and non-linear mixed
models, variograms and so-called growth curve models are introduced as central inferential tools for these
studies. Model diagnostics, dynamic ARX-type models and the GMM estimation principle also get a lot of
attention. A major part of the course deals with modelling continuous dependent variables, but cases of
qualitative, ordinal and count dependent variables are covered as well. The course can be taken either
as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of
exercises in the computer lab.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.
Person responsible:
Markku RAhiala

806357A: Statistical finance, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen kielet: Finnish
800697S: Pro Gradu Thesis, 20 op

Opiskelumuoto: Advanced Studies
Laji: Diploma thesis
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
20 cr

Language of instruction:
Finnish (also English)

Timing:
5. year of studies

Learning outcomes:
After writing the Master's degree, student has written an analytical and logical study of a problem or theory in a field of mathematics, applied mathematics or statistics. Completing the thesis successfully, student is able to write scientific articles and texts in mathematics.

Contents:
The scope of the Master's thesis is 20 cr for Teacher students and 30 cr in other disciplines. In Master's thesis, the student engages in researching a specific mathematical area or problem in the field of mathematics, applied mathematics or statistics.

Mode of delivery:
Thesis

Learning activities and teaching methods:
Own work, meetings with the supervisor

Target group:
Major students

Prerequisites and co-requisites:
Bachelor's degree (or equivalent), 20-50 cr advanced studies

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Thesis
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Professors and other teaching personnel

Working life cooperation:
-

802632S: Special course for teachers of mathematics, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Pekka Salmi
Opintokohteen kielet: Finnish

Leikkaavuudet:
802641S Special Course for Teachers of Mathematics: Training 2.0 op
802640S Special Course for Teachers of Mathematics: High School Mathematics 3.0 op
802639S Special Course for Teachers of Mathematics: Content Planning 5.0 op
ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
4.-5. year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- combine mathematical thinking and teaching
- plan mathematical tasks which support profound mathematical understanding rather than computational procedures

Contents:
This module aims at bridging the gap between the mathematical content in the BSc with the skills needed for teaching at schools. It consists of the following parts:

Content planning (4 cr)
This part involves planning and implementing tutorials for conceptual understanding for freshmen. The planning is done as group work and it is supported by a seminar.

Matriculation exam questions (3 cr)
This part is delivered by the normal school teachers. It covers scoring of the national exam's questions.

Other (3 cr)
This part contains practical experience of working as a teacher of mathematics, e.g. as a tutor.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures, seminars (depending the selected modules)

Target group:
Teacher students

Prerequisites and co-requisites:
Studies required in Bachelor's degree

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Modules included have different types of criterias.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Pekka Salmi

Working life cooperation:
-

H325003: Mathematics, optional advanced studies, 0 - 120 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.
802653S: Lebesgue Measure and Integration Theory, 5 op

- **Voimassaolo:** 01.08.2010 -
- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opettajat:** Mikael Lindström
- **Opintokohteen kielet:** Finnish

**Assessment methods and criteria:**
Read more about [assessment criteria](#) at the University of Oulu webpage.

801698S: Cryptography, 5 op

- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
- **Opettajat:** Tapani Matala-aho
- **Opintokohteen oppimateriaalit:**
  - Trappe, Wade; Washington, Lawrence C., 2005
- **Opintokohteen kielet:** Finnish

**Learning outcomes:**
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

**Contents:**
In our lectures we study mathematical basics of encrypting, key exchange and signature systems. As examples, we mention elementary group and number theory used in primality tests and factoring, complexity estimates of computations-in particular in finite fields, repeated squaring and discrete logarithm in finite cyclic groups- applied in multiplicative groups of finite fields and addition groups of elliptic curves. Deduction of addition formulae in projective and affine Weierstrass elliptic curves. Diffie-Hellman key exchange, ElGamal encrypting and signature systems in finite cyclic groups applied in finite fields or in elliptic curves defined over finite fields. DSA, ECDSA, Massey-Omura. Some algorithms and tests: AKS, Fermat, Lenstra , Lucas, Miller-Rabin, Pohlig-Hellman, Pollard's p-1 and rho, pseudoprimes, quadratic sieve, Solovay-Srassen.

**Assessment methods and criteria:**
Read more about [assessment criteria](#) at the University of Oulu webpage.

802655S: Continued Fractions, 5 op

- **Voimassaolo:** 01.01.2011 -
- **Opiskelumuoto:** Advanced Studies
- **Laji:** Course
- **Vastuuysikkö:** Department of Mathematical Sciences
- **Arvostelu:** 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Language of instruction:
FI/EN

Recommended or required reading:
Kenneth H. Rosen: Elementary number theory and its applications.
Lisa Lorentzen and Haakon Waadeland: Continued Fractions with Applications (1992).
Oskar Perron: Die Lehre von den Kettenbruchen (1913).

Course material: http://cc.oulu.fi/~tma/OPETUS.html

802644S: Introduction to Functional Analysis, 10 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelut: 1 - 5, pass, fail
Opettajat: Mahmoud Filali
Opintokohteen kielet: Finnish

Learning outcomes:
If we think of functional analysis as infinite dimensional linear algebra, then the course offers the tools and the ways to handle this infinite dimension. After completing the course successfully, the student will be able to follow almost any material on functional analysis.

Contents:
After recalling some basic definitions on linear algebra and giving the basic definitions concerning normed spaces, we present the uniform boundedness principle and the open mapping theorem. In this first part of the course, the relative compactness of the unit ball in a normed space is studied under the norm topology. Hahn-Banach Theorem is presented in its various forms: algebraic, analytic and geometric, and followed by Krein-Milman Theorem. We end up with the weak topology on normed spaces and the weak* topology on Banach duals. The relative compactness of the unit ball is studied with respect to these two topologies.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Mahmoud Filali

802636S: Information Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelut: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen oppimateriaali:
Ash, Robert, , 1990
Cover, Thomas M.; Joy, Thomas A., , 2006
Gallager, Robert G., , 1968
MacKay, David J. C., , 2003
Opintokohteen kielet: Finnish

ECTS Credits:
160 cr

Learning outcomes:
On successful completion of this course, the student will be able to
- explain the basic concepts and results of information theory
- solve mathematical information theoretic problems
- derive the central results of the theory

Contents:
The course is an introduction Claude Shannon's mathematical theory of communication. The focus is on the information content of an information source, compression of information, coding, transmission of coded information through an information channel as well as decoding of the received message.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Lasse Holmström

802635S: Introduction to partial differential equations, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen oppimateriaali:
Colton, David, , 1988
Kress, Rainer, , 1999
Folland, Gerald B., , 1995
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Learning outcomes:
On successful completion of this course, the student will be able to
- solve linear and quasi-linear partial differential equations of first order using the method of characteristics
- apply the method of separation of variables to solve initial-boundary value problems for heat, wave and Laplace equations
- verify that a given function is a fundamental solution of a partial differential operator
- use single and double layer potentials to solve boundary value problems for Laplacian

Contents:
Linear and nonlinear equations of the first order, trigonometric Fourier series, Laplace equation in R^n and in bounded domains, potential theory, Green's function, Heat equation in R^n and in bounded domains, Wave equation in R^n and in bounded domans, d'Alembert formula for any dimensions, Fourier method.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Valeriy Serov

802652S: Hilbert Spaces, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
  800624S  Analysis III  10.0 op

ECTS Credits:
5 ECTS credits
Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

800651S: Functional analysis, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr
Language of instruction:
Finnish (English if neede)
Timing:
4-5 year of studies. Timig varies.
Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results in functional analysis.
- apply the results and methods of the course in various problems both in pure and applied mathematics.

Contents:
The course presents the theory of Banach and Hilbert spaces, Banach fixed point theorem, basic theory of
operators, Baire category theorem, principle of uniform boundedness, open mapping theorem, closed
graph theorem, Hahn-Banach theorem, compact operators and their spectrum.

Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
56h lectures, 24h exercises
Target group:
Major students
Prerequisites and co-requisites:
Compulsory basic and intermediate studies.
Recommended optional programme components:
-
Recommended or required reading:
Lecture notes
K. Astala, P. Piiroinen, H.-O. Tylli, Funktionaalianalyysin peruskurssi, Helsingin yliopisto, luentomoniste
2008.

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible:
Mikael Lindström
Working life cooperation:
-

802629S: Function estimation, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods

Learning outcomes:
Upon completing the course the student will be able to
- characterise the basic features non-parametric function estimation methods
- apply such estimation methods to practical problems
- derive some of the basic results of non-parametric function estimation for kernel estimators

Contents:
The course focuses on the theory and practice of non-parametric function estimation with a special emphasis on kernel methods. The particular functions considered are a probability density function and a regression function.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions. Probability theory I. Probability theory II or Random variables and distributions.

Recommended optional programme components:
No

Recommended or required reading:
Lecture notes written by the instructor.

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the homework problems he/she has solved during the course. This is agreed in the beginning of the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström
800674S: Fourier transform and distributions, 10 op

Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Valeriy Serov  
Opintokohteen oppimateriaali:  
Stein, Elias M.; Shakarchi R., , 2003  
Taylor, Michael E., , 1996  
Grafakos Loukas , , 2004  
Stakgold, Ivar , , 1998  
Opintokohteen kielet: Finnish

ECTS Credits:  
10 cr  
Language of instruction:  
English  
Timing:  
4.-5. year of studies. Timing varies.

Learning outcomes: 
On successful completion of this course, the student will be able to 
- calculate the Fourier transform of a given integrable function on the line  
- perform basic operations, such as differentiation, convolution and Fourier transformation, on distributions  
- use Fourier transform to find, and provide estimates for, fundamental solutions of partial differential operators  
- formulate direct and inverse scattering problems for the Schrödinger operator

Contents: 

Mode of delivery: 
Face-to-face teaching

Learning activities and teaching methods: 
56h lectures, 28h exercises

Target group: 
Major students

Prerequisites and co-requisites: 
Euclidean topology, Series and integrals, Multidimensional analysis, Complex analysis I and II, and Linear algebra I and II.

Recommended optional programme components: 

Recommended or required reading: 
Luentomoniste  
L. Grafakos: Classical and Modern Fourier Analysis, Pearson Education, 2004;

**Assessment methods and criteria:**

Final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**

1-5

**Person responsible:**

Valeriy Serov

**Working life cooperation:**

-

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**802647S: Fourier series and the discrete Fourier transform, 10 op**

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<thead>
<tr>
<th>Voimassaolo:</th>
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<tr>
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<td>Department of Mathematical Sciences</td>
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<td>1 - 5, pass, fail</td>
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<td>Valeriy Serov</td>
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Ei opintojaksokuvauksia.

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**802656S: Algebraic numbers, 5 op**

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<td>Department of Mathematical Sciences</td>
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<td>Arvostelu:</td>
<td>1 - 5, pass, fail</td>
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<td>Opintokohteen kiele:</td>
<td>Finnish</td>
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**Language of instruction:**

FI/EN

**Learning outcomes:**

As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course.

More detailed: For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding.

When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

**Contents:**

First we revise some basics of rings and fields which are needed to proceed ahead field extensions. In particular, divisibility in an integral domain is carefully studied yielding to applications in the theory of polynomial algebra and algebraic integers.

The theory of algebraic numbers is strongly based on polynomial algebra, where the properties of zeros and divisibility of polynomials are considered.

The definition of an algebraic number will be generalized to the algebraic elements of field extensions going forward to algebraic fields. Considered as most important algebraic fields we get number fields which are finitely generated subfields of the field \( \mathbb{A} \) of all complex algebraic numbers. In particular, we study quadratic number fields.
Further, we shall consider the divisibility and factorization of algebraic integers with some applications to Diophantine equations.

Prerequisites and co-requisites:
Algebra I and II, Linear algebra I and II, Basics in Number Theory (Number theory I)

Recommended or required reading:
I.N. Stewart and D.O. Tall: Algebraic number theory.
Daniel Marcus: Number fields.
J.B. Fraleigh: Abstract algebra.
Michael Artin: Algebra.

Course material: http://cc.oulu.fi/~tma/OPETUS.html

802637S: Advanced Problem Solving, 2 - 6 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Peter Hästö
Opintokohteen kielet: English

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802645S: Number Theory A, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802646S: Number Theory B, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802631S: Modern real analysis, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Learning outcomes:
On successful completion of this course, the student will be able to
- derive and prove basic results of modern real analysis.
- apply the results and methods of modern real analysis in different topics of mathematics, like in the theory of partial differential equations.

Contents:
The course presents Lebesgue spaces (Hölder’s and Minkowski’s inequalities, completeness, dual spaces), the Vitali covering theorem, the Hardy-Littlewood maximal function, approximation with smooth functions using convolution, Lebesgue’s density theorem, Sobolev’s inequalities.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

800688S: Theory of Optimization, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikko: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Erkki Laitinen
Opintokohteen oppimateriaali:
Luenberger, David G., , 1984
Peressini, Anthony L. , , 1988
Opintokohteen kielet: Finnish
Leikkaavuudet:
802666S Linear Optimization 5.0 op

ECTS Credits:
10 cr
Language of instruction:
Finnish
Timing:
4.-5. year of studies. Timing varies.
Learning outcomes:
On successful completion of this course, the student will be able to
- identify the correct methods for solving the conventional optimization problems
- implement the most typical numerical algorithms for solving linear and nonlinear optimization problems

Contents:
The lecture course is focused to methods, which can apply for solving essential optimization problems of technical and economical sciences. The lectures consist of following topics: Linear programming, convex sets and functions and nonlinear convex optimization. The topics are considered theoretically and also numerical algorithms for problem solution are presented.

Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
56h lectures, 28h exercises
Target group:
Major students
Prerequisites and co-requisites:
Euclidean topology, Series and integrals, and Linear algebra I and II
Recommended optional programme components:
- 

Recommended or required reading:

Assessment methods and criteria:
Mid-term exam or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Erkki Laitinen

Working life cooperation:
-

800660S: Group Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Niemenmaa Markku
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
4-5 year of studies. Timing varies.

Learning outcomes:
On successful completion of this course, the student will be able to
- use different proving techniques related to the theory
- prove the Sylow theorems and deal with their applications
- prove important results in the theory of finite solvable groups

Contents:
Aim: To provide the student with the basics of group theory and its development during the past hundred years. Basics of group theory, permutations, studies on the arithmetical

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 56 h, exercises 28 h.

Target group:
Major students

Prerequisites and co-requisites:
802355A Number theory and groups
802355A Rings, Fields and polynomials
800343A Permutations, fields and Galois' theory

Recommended optional programme components:
-
Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Mid-term exam or final exam.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Markku Niemenmaa

Working life cooperation:
-

802633S: Statistical Pattern Recognition, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen oppimateriaali:
Duda, Richard O., 2001
Theodoridis, Sergios, 2002
Webb, A. R., 2002
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
Spring semester, 3rd and 4th periods.

Learning outcomes:
Upon completing the course the student will
-be familiar with the most common classifiers used in pattern recognition
-be able to apply pattern recognition methods to practical problems
-be able derive some of the basic mathematical results of pattern recognition theory

Contents:
The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

Recommended or required reading:
Lecture notes.
Optional reading:

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

801643S: Topology, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Mahmoud Filali
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr

Language of instruction:
English (also Finnish)

Timing:
3.-5. year of studies. Timing varies.

Learning outcomes:
After completion of the course, the student should be able to follow more advanced courses or seminars on abstract harmonic analysis.

Contents:
This is an advanced course, aimed to final year students and to postgraduate students. The course covers topological groups and their uniform structures; subgroups, Quotient groups and product groups; and invariant pseudo-metrics on groups. The last part of the course presents some basics on compact semigroups with some examples such as Ellis group and semigroup compactifications

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56h lectures, 28h exercises

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics, 800329A Topologia I

Recommended optional programme components:
- 

Recommended or required reading:
Lecture notes
Assessment methods and criteria:
Mid-term exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mahmoud Filai

802651S: Measure and Integration, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802650S: Fractal Geometry, 10 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Esa Järvenpää
Opintokohteen kielet: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

802660S: Operator theory and integral equations, 10 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen kielet: English

Ei opintojaksokuvauksia.

H326603: Statistics optional advanced studies, 0 - 120 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohde: Statistical methods in epidemiology, 9 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Läääärä Esa
Opintokohteen oppimateriaali:
Santos Silva, Isabel dos, 1999
Clayton, David, , 1993
Rothman, Kenneth J., , 1998
Opintokohde: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Opintokohde: Analysis of longitudinal data, 5 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Peter J. Diggle et al., , 2002
Hsiao, Cheng, , 2003
McCulloch, Charles E., , 2001
Fitzmaurice, Garrett M., , 2004
Opintokohde: Finnish

ECTS Credits:
5 cr

Learning outcomes:
A student who has successfully completed the course is supposed to
- be familiar with so-called mixed models for both discrete and continuous dependent variables
- be able to make use of these mixed models while studying longitudinal data

Contents:
The purpose of the course is to teach the students, how one can simultaneously study dependencies
between observed variables and variations between individuals in the panel. Linear and non-linear mixed
models, variograms and so-called growth curve models are introduced as central inferential tools for these
studies. Model diagnostics, dynamic ARX-type models and the GMM estimation principle also get a lot
of attention. A major part of the course deals with modelling continuous dependent variables, but cases of
qualitative, ordinal and count dependent variables are covered as well. The course can be taken either
as a graduate course or as an undergraduate course. It consists of 52 hours of lectures and 36 hours of
exercises in the computer lab

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Person responsible:
Jussi Klemelä
805679S: Time series analysis, 5 op

Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettaja: Jussi Klemelä  
Opintokohteen oppimateriaali:  
Harvey, Andrew C., , 1993  
Lütkepohl, Helmut , , 1991  
Hamilton, James D., , 1994  
Opintokohteen kielet: Finnish  
ECTS Credits:  
5 cr  
Learning outcomes:  
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply computer programs to fit time series models. Furthermore, a student learns to read scientific articles about time series.  
Contents:  
The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram.  
Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH). Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities.  
Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.  
Recommended or required reading:  
Assessment methods and criteria:  
Read more about assessment criteria at the University of Oulu webpage.  
Person responsible:  
Jussi Klemelä  

805683S: The Statistical Foundation of Econometrics, 5 - 6 op

Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuysikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettaja: Jussi Klemelä  
Opintokohteen oppimateriaali:  
Harvey, Andrew C. , , 1990  
Hayashi, Fumio , , 2000  
Gourieroux, Christian , , 1995  
Gourieroux, Christian , , 1995  
Opintokohteen kielet: Finnish  
Leikkaavuudet:  
805339A The statistical foundations of econometrics 5.0 op  
ECTS Credits:
5/6 cr

**Language of instruction:**
Finnish

**Learning outcomes:**
The course familiarizes students with applications of statistical models when inferences are made on economic phenomena. The principles of statistical inference on economic phenomena are the same as those of general statistical inference but there are some special issues that make the inference different in economics than in other application areas of statistics. After finishing the course, a student can apply both linear regression and nonlinear regression and a student is able to apply the generalized method of moments as well as the method of instrumental variables. A student can diagnose the validity of the assumptions of the linear regression model and tune his inferences accordingly.

**Contents:**
The course starts with the study of the linear regression model, and covers asymptotic inference related to the linear regression model, tests of the parameter restrictions and tests of a structural change. Besides linear regression, also nonlinear regression and the generalized method of moments is covered, as well as inference based on instrumental variables and problems stemming from measurement errors. Inference under heteroscedasticity and autocorrelated disturbances is included. The basic theory of time series analysis (cointegration and autoregressive conditional heteroscedasticity) and the basic theory of panel data is included.

**Recommended or required reading:**
William H. Greene: Econometric Analysis (Prentice Hall)

**Assessment methods and criteria:**
Read more about assessment criteria at the University of Oulu webpage.

**Person responsible:**
Jussi Klemelä.

805681S: Generalized Linear Models, 9 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

805699S: Statistical methods in epidemiology, 8 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

806618S: Computationally intensive statistical methods, 9 op

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Department of Mathematical Sciences  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish
806621S: Spatial Data Analysis, 10 op

Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuyksikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806628S: Statistical Finance, 5 op

Voimassaolo: 01.08.2009 -  
Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuyksikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Jussi Klemelä  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806629S: Introduction to Sampling Methods, 4 op

Voimassaolo: 01.01.2010 -  
Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuyksikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Lääätä Esa  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

806630S: Market Risk Analysis, 5 op

Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuyksikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Jussi Klemelä  
Opintokohteen kielet: Finnish  
Leikkaavuudet:  
806330A Analysis of Market Risk 5.0 op

ECTS Credits:  
5 cr  
Language of instruction:  
Finnish  
Timing:  
3. year of studies or later. Timing varies.
Learning outcomes:
The student knows how to estimate the unconditional value-at-risk using empirical quantiles, parametric modeling, semiparametric modeling, and extreme value theory. The student knows also how to estimate the conditional value-at-risk using GARCH models. The student can read scientific articles about risk management.

Contents:
The course is an introduction to the quantitative risk management of a portfolio of stocks. The course introduces various risk measures, extreme value theory, and modeling of financial time series. The course covers:

- conditional and unconditional loss distribution,
- Value-at-Risk and other risk measures, standard methods of estimating Value-at-Risk: multivariate normal modeling, historical simulation/empirical quantiles, and the Monte Carlo method,
- modeling of distributions: multivariate distributions, normal mixture distributions, spherical and elliptical distributions, and dimension reduction,
- modeling of financial time series: ARMA models, GARCH models, and volatility models, copulas and measures of dependence,
- extreme value theory: block maxima and threshold exceedance methods.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises.

Target group:
students of mathematical sciences, students of finance and economics

Prerequisites and co-requisites:
806113P Introduction to Statistics

Recommended optional programme components:
-

Recommended or required reading:

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
Home page of the course is http://cc.oulu.fi/~jklemel/marketrisk/

805651S: Stochastic processes, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Department of Mathematical Sciences
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojakskokuvauksia.
**806622S: Probability, 10 op**

Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuyksikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

**805611S: Mathematical statistics II, 10 op**

Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuyksikkö: Department of Mathematical Sciences  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Jussi Klemelä  
Opintokohteen oppimateriaali:  
Lehmann, E. L., , 2001  
Migon, H. S., , 1999  
Opintokohteen kielet: Finnish  
Leikkaavuudet:  
805627S Theory of Statistical Inference 5.0 op

Assessment methods and criteria:  
Read more about assessment criteria at the University of Oulu webpage.