Opasraportti

(2016 - 2017)

Tutkintorakenteet

Bachelor of Science (mathematical sciences)

Tutkintorakenteen tila: published
Lukuvuosi: 2016-17
Lukuvuoden alkamispäivämäärä: 01.08.2016

Compulsory general studies (vähintään 8 op)

902002Y: English 1 (Reading for Academic Purposes), 2 op
902004Y: English 2 (Scientific Communication), 2 op
800012Y: Orientation for New Students, 3 op
901035Y: Second Official Language (Swedish), Oral Skills, 1 op
901034Y: Second Official Language (Swedish), Written Skills, 1 op

Mandatory general studies

The courses listed below are mandatory general studies. The course Introduction to LaTeX (800149P, 2 op) can be completed togehter with Proseminar (Bachelor's thesis).

H325090: Optional language and general studies, 0 - 10 op

Electives

800149P: Introduction to LaTeX, 2 op
900070Y: Scientific Communication I, 2 op
030005P: Information Skills, 1 op

Compulsory major studies (55 op)

The following studies are compulsory for everyone. Depending on orientation studies, further optional and compulsory studies must be chosen. Also Proseminar (801323A/805331A, 6 op) and maturity (800300A, 0 op) is compulsory.

802355A: Algebraic Structures, 5 op
802354A: Basics in Algebra, 5 op
802162P: Continuity and Limit, 5 op
802163P: Derivative, 5 op
802120P: Introduction to Matrices, 5 op
802161P: Introduction to Real Functions, 5 op
806113P: Introduction to Statistics, 5 op
802151P: Introduction to mathematical deduction, 5 op
802320A: Linear Algebra, 5 op
Orientation modules

In addition to compulsory major studies, students must choose optional studies in major subject depending on line of orientation.

Subject teacher’s orientation module

H325050: Subject teacher’s orientation module, 0 - 100 op

Compulsory studies
- 802357A: Euclidean Spaces, 5 op
- 801323A: Seminar, 6 op
- 800300A: Maturity test, 0 op

Optional studies (min 5 ECTS credits)
- H325035: Optional intermediate studies in mathematics, 0 - 180 op

Electives
- 800329A: Topology, 8 op
- 802362A: Introduction to computational inverse problems, 5 op
- 802328A: Basics in Number Theory, 5 op
- 802331A: Principles to Mathematical Modelling, 8 op
- 802360A: Introduction to inverse problems, 4 op
- 801396A: Introduction to Probability Theory II, 5 op
- 801346A: Introduction to Cryptography, 4 op
- 802364A: Introduction to Mathematical Software, 6 op
- 802322A: Basics in mathematical modelling, 5 op
- 801329A: Mathematics in Teaching, 3 op
- 800104P: Number Systems, 4 op
- 031076P: Differential Equations, 5 op
- 806112P: Basic Methods of Data Analysis, 10 op

H326635: Optional intermediate studies in statistics, 0 - 180 op

Electives
- 805324A: Time series analysis, 5 op
- 805308A: Analysis of longitudinal data, 5 op
- 805349A: Likelihood Inference, 5 op
- 805350A: Estimation and Test Theory, 5 op
- 805351A: Linear Regression, 5 op
- 805352A: Generalized Linear Models, 5 op
- 805353A: Statistical Software, 5 op
- 801396A: Introduction to Probability Theory II, 5 op

Mathematics orientation module

H325051: Mathematics orientation module, 0 - 100 op

Compulsory
- 802335A: Introduction to Real Analysis, 5 op
- 802351A: Vector Calculus, 5 op
- 802358A: Metric Spaces, 5 op
- 801323A: Seminar, 6 op
- 800300A: Maturity test, 0 op

Electives
- H325035: Optional intermediate studies in mathematics, 0 - 180 op

Electives
- 800329A: Topology, 8 op
- 802362A: Introduction to computational inverse problems, 5 op
- 802328A: Basics in Number Theory, 5 op
- 802331A: Principles to Mathematical Modelling, 8 op
- 802360A: Introduction to inverse problems, 4 op
- 801396A: Introduction to Probability Theory II, 5 op
- 801346A: Introduction to Cryptography, 4 op
- 802364A: Introduction to Mathematical Software, 6 op
802322A: Basics in mathematical modelling, 5 op
801329A: Mathematics in Teaching, 3 op
800104P: Number Systems, 4 op
031076P: Differential Equations, 5 op
806112P: Basic Methods of Data Analysis, 10 op
H326635: Optional intermediate studies in statistics, 0 - 180 op

Electives
805324A: Time series analysis, 5 op
805308A: Analysis of longitudinal data, 5 op
805349A: Likelihood Inference, 5 op
805350A: Estimation and Test Theory, 5 op
805351A: Linear Regression, 5 op
805352A: Generalized Linear Models, 5 op
805353A: Statistical Software, 5 op
801396A: Introduction to Probability Theory II, 5 op

Statistics orientation module
H326650: Statistics orientation module, 0 - 100 op

Compulsory
802351A: Vector Calculus, 5 op
806112P: Basic Methods of Data Analysis, 10 op
805331A: Project seminar I, 6 op
800300A: Maturity test, 0 op

Electives
H326635: Optional intermediate studies in statistics, 0 - 180 op

Electives
805324A: Time series analysis, 5 op
805308A: Analysis of longitudinal data, 5 op
805349A: Likelihood Inference, 5 op
805350A: Estimation and Test Theory, 5 op
805351A: Linear Regression, 5 op
805352A: Generalized Linear Models, 5 op
805353A: Statistical Software, 5 op
801396A: Introduction to Probability Theory II, 5 op
H325035: Optional intermediate studies in mathematics, 0 - 180 op

Electives
800329A: Topology, 8 op
802362A: Introduction to computational inverse problems, 5 op
802328A: Basics in Number Theory, 5 op
802331A: Principles to Mathematical Modelling, 8 op
802360A: Introduction to inverse problems, 4 op
801396A: Introduction to Probability Theory II, 5 op
801346A: Introduction to Cryptography, 4 op
802364A: Introduction to Mathematical Software, 6 op
802322A: Basics in mathematical modelling, 5 op
801329A: Mathematics in Teaching, 3 op
800104P: Number Systems, 4 op
031076P: Differential Equations, 5 op
806112P: Basic Methods of Data Analysis, 10 op

Minor subjects (vähintään 50 op)

Bachelor studies contains also studies in major and minor subjects. The minimum requirement is that student does either two smaller minor subjects (at least 25 cr each) OR one larger minor subject (at least 60 cr).

Minor studies for students in teacher education

The choice of minor subjects defines how students qualify as teachers. Pedagogical studies for teachers forms a natural 30 cr minor subject for those students who are doing teachers studies. The other minor subject should be either physics, chemistry or computer sciences. Any other combinations should be applied separately from the Faculty of Sciences. Notice that when minimum requirements are fullfilled, one is free to choose other minor subjects (taking the study permissions into account).
Remark. Master studies in different programs might contain different requirements for major and minor studies. These requirements should be taken into account when choosing minor studies in Bachelor’s degree. More information can be found in the Study Guide.

Physics as a minor subject

Chemistry as a minor subject

Computer sciences as a minor subject

Pedagogical studies

Other minor studies

Other studies

This part contains all courses which are not minor studies, such as, single courses in different subjects, extra language courses, etc.

Master's degree (Mathematical Sciences)

Tutkintorakenteen tila: published

Lukuvuosi: 2016-17

Lukuvuoden alkamispäivämäärä: 01.08.2016

Studies of the line of specialization

Subject teacher’s orientation

800600S: Maturity test, 0 op
800697S: Pro Gradu Thesis, 20 op
802639S: Special Course for Teachers of Mathematics: Content Planning, 5 op
802640S: Special Course for Teachers of Mathematics: High School Mathematics, 3 op
802641S: Special Course for Teachers of Mathematics: Training, 2 - 5 op
H325052: Subject teacher's advanced module, 0 - 100 op

Advanced studies for subject teacher students
802662S: Supervising advanced problems, 5 op
802648S: Mathematical Problem Solving, 10 op
800660S: Group Theory, 10 op
802655S: Continued Fractions, 5 op
802656S: Algebraic numbers, 5 op
802645S: Number Theory A, 5 op
802646S: Number Theory B, 5 op
802651S: Measure and Integration, 5 op

Mathematics orientation

H325053: Mathematics advanced module, 0 - 100 op

Electives
800660S: Group Theory, 10 op
802655S: Continued Fractions, 5 op
802656S: Algebraic numbers, 5 op
802645S: Number Theory A, 5 op
802651S: Measure and Integration, 5 op
802664S: Differential geometry, 10 op
802644S: Introduction to Functional Analysis, 10 op
802647S: Fourier series and the discrete Fourier transform, 10 op
802635S: Introduction to partial differential equations, 10 op
802665S: Numerical Analysis, 5 op
802666S: Linear Optimization, 5 op
802667S: Nonlinear Optimization, 5 op
802633S: Statistical Pattern Recognition, 10 op
802636S: Information Theory, 10 op
800600S: Maturity test, 0 op
800698S: Pro gradu thesis, 30 op

Statistics orientation

H326651: Statistics advanced module, 0 - 100 op

Compulsory
805642S: Pro gradu thesis, 30 op
805644S: Maturity test, 0 op
805627S: Theory of Statistical Inference, 5 op
805620S: Pro Gradu seminar, 8 op
805628S: Probability Distributions, 5 op
806624S: Practical training/consulting, 5 - 7 op

H326603: Statistics optional advanced studies, 0 - 120 op

Electives
802633S: Statistical Pattern Recognition, 10 op
802636S: Information Theory, 10 op
802629S: Function estimation, 10 op
031051S: Numerical Matrix Analysis, 5 op
806633S: Introduction to Bayesian Statistics, 5 op
805679S: Time series analysis, 5 op

Applied mathematics orientation

H325851: Applied mathematics advanced module, 0 - 100 op

Compulsory Advanced Studies
800698S: Pro gradu thesis, 30 op
800600S: Maturity test, 0 op

Optional Advance Studies
802647S: Fourier series and the discrete Fourier transform, 10 op
802635S: Introduction to partial differential equations, 10 op
802633S: Statistical Pattern Recognition, 10 op
802636S: Information Theory, 10 op
802629S: Function estimation, 10 op
031051S: Numerical Matrix Analysis, 5 op
802665S: Numerical Analysis, 5 op
802666S: Linear Optimization, 5 op
802667S: Nonlinear Optimization, 5 op

Mathematics and computer sciences orientation

H325851: Applied mathematics advanced module, 0 - 100 op

Compulsory Advanced Studies
800698S: Pro gradu thesis, 30 op
800600S: Maturity test, 0 op

Optional Advance Studies
802647S: Fourier series and the discrete Fourier transform, 10 op
802635S: Introduction to partial differential equations, 10 op
802633S: Statistical Pattern Recognition, 10 op
802636S: Information Theory, 10 op
802629S: Function estimation, 10 op
031051S: Numerical Matrix Analysis, 5 op
802665S: Numerical Analysis, 5 op
802666S: Linear Optimization, 5 op
Minor subjects

Other studies

Other studies, which are not included to minor and major subjects.

Opintojaksojen kuvaukset

Tutkintorakenteisiin kuuluvien opintokohteiden kuvaukset

902002Y: English 1 (Reading for Academic Purposes), 2 op

Voimassaolo: 01.08.1995 -
Opiskelumuoto: Language and Communication Studies
Laji: Course
Vastuuysikkö: Languages and Communication
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: English

Proficiency level:

Status:
This course is mandatory for students of the following degree programmes:
Faculty of Science
• Biology
• Chemistry
• Mathematical Sciences
• Physics
Oulu Mining School
• Geosciences degree programme
Faculty of Information Technology and Electrical Engineering
• Department of Information Processing Science

Students in the Department of Geography take English 3.

Engineering students in the following programmes take their English courses in the Faculty of Technology:
Oulu Mining School:
• Mining Technology and Mineral Processing degree programme

Faculty of Information Technology and Electrical Engineering
• Department of Electrical Engineering
• Department of Communications Engineering
• Department of Computer Science and Engineering

Please consult the Faculty Study Guide to establish the language requirements for your own degree program.

Required proficiency level:
English must have been the A1 or A2 language at school or equivalent English skills should have been acquired otherwise.

ECTS Credits:
2 ECTS credits (total work load 54 hours including classroom meetings.)
Language of instruction: English

Timing:
- Biology: 1st year spring term
- Chemistry: 1st year autumn term
- Geology: 1st year spring term
- Information Processing Science: 1st year spring term
- Mathematical Sciences (pedagogy): 1st year spring term
- Mathematical Sciences: 2nd year autumn term
- Physical Sciences: 1st year autumn term

Learning outcomes:
By the end of the course, you are expected to be able to
- have acquired effective vocabulary learning techniques
- be able to distinguish parts of words to infer meanings
- utilize your knowledge of text structure and cohesion markers to understand academic texts
- extract information and learn content from English readings in scientific and professional contexts

Contents:
The course will focus on reading strategies; these include recognizing how texts are organized, identifying key points in a text, and understanding words in context. Vocabulary work in the course will focus on a) academic vocabulary, as used in formal scientific writing, and b) using your knowledge of the meanings of parts of words (affixes) to infer meaning.

Mode of delivery:
Contact teaching

Learning activities and teaching methods:
The scope of the course is 2 op (54 hours student workload).

Target group:
1st year students of Biology, Chemistry, Geology, Information Processing Science, Physics, and Mathematics (pedagogy); 2nd year students of Mathematics

Prerequisites and co-requisites:
-

Recommended optional programme components:
Students are also required to take 902004Y Scientific Communication, which is taken AFTER completion of this course.

Recommended or required reading:
Photocopies will be provided by the teacher and/or required texts will be accessible online or from the university library.

Assessment methods and criteria:
Student work is monitored by continuous assessment. You are required to participate regularly and actively in all contact teaching provided, and successfully complete all required coursework. There will be three monthly tests on material covered so far.

Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Karen Niskanen

Working life cooperation:
-

Other information:
N.B. Students with grades laudatur or eximia in their A1 English school-leaving examination can be exempted from this course and will be granted the credits by the Faculty of Science.

902004Y: English 2 (Scientific Communication), 2 op

Voimassaolo: 01.08.1995 -
Opiskelumuoto: Language and Communication Studies
Laji: Course
Vastuuysikkö: Languages and Communication
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: English
Leikkaavuudet:
Proficiency level:
B2/C1 on the CEFR scales

Status:
This course is mandatory for all 2nd year students (except geographers) who will have English as their foreign language in their B.Sc. degree. This includes the students who were exempted from ‘Reading for Academic Purposes’(902002Y). Please consult the faculty study guide to establish the language requirements on your own degree programme.

Required proficiency level:
Students taking this course must have had English as the A1 or A2 language at school or the equivalent English skills should have been acquired otherwise. The course ‘Reading for Academic Purposes’ (902002Y) is a pre-requisite, unless exempted.

ECTS Credits:
The student workload is 53 hrs work/ 2 ECTS credits.

Language of instruction:
English

Timing:
Biology: 2nd year autumn term
Chemistry: 2nd year spring term
Geology: 2nd year spring term
Information Processing Science: 2nd year autumn term
Mathematics: 2nd year spring term
Physics: 2nd year autumn term

Learning outcomes:
By the end of the course, you are expected:
1. to have demonstrated your use of appropriate strategies and techniques for communicating effectively in English in an academic context.
2. to have demonstrated the ability to prepare and present scientific subjects to your classmates, using appropriate field-related vocabulary.

Contents:
Skills in listening, speaking, and presenting academic topics are practised in the classroom, where there is an emphasis on working in pairs and small groups. Homework tasks include online lecture listening and reading, preparation for classroom discussions and written work to support the classroom learning.

Mode of delivery:
Contact teaching

Learning activities and teaching methods:
Contact teaching 28 hours, homework 28 hours

Target group:
2nd year students of Biology, Chemistry, Geology, Information Processing Science, Mathematics, Physics

Prerequisites and co-requisites:

Recommended optional programme components:
Also required: 902002Y Reading for Academic Purposes Englannin kieli 1

Recommended or required reading:
Course materials will be provided by the teacher.

Assessment methods and criteria:
Continuous assessment is based on regular attendance, active participation in all lessons and the successful completion of all homework tasks.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass / fail.

Person responsible:
Karen Niskanen

Working life cooperation:

Other information:

800012Y: Orientation for New Students, 3 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: General Studies  
Laji: Course  
Vastuuyksikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

901035Y: Second Official Language (Swedish), Oral Skills, 1 op

Voimassaolo: 01.08.2014 -  
Opiskelumuoto: Language and Communication Studies  
Laji: Course  
Vastuuyksikkö: Languages and Communication  
Opintokohteen kielet: Swedish  
Leikkaavuudet:

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<td>ay901035Y</td>
<td>Second Official Language (Swedish), Oral Skills (OPEN UNI)</td>
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901034Y: Second Official Language (Swedish), Written Skills, 1 op

Voimassaolo: 01.08.2014 -  
Opiskelumuoto: Language and Communication Studies  
Laji: Course  
Vastuuyksikkö: Languages and Communication  
Opintokohteen kielet: Swedish  
Leikkaavuudet:

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<tr>
<td>901004Y</td>
<td>Swedish</td>
<td>2.0 op</td>
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H325090: Optional language and general studies, 0 - 10 op

Voimassaolo: 01.08.2015 -  
Opiskelumuoto: General Studies  
Laji: Study module  
Vastuuyksikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Electives

800149P: Introduction to LateX, 2 op

Opiskelumuoto: Basic Studies  
Laji: Course  
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish  
Leikkaavuudet:  
761115P  Laboratory Exercises in Physics 1  5.0 op  
761115P-03  Laboratory Exercises in Physics 1, Introduction to LaTeX  0.0 op  

ECTS Credits:  
2 cr  

Language of instruction:  
Finnish (in english if needed)  

Timing:  
2-3 year of studies, before making the Bachelor's thesis  

Learning outcomes:  
After completing the course, student  
- is able to describe the principles of LaTeX document preparation system  
- can form basic template of LaTeX document and modify it to his/her needs  
- knows basic commands when writing mathematical text  
- is able to use different environments (e.g. enumerations, equations)  
- can recognize and fix errors in LaTeX code  
- is able to write Bachelor's and Master's thesis using LaTeX  

Contents:  
Bachelor's and Master's thesis are written using LaTeX document preparation system. This course introduces basics in LaTeX by giving basic knowledge of the principles of LaTeX.  

Mode of delivery:  
Lectures/exercises (computer class)  

Learning activities and teaching methods:  
Face-to-face teaching  

Target group:  
Major students  

Prerequisites and co-requisites:  
first year math studies  

Recommended optional programme components:  
Must be completed before Bachelor's thesis.  

Recommended or required reading:  
Lecture notes  
Tobias Oetiker, Hubert Partl, Irene Hyna and Elisabeth Schlegl,  The Not So Short Introduction to LATEX2\2pdf  

Assessment methods and criteria:  
Participation in lectures/exercises and home work.  

Grading:  
Pass/Fail  

Person responsible:  
Markus Harju  

Working life cooperation:  
-  

900070Y: Scientific Communication I, 2 op  

Voimassaolo: 01.08.2011 -
Opiskelumuoto: Language and Communication Studies
Laji: Course
Vastuuyksikkö: Languages and Communication
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
- ay900070Y Scientific Communication I (OPEN UNI) 2.0 op

Proficiency level:
-

Status:
This course unit is compulsory for students of Faculty of Education.

Required proficiency level:
-

ECTS Credits:
2 ECTS credits

Language of instruction:
Finnish

Timing:
1st year of studies

Learning outcomes:
Upon completion of the course unit the student should be able to prepare a verbally and stylistically fluent scientific presentation. The student should be able to assess and revise his/her own texts and apply the conventions and practices of scientific writing to his/her own work, especially to his/her scientific theses or dissertations. The student should be able to recognise his/her strengths and weak points as a communicator.

Contents:
The basics and various types of scientific communication. The basic notions of grammatical correctness and the stylistic and formal conventions demanded by proper scientific discourse. Critical approach to source literature and the most common formal standards (referencing techniques, constructing bibliographies etc.). Throughout the course unit the student analyses and produces texts of various types.

Mode of delivery:
Multi-modal teaching

Learning activities and teaching methods:
Contact lessons 20 hrs. Independent study 34 hrs.

Target group:
Students of the Faculty of Education

Prerequisites and co-requisites:
-

Recommended optional programme components:
-

Recommended or required reading:
the Material in the Optima learning environment,

Assessment methods and criteria:
Active participation in teaching and completion of given assignments.
Read more about assessment criteria at the University of Oulu webpage.
Grading:
pass / fail

Person responsible:
Jukka Käräjäoja

Working life cooperation:
-

Other information:
-

030005P: Information Skills, 1 op

Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Faculty of Technology
Arvostelu: 1 - 5, pass, fail
Opettajat: Sassali, Jani Henrik, Ursula Heinikoski
Opintokohteen kielet: Finnish
Leikkaavuudet:
030004P Introduction to Information Retrieval 0.0 op

ECTS Credits:
1 ECTS credit

Language of instruction:
Finnish

Timing:
2nd or 3rd year

Learning outcomes:
Students know the different phases of information retrieval process and basic techniques of scientific information retrieval. They will find the most important reference databases of their discipline and know how to evaluate information sources and retrieval results.

Contents:
Retrieval of scientific information, the retrieval process, key databases of the discipline, and evaluation of information retrieval and information sources.

Mode of delivery:
Blended teaching: classroom training, web-based learning material and exercises in Optima environment, a final assignment on a topic of the student’s own choice

Learning activities and teaching methods:
Training sessions 8h, group working 7h, self-study 12h

Target group:
Compulsory for all students of the Faculty of Technology, the Faculty of Information Technology and Electrical Engineering and the Faculty of Architecture. In the Faculty of Science compulsory for students of biology, physics, geosciences, chemistry and geography. Optional for students of biochemistry and mathematics.

Prerequisites and co-requisites:
-

Recommended optional programme components:
-

Recommended or required reading:
Web learning material https://wiki.oulu.fi/display/030005P.

Assessment methods and criteria:
Passing the course requires participation in the training sessions and successful completion of the course assignments. Read more about assessment criteria at the University of Oulu webpage.

**Grading:**
pass/fail

**Person responsible:**
Science and Technology Library Tellus, tellustieto (at) oulu.fi

**Working life cooperation:**
-

**Other information:**
-

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**802355A: Algebraic Structures, 5 op**

**Voimassaolo:** 01.08.2010 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Kari Myllylä
**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
800333A  Algebra I  8.0 op

**ECTS Credits:**
5 ECTS credits
**Language of instruction:**
Finnish
**Timing:**
Second year, 1. period

**Learning outcomes:**
After completing the course, student is able to
- derive and proof main results in the course
- use and apply different proof techniques
- recognize algebraic structures and the concepts
- see connections and differences between different algebraic structures

**Contents:**
The course introduces algebraic structures, such as rings, subrings, ideals, integral domains, fields and finite fields. The course gives an understanding of algebraic terms and concepts used in mathematics and physics.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
28h lectures, 14h exercises

**Target group:**
Major students

**Prerequisites and co-requisites:**
802354A Number theory and groups

**Recommended optional programme components:**
-

**Recommended or required reading:**
Lecture notes

**Assessment methods and criteria:**
Midterm exam or final exam
Read more about assessment criteria at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
802354A: Basics in Algebra, 5 op

Voimassaolo: 01.08.2010 -  
Opiskelumuoto: Intermediate Studies  
Laji: Course  
Vastuuysikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Kari Myllylä  
Opintokohteen kielet: Finnish  
Leikkaavuudet:  
- ay802354A Number Theory and Groups (OPEN UNI) 5.0 op  
- 800333A Algebra I 8.0 op  

ECTS Credits:  
5 ECTS credits  
Language of instruction:  
Finnish  
Timing:  
1. year, 3. period  
Learning outcomes:  
After completing the course, student is able to  
- derive and proof main results in the course  
- use and apply different proof techniques  
- recognize algebraic structures and the concepts  
- see connections and differences between different algebraic structures  
Contents:  
The course includes basics in arithmetics and algebraic structures, such as, congruence, residue classes, prime numbers, Euclidean algorithm, the fundamental theorem of arithmetic, Euler-Fermat formula, groups and morphisms. The course gives an understanding of algebraic terms and concepts used in mathematics and physics.  
Mode of delivery:  
Face-to-face teaching  
Learning activities and teaching methods:  
28h lectures, 14h exercises  
Target group:  
Major and minor students  
Prerequisites and co-requisites:  
802151P Introduction to mathematical deduction  
Recommended optional programme components:  
-  
Recommended or required reading:  
Lecture notes  
Assessment methods and criteria:  
Midterm exam or final exam  
Read more about assessment criteria at the University of Oulu webpage.  
Grading:  
1-5  
Person responsible:  
Kari Myllylä  
Working life cooperation:  
-  

802162P: Continuity and Limit, 5 op

Voimassaolo: 01.06.2015 -  
Opiskelumuoto: Basic Studies
Lahti: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:

- 800119P Analysis 1 5.0 op
- 802155P Continuity and limit 4.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
1. year, 2. period

Learning outcomes:
After completing the course, student is able to derive and proof main results of the course use different types of proof techniques define the limit of function and the continuity of function derive and proof the limit using different proof techniques deduce the continuity of functions using different proof techniques.

Contents:
The main concept of the course are the limit of a real-valued function and the continuity of real-valued function. Interrelations between these concepts are also studied.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises

Target group:
Main and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Final exam Read more about assessment criteria at the University of Oulu webpage.

Grading:
Failed, 1-5

Person responsible:
Esa Järvenpää

Working life cooperation:
-

Other information:
-

802163P: Derivative, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Basic Studies

Lahti: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:

- 800317A Analysis 2 5.0 op
- 802156P Derivative 4.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
1. year, 3. period

Learning outcomes:
After completing the course, student is able to
- derive and proof main results of the course
- use different types of proof techniques
- use and apply the concept of derivative in different types of problems

Contents:
The course considers the concept of derivative of real-valued function and applies this concept to different types of situations.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14 h exercises

Target group:
Pää- ja sivuaineopiskelijat

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction
802155P Limits and continuity

Assessment methods and criteria:
Final exam

Grading:
Fail, 1-5

Person responsible:
Esa Järvenpää

Working life cooperation:
No

Other information:

802120P: Introduction to Matrices, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
802118P Linear Algebra I 4.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
1. year, autumn

Learning outcomes:
After completing the course the student is able to
- apply arithmetic operations of matrices
- solve system of linear equations by matrix methods and can apply matrix factorizations to find the solution of the system of linear equations.
- recognize the vector space and understands the concepts of basis and dimension of a vector space
- analyse matrices by the parameters, vectors and vector spaces of matrices
- diagonalize matrices and apply diagonalization to the simple problems

Contents:
Vectors and matrices, Systems of linear equations, determinant of a matrix, matrix factorizations, vector spaces, base, dimension, rank of matrix, eigenvalues and eigenvectors of a matrix, diagonalization.
Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 28 h, Exercises and group work 14 h, independent work

Target group:
Major and minor studies

Prerequisites and co-requisites:
802151P Introduction to Mathematical Deduction

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Exercise points and/or exams

Grading:
Fail, 1-5

Person responsible:
Tero Vedenjuoksu

Working life cooperation:
-

Other information:
Homepage in Noppa-portal.

802161P: Introduction to Real Functions, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Leikkaavuudet:
- 802154P Elementary functions  3.0 op
- 800147P Basic Methods in Mathematics I / appl.  8.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
1st year, 1st period

Learning outcomes:
After completing the course the student is able to
- operate with elementary functions
- calculate derivatives and apply them
- use different integration techniques
- apply calculus in problem solving

Contents:
The course concerns real-valued functions of one variable and their calculus. In addition to calculation techniques, effort is made to understand the underlying concepts so that they can be applied in problem solving. The aim of the course is to develop calculation routine as well as deductive skills.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises, 91h study a part of which may be guided

Target group:
Mathematics major and minor students

Prerequisites and co-requisites:
No

Recommended optional programme components:
-
806113P: Introduction to Statistics, 5 op

Voimassaolo: 01.01.2011 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Hanna Heikkinen
Opintokohteen oppimateriaali:
Wild, Christopher J. , , 2000
Grönroos, Matti (2) , , 2003
Opintokohteen kielet: Finnish
Leikkaavuudet:
806118P  Introduction to Statistics  5.0 op
806119P  A Second Course in Statistics  5.0 op
806116P  Statistics for Economic Sciences  5.0 op

ECTS Credits:
5 cr
Language of instruction:
Finnish
Timing:
3rd period. It is recommended to complete the course at the 1st spring semester.
Learning outcomes:
Upon completion of the course, student will be
- able to identify and define the main principles of statistical research, collection of the data and analysis
- able to apply basic methods of descriptive statistics and statistical inference in simple quantitative research using a statistical software
- able to critically evaluate results of the statistical research presented in media
- prepared for teaching statistics in secondary school and high school
- prepared for participating in a group.
Contents:
- the nature and the meaning of statistics
- data and the acquisition of them: observations, variables, measuring and designs of a study
- the descriptive statistics of empirical distributions: tables, graphical presentations and descriptive measures of center, variation and dependence
- the principles and the basic methods of statistical inference: random sample, sample statistics, point estimation, confidence intervals and statistical testing of hypotheses
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
Lectures 16 h (partly compulsory) / instructed group work (28 h) / independent work 80 h. Group works will be returned. Additional independently implemented learning diary tasks. Independent work contains also preparation for group work and peer assessment.
Target group:
Students of mathematical sciences and other interested students.
Prerequisites and co-requisites:
The recommended prerequisite prior to enrolling for the course is the completion of the courses: 802151P Introduction to mathematical deduction, 802154P Elementary functions, 802155P Continuity and limit ja 801195P Introduction to Probability Theory.

Recommended optional programme components:
After the course, student is able to continue other statistics courses.

Recommended or required reading:
Lecture notes.

Assessment methods and criteria:
This course utilizes continuous assessment. Practical works and learning diaries are assessed weekly. The assessment of the course is based on the learning outcomes of the course. The more detailed assessment criteria is available in the beginning of the course. In addition one compulsory lecture and peer assessment. Read more about assessment criteria at the University of Oulu webpage.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Hanna Heikkinen

Working life cooperation:
No

802151P: Introduction to mathematical deduction, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
    ay802151P Introduction to mathematical deduction (OPEN UNI) 5.0 op

ECTS Credits:
5 ECTS

Language of instruction:
Finnish

Timing:
First period at the first semester.

Learning outcomes:
After completing the course, student
- is able to use different methods proving techniques
- is able to use basic set theoretic concepts and definitions
- is able to define and apply basic definitions related to functions

Contents:
The course in an introduction to mathematical deduction and introduces different types of proof techniques. The course covers the concepts familiar from upper secondary school studies more profound way. Main concepts in this course are basic set theory and functions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 30h, exercises 18h

Target group:
Major and minor students

Prerequisites and co-requisites:
-

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam
802320A: Linear Algebra, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
  802119P  Linear Algebra II  5.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd year, 1st period

Learning outcomes:
On successful completion of this course, the student will be able to
- apply the definition of linear space and concepts associated with linear spaces such as basis
- work with linear mappings and their matrix representations
- apply the definition of inner product space and concepts associated with inner product spaces such as orthogonality
- prove results related to linear spaces

Contents:
The aim of the course is to provide the student with the knowledge needed in almost all later courses in mathematics:
abstract vector spaces and subspaces, linear independence and bases, inner product spaces, linear mappings and
concepts associated with linear mappings such as kernel, eigenvalues and eigenvectors.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises, 91h independent study

Target group:
Mathematics majors and minors students

Prerequisites and co-requisites:
802120P Introduction to Matrices

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Final exam

Grading:
1-5, fail

Person responsible:
Pekka Salmi

Working life cooperation:
No

Other information:

801195P: Probability Theory, 5 op

Voimassaolo: 01.01.2011 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Tuominen, P., 1993
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits.

Language of instruction:
Finnish.

Timing:
Fall semester, 2nd period.

Learning outcomes:
Upon completing the course the student will be able to
- solve simple practical problems associated with probability
- solve simple theoretical problems associated with probability
- derive the basic properties of probability, starting from the axioms

Contents:
The course is an introduction to probability. In the beginning high school level probability is reviewed and after that axiomatic treatment of the theory starts. The central concepts discussed include probability space, conditional probability, independence, and random variable together with its distribution and expected value.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
35 h of lectures, 14 h of exercises.

Target group:
Mathematics, applied mathematics and statistics majors. Other students taking mandatory or optional mathematics courses.

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction
802154P Elementary functions

Recommended optional programme components:

- Recommended or required reading:
 Lectures.

Assessment methods and criteria:
Two exams covering the two halves of the course are arranged during the course. Another option is to take an exam that covers the whole course.

Read more about assessment criteria at the University of Oulu webpage.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Pekka Salmi.

Working life cooperation:

- Other information:
Level: intermediate studies.

802164P: Series and Integral, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Leikkaavuudet:
- 800318A Analysis 3 5.0 op
- 802353A Series and Integrals 6.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
1st year, 4th period

Learning outcomes:
After completing the course, the student is able to
- operate with series
- define and calculate Riemann integrals
- formulate the Fundamental Theorem of Calculus and apply it to evaluate integrals

Contents:
The course is continuation for the courses Continuity and Limit and Derivative. The goal is the same as in the prerequisite courses, that is, to develop mathematical thinking and extend the knowledge of mathematical analysis.
The contents of the course are series and Riemann integral. A central result is the Fundamental Theorem of Calculus that connects the Riemann integral to antiderivative.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h exercises, 14h exercises, 91h independent study

Target group:
Mathematics major and minor students

Prerequisites and co-requisites:
- 802162P Continuity and Limit
- 802163P Derivative

Recommended optional programme components:
-

Recommended or required reading:
lecture notes

Assessment methods and criteria:
Final exam

Grading:
1-5, fail

Person responsible:
Mahmoud Filali

Working life cooperation:
No

Other information:
-

H325050: Subject teacher's orientation module, 0 - 100 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Basic and Intermediate Studies
Laji: Study module
Vastuuysikkö: Field of Mathematics

Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Compulsory studies

802357A: Euclidean Spaces, 5 op
Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Ville Suomala
Opintokohteen kielet: Finnish
Leikkaavuudet:
  802352A  Euclidean Topology  4.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
Subject teachers: 2. year 2. period

Learning outcomes:
After passing the course the student
- will be able to define basic topological concepts
- will be able to handle sequences
- will be able to justify basic properties of continuous vector valued functions

Contents:
Sequences, continuity and limit of a vector valued function, basic topological concepts

Mode of delivery:
Contact teaching

Learning activities and teaching methods:
28 hours of lectures, 14 hours of exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction,
802161P Introduction to real functions,
802162P Continuity and limits

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Final exam
Grading:
Fail, 1-5

Person responsible:
Maarit Järvenpää

Working life cooperation:
-

Other information:
-
801323A: Seminar, 6 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
800331A  Proseminar  10.0 op

ECTS Credits:
6 cr
Language of instruction:
Finnish (also English)
Timing:
2.-3. year of studies
Learning outcomes:
After completing the Bachelor's thesis, student
- is able to form a clear and logical
- is able to concentrate to important and essential details in the subject of thesis
- gain experience presenting mathematical concept and research studies.

Contents:
Proseminar (Bachelor's thesis) is a small mathematical study based on literature. Student is familiarized to
write mathematical texts and obtain information using literature. Thesis includes an oral presentation from
the subject of the thesis.
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
Seminars and own work
Target group:
Major students
Prerequisites and co-requisites:
Compulsory basic and intermediate studies.
Recommended optional programme components:
Maturity test is written from the topic of Bachelor's thesis.
Recommended or required reading:
-
Assessment methods and criteria:
Opinnäytetyö
Read more about assessment criteria at the University of Oulu webpage.
Grading:
Pass/Fail
Person responsible:
Maarit Järvenpää
Working life cooperation:
-

800300A: Maturity test, 0 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
0 cr
Language of instruction:
Finnish/Swedish
Timing:
Third year
Learning outcomes:
Maturity test
Contents:
Students must take a written maturity test to demonstrate their language skills and how well they know the topic of their thesis. The maturity test is taken in the language in which the student has received his or her education in Finland. If the student has received his or her education in a language other than Finnish or Swedish, the degree programme determines the language of the maturity test. In such cases only the contents of the maturity test is evaluated, not the language.
Mode of delivery:
Maturity test written in examination room.
Learning activities and teaching methods:
Maturity test
Target group:
Major students
Prerequisites and co-requisites:
Bachelor's degree (or similar)
Recommended optional programme components:
-
Recommended or required reading:
-
Assessment methods and criteria:
Maturity test
Read more about assessment criteria at the University of Oulu webpage.
Grading:
Pass/Fail
Person responsible:
Supervisor of thesis
Working life cooperation:
-

Optional studies (min 5 ECTS credits)

H325035: Optional intermediate studies in mathematics, 0 - 180 op
Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Study module
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Electives

800329A: Topology, 8 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Mahmoud Filali
Opintokohteen oppimateriaali:
Vala K., Suominen K., 1990
Opintokohteen kielet: Finnish

ECTS Credits:
8 cr

Language of instruction:
English (also Finnish)

Timing:
Second year or later. Fall/spring term

Learning outcomes:
On successful completion of this course, the student will be able to follow more advanced topology and analysis.

Contents:
The course presents the very basics of topology that mathematics students should know. It starts with elementary set theory, then it goes on covering metric spaces including Baire's theorem; topological spaces and convergence in topological spaces; separation axioms including Urysohn's lemma and Tietze extension theorem; compact spaces including Tychonoff theorem; and ends with connected spaces.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56 hours lecture, 28 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics.

Recommended optional programme components:

Recommended or required reading:
S. Willard: General Topology;
K. Suominen & K. Vala: Topologia;

Assessment methods and criteria:
Final exam, or mid-term exams
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5
802362A: Introduction to computational inverse problems, 5 op

- Voimassaolo: 01.08.2010 -
- Opiskelumuoto: Intermediate Studies
- Laji: Course
- Vastuuysikkö: Field of Mathematics
- Arvostelu: 1 - 5, pass, fail
- Opettajat: Mikko Orispää
- Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802328A: Basics in Number Theory, 5 op

- Voimassaolo: 01.06.2011 -
- Opiskelumuoto: Intermediate Studies
- Laji: Course
- Vastuuysikkö: Field of Mathematics
- Arvostelu: 1 - 5, pass, fail
- Opettajat: Tapani Matala-aho
- Opintokohteen oppimateriaali:
  - Hardy, G. H., 1979
  - Rosen, Kenneth H., 1993
- Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Language of instruction:
Finnish/English

Timing:
2.-3. year of studies. Timing varies.

Learning outcomes:
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

Contents:
In our lectures we consider arithmetical properties of the common numbers involved in studing mathematics and in particular number theory. Also the methods will get a special interest. Examples of the numbers under the research will be binomials, continued fractions, sums of powers and some numbers sharing a name with the mathematicians Bernoulli, Euler, Fermat, Fibonacci, Heron, Lucas, Mersenne, Neper, Pythagoras, Stirling, Wilson and Wolstenholme. From the tools we mention congruences of rational numbers and polynomials, difference operators, generating series, irrationality considerations, matrix presentations, recurrences and telescopes.

Mode of delivery:
Face-to-face teaching

**Learning activities and teaching methods:**
36h lectures, 18h exercises

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
802354A Lukuteoria ja ryhmät,
802355A Rings, fields and polynomials
802118P Linear algebra I
802119P Linear algebra II
802352A Euclidean topology
802353A Series and integrals

**Recommended optional programme components:**
-

**Recommended or required reading:**
Lecture notes,
G.H. Hardy ja E.M. Wright: An Introduction to the Theory of Numbers;
Kenneth H. Rosen: Elementary number theory and its applications.

**Assessment methods and criteria:**
Mid-term exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Tapani Matala-aho

**Working life cooperation:**
-

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**802331A: Principles to Mathematical Modelling, 8 op**

**Voimassaolo:** 01.08.2009 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

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**802360A: Introduction to inverse problems, 4 op**

**Voimassaolo:** 01.08.2010 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Sari Lasanen
**Opintokohteen kielet:** Finnish

**ECTS Credits:**
4 cr
Language of instruction:
Finnish. Alternatively, a book examination in English.

Learning outcomes:
Upon completion, the student will be able to
- recognise several inverse problems
- describe typical properties of inverse problems
- solve simple inverse problems with accurate and inaccurate data

Contents:
1. Examples of inverse problems and their typical properties
2. Well-posed and ill-posed problems
3. Least squares solutions
4. Tikhonov regularization
5. Statistical inverse problems

Learning activities and teaching methods:
Lectures 4x45 min/week. Exercises 2x45 min/week.

Target group:
Suitable for major and minor students.

Prerequisites and co-requisites:
- 802118P Linear Algebra I
- 802119P Linear Algebra II
Also recommended:
- 800322A Multidimensional Analysis (or Analysis II)
- 801396A Introduction to Probability Theory II
- 802352A Euclidian Topology
- 800345A Differential Equations I

Assessment methods and criteria:
Exam.
Read more about assessment criteria at the University of Oulu webpage.

Other information:
This course does not contain numerical programming tasks. Computer-aided computations are contained in a separate course 802362A Introduction to Computational Inverse Problems.

801396A: Introduction to Probability Theory II, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Tuominen, P., 1993
Opintokohteen kielet: Finnish

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
2. year, Fall semester

Learning outcomes:
On successful completion of this course, the student will be able to
- understand probability theory deeper than before
- apply various stochastic models
- derive the basic results associated with the new concepts introduced
Contents:
The course is a direct continuation for the course Probability Theory I. The new concepts include for instance the moments of a distribution, the probability generating function, the Law of Large Numbers, the Central Limit Theorem as well as two-dimensional distributions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
24h lectures, 12h exercises

Target group:
Major- and minor students. Recommended for students aiming to Master's degree with major in statistics or major in mathematics and computer sciences.

Prerequisites and co-requisites:
801195P Introduction to probaility I
802352A Euclidean topology
802353A Series and integrals

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Kenneth Nordström.

801346A: Introduction to Cryptography, 4 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen kielet: Finnish
Leikkaavuudet:

802336A Introduction to Cryptography 5.0 op

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
2. year or later, Fall term (1. or 2. period)

Learning outcomes:
After completeing the course, student
- knows the principles of some traditianl symmetric key methods
- knows how public key methods (RSA, discrete logarithm, knapsack) work
- is familiar with the possibility to use and apply number theory in cryptography

Contents:
The course considers some traditianl symmetric key methods (affine system, matrix cryptography) and three public key methods, namely RSA, discrete logarithm and knapsack.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
27 h lectures, 15 h exercises

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
Compulsory basic and intermediate studies in mathematics.

**Recommended or required reading:**
Lecture notes

**Assessment methods and criteria:**
Final exam
Read more about assessment criteria at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Tapani Matala-aho

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**802364A: Introduction to Mathematical Software, 6 op**

**Voimassaolo:** 01.08.2010 -
**Opiskeluupuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Mikko Orispää
**Opintokohteen kielet:** Finnish

**ECTS Credits:**
6 cr

**Language of instruction:**
Lecturing language is Finnish, but the main points can be explained also in English if necessary. The software and the majority of course material is also in English.

**Timing:**
Autumn semester, period one.

**Learning outcomes:**
Upon completion of the course, the student
- knows the basics of the use of the most common mathematical software
- is able to use mathematical software in solving mathematical tasks and problems
- is able to independently deepen her knowledge of different mathematical software as necessary.

**Contents:**
During the course, the student learns the basics of some of commonly used mathematical software which include
- R
- Matlab
- Mathematica

Time permitting, it is also possible to learn other mathematical software depending the interests of the students.

**Mode of delivery:**
The course is arranged in a computer class as a series of lectures and rehearsals. On the lectures, the students have the possibility to use and try the mathematical software during the lectures. In the rehearsals, different given problems and tasks are solved together.

**Learning activities and teaching methods:**
Lectures 22h / Rehearsals 22h / Self-study 60h. The self-study contains the independent learning of the software and also the preparation of the final assignments.
**Target group:**
Anybody interested in mathematical software.

**Prerequisites and co-requisites:**
The required prerequisite is the completion of following courses (or corresponding knowledge of the subject):
- 802118P Linear Algebra I
- 802119P Linear Algebra II.

**Recommended optional programme components:**
The course is an independent entity and does not require additional studies carried out at the same time.

**Recommended or required reading:**
The required and recommended reading consists mainly on free material (manuals/tutorial) found in the internet. More information will be given at the beginning of the course.

**Assessment methods and criteria:**
The course is assessed by final assignments. The student who wish to complete the course at A-level will make two separate assignments of given topics using (at least) two different mathematical software. Those who wish to complete the course in S-level will need to discuss with the lecturer about the extra work needed to pass. For example, it could be possible to do assignments of wider topics, making an assignment(s) with a software not covered in the course, or making an assignment that requires particular skills and knowledge.
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
The course utilizes verbal grading scale “Pass/ fail”.

**Person responsible:**
Mikko Orispää

**Working life cooperation:**

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**802322A: Basics in mathematical modelling, 5 op**

- **Opiskelumuoto:** Intermediate Studies
- **Laji:** Course
- **Vastuuysikkö:** Field of Mathematics
- **Arvostelu:** 1 - 5, pass, fail
- **Opettajat:** Erkki Laitinen
- **Opintokohteen kielet:** Finnish

**801329A: Mathematics in Teaching, 3 op**

- **Voimassaolo:** 01.06.2015 -
- **Opiskelumuoto:** Intermediate Studies
- **Laji:** Course
- **Vastuuysikkö:** Field of Mathematics
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen kielet:** Finnish
- **Leikkaavuudet:**
  - 800146P Introduction to teaching 5.0 op

**ECTS Credits:**
3 cr/ 81 hours of work

**Language of instruction:**
Finnish
Timing:
1st year, periods 3 and 4

Learning outcomes:
The student can reflect critically on the learning and teaching of mathematics. The student can analyze the connection between mathematics at school and at university.

Contents:
Learning and teaching mathematics are thought about and discussed. The course consists of reflective exercises and seminar meetings where the exercises are discussed. A student analyzes the connection between mathematics at school and at university. A student writes a learning journal.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
24 h seminar meetings, 57 h self-study and group work.

Target group:
Mathematics teacher students

Prerequisites and co-requisites:
-

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Active participation, learning journal, group work

Grading:
Pass/Fail

Person responsible:
Riikka Palkki

Working life cooperation:
-

Other information:
-

800104P: Number Systems, 4 op

Voimassaolo: 01.03.2011 -
Opiskelumuoto: Basic Studies
Lajj: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
  800347A Number systems 5.0 op

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
Autumn semester, period I. Recommended to complete the course at the first or second autumn semester.
Learning outcomes:
Having completed the course, the student is able to
- define and construct the most common number systems
- list and use the basic arithmetic operations in number systems

Contents:
The course considers the basics of arithmetic and algebra in the setting of the most common
number systems (natural numbers, integers, rationals and reals). The course begins with the
construction of natural numbers and continues, through integers and rational numbers, to the
construction of real numbers.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 28 h, exercises 14 h, self-study 66 h

Target group:
Major and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction

Recommended optional programme components:
For first year students, recommended to be completed simultaneously with the course "802155P
Continuity and Limit".

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam

Grading:
1-5, fail

Person responsible:
Jukka Kauppi

Working life cooperation:
-

031076P: Differential Equations, 5 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Applied Mathematics and Computational Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
ay031076P Differential Equations (OPEN UNI) 5.0 op
800320A Differential equations 5.0 op
031017P Differential Equations 4.0 op

Ei opintojaksokuvauksia.

806112P: Basic Methods of Data Analysis, 10 op

Opiskelumuoto: Basic Studies
Introduction to Regression and Analysis of Variance

**ECTS Credits:**
10 cr

**Language of instruction:**
Finnish

**Timing:**
The course is held in the autumn semester, during periods 1 and 2.

**Learning outcomes:**
On successful completion of this course, the student will be able to
- analyze continuous and categorical response in the most common experimental and observational studies
- critically evaluate chosen model
- use some statistical software

**Contents:**
Skills for performing statistical analyses and inferences on the basis of data obtained in common experimental and observational studies are expanded and deepened. Topics included are e.g. (1) principles of collection, description, and modelling of, and inference on statistical data; (2) basic methods of analysing continuous outcome variables, like comparison of groups, analysis of variance, regression analysis, residuals and model diagnostics, nonparametric methods, treatment of correlated and lifetime (censored) observations; (3) and basic methods of analysing binary, categorical and count data.

**Mode of delivery:**
Face-to-face teaching.

**Learning activities and teaching methods:**
56h lectures, 42h exercises, self-study.

**Target group:**
Major and minor students.

**Prerequisites and co-requisites:**
For major students:
801195P Introduction to Probability Theory I, 806113P Introduction to statistics, 802118P Linear algebra I,
802154P Elementary functions, 802155P Limits and continuity, 802156P Derivative
For minor students: 806109P Basic Methods in Statistics I

**Recommended optional programme components:**
To be completed before 805310A Statistical inference I, 806359A Regression modelling and other studies in statistics.

**Recommended or required reading:**
Lecture notes.

**Assessment methods and criteria:**
Intermediate (2) or final exam.
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
The course utilizes a numerical grading scale 1-5 / fail.

**Person responsible:**
Jari Päkkilä

**Working life cooperation:**
-

H326635: Optional intermediate studies in statistics, 0 - 180 op

*Voimassaolo:* 01.08.2010 -
*Opiskelumuoto:* Intermediate Studies
*Laji:* Study module
*Vastuuysikkö:* Field of Mathematics
*Arvostelu:* 1 - 5, pass, fail

*Opintokohteen kielet:* Finnish

Ei opintojaksokuvauksia.

**Electives**

805324A: Time series analysis, 5 op

*Opiskelumuoto:* Intermediate Studies
*Laji:* Course
*Vastuuysikkö:* Field of Mathematics
*Arvostelu:* 1 - 5, pass, fail
*Opettajat:* Jussi Klemelä

*Opintokohteen oppimateriaali:*
Harvey, Andrew C., , 1993
Lütkepohl, Helmut , , 1991
Hamilton, James D., , 1994

*Opintokohteen kielet:* Finnish

**ECTS Credits:**
5 cr

**Language of instruction:**
Finnish

**Learning outcomes:**
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply statistical software to fit time series models.

**Contents:**
1. The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram.
2. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models.
3. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH).
4. Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
Besides lectures, there are voluntary exercises.
There are 14 times 2 hour lectures and 7 times 2 hour exercises.

**Target group:**
Students of mathematical sciences, econometrics and finance students.

**Prerequisites and co-requisites:**
Basic probability theory.

**Recommended optional programme components:**
-

**Recommended or required reading:**

**Assessment methods and criteria:**
Examination
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1 - 5

**Person responsible:**
Jussi Klemelä

**Working life cooperation:**
-

**Other information:**
Home page of the course is [http://cc.oulu.fi/~jklemela/timeseries/](http://cc.oulu.fi/~jklemela/timeseries/)
Recommended reading:

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805308A: Analysis of longitudinal data, 5 op

**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen oppimateriaali:**
Peter J. Diggle et al., 2002
Hsiao, Cheng, 2003
McCulloch, Charles E., 2001
Fitzmaurice, Garrett M., 2004

**Opintokohteen kielet:** Finnish

**ECTS Credits:**
5/6 cr

**Language of instruction:**
Finnish

**Timing:**
Every second year.

**Learning outcomes:**
After finishing the course a student can apply pooled ordinary least squares, generalized least squares, random effects methods, and fixed effects methods.

**Contents:**
1. Introduction: data types, omitted variables.
2. Mathematical tools: conditional expectation, basic asymptotic theory.
4. Estimating systems of equations by ordinary least squares and by generalized least squares, panel data and seemingly unrelated regression as examples, simultaneous exogeneity and strict exogeneity, consistency and asymptotic normality, homoskedasticity and heteroskedasticity.
5. Pooled ordinary least squares for panel data, aggregated time effect, dummy variables, testing serial correlation and heteroskedasticity.
6. Unobserved effects model: random effects and fixed effects.
7. Random effects methods: random effects structure of the covariance matrix.
8. Fixed effects methods: fixed effects transformation, the use of dummy variables, first differencing transformation.
9. Comparison of estimators.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises. There are 14 times 2 hour lectures and 7 times 2 hour exercises.

Target group:
Students of economics and mathematical sciences.

Prerequisites and co-requisites:
Basic Mathematics for Economics 1 and 2, Basic Methods in Statistics 1, Introduction to Econometrics.

Recommended or required reading:

Assessment methods and criteria:
Examination
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1 - 5

Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
The course is organized every two years.
The home page of the course is http://cc.oulu.fi/~jklemela/panel/

805349A: Likelihood Inference, 5 op

Voimassaalo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
805310A Statistical Inference I 10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd or 3rd year of B.Sc. studies, spring term
Learning outcomes:
After successful completion of the course the student can describe the basic principles of likelihood inference, derive likelihood functions of models with few parameters, compute likelihood quantities based on them, and interpret results such obtained.

Contents:
Statistical model and observation data; likelihood function, log-likelihood, score, information; maximum likelihood estimation, relative likelihood, likelihood interval and likelihood region, profile likelihood; normal approximation of log-likelihood; use of R environment in inferential problems.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h), and independent work

Target group:
Students having statistics as the major or a minor subject

Prerequisites and co-requisites:
Introduction to Probability Theory I, Basic Methods of Data Analysis

Recommended optional programme components:
Is needed in nearly all intermediate and advanced courses in statistics

Recommended or required reading:

Assessment methods and criteria:
Final exam. Read more about assessment criteria at the University of Oulu webpage.

Grading:
Fail, 1-5

Person responsible:
Esa Läärä

Working life cooperation:
No

Other information:
-

805350A: Estimation and Test Theory, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish
Leikkaavuudet:
    805310A  Statistical Inference I  10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish
Timing:
2nd or 3rd year during B.Sc. studies

Learning outcomes:
After successful completion of the course the student can describe the basic principles of frequentist and bayesian statistical inference, compute point and interval estimates, test statistics and P-values based on likelihood function of models with few parameters, and interpret results thus obtained.

Contents:
Statistical model and observational data; construction and properties of point estimators and confidence intervals; likelihood ratio, score and Wald test statistics and their asymptotic sampling distribution; jackknife and bootstrap methods; elements of bayesian inference; use of R environment in inferential problems.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h), and independent work

Target group:
Students having statistics as the major or a minor subject

Prerequisites and co-requisites:
Likelihood inference, Introduction to probability theory I, Basic Methods of Data Analysis

Recommended optional programme components:
Needed in nearly all intermediate and advanced courses of statistics

Recommended or required reading:

Assessment methods and criteria:
Final Exam. Read more about assessment criteria at the University of Oulu webpage

Grading:
Fail, 1-5

Person responsible:
Esa Läärä

Working life cooperation:
No

Other information:
-

805351A: Linear Regression, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish
Leikkaavuudet:
806359A Regression modelling 10.0 op

ECTS Credits:
5 ECTS credits  

**Language of instruction:**  
Finnish  

**Timing:**  
2nd or 3rd year during B.Sc. studies  

**Learning outcomes:**  
After successful completion of the course the student can describe basic concepts and assumptions in linear models for continuous outcome variables as well as main principles of regression modelling, and can also apply these methods in analysis of experimental and non-experimental observation data.  

**Contents:**  
Linear regression models for a continuous outcome variable; formulation of the model, selection of variables and interpretation of parameters; fitting the models, estimation of parameters and prediction using method of least squares; model criticism and diagnostics; use of R environment and SAS software in modelling.  

**Mode of delivery:**  
Face-to-face teaching  

**Learning activities and teaching methods:**  
Lectures (28 h), practicals and computer classes (14 h) and independent work.  

**Target group:**  
Students having statistics as the major or a minor subject.  

**Prerequisites and co-requisites:**  
Basic Methods of Data Analysis; Core courses in the B.Sc curriculum of mathematical sciences.  

**Recommended optional programme components:**  
Prerequisite to the course Generalized Linear Models  

**Recommended or required reading:**  

**Assessment methods and criteria:**  
Active participation in practicals and final exam. Read more about assessment criteria at the University of Oulu webpage  

**Grading:**  
Fail, 1-5  

**Person responsible:**  
Esa Läärä  

**Working life cooperation:**  
No  

**Other information:**  
-  

**805352A: Generalized Linear Models, 5 op**  

Voimassaolo: 01.06.2015 -  
Opiskelumuoto: Intermediate Studies  
Laji: Course  
Vastuuysikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Mikko Sillanpää  
Opintokohteen kielet: Finnish  
Leikkaavuudet:  

805630S Generalized Linear Models 5.0 op
Regression modelling 10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd or 3rd year of studies in B.Sc. programme

Learning outcomes:
After successful completion of the course the student can describe the basic concepts and assumptions of generalized linear models as well as main principles of regression modelling, and can also apply these methods in analysis of experimental and observational data.

Contents:
Generalized linear regression models for continuous, binary and count outcomes; formulation of the model, selection of variables and interpretation of parameters; fitting the models, estimating the parameters and prediction by the method of maximum likelihood; model criticism and diagnostics; use of R environment and SAS software in modelling.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h)

Target group:
Students having statistics as the major or a minor subject

Prerequisites and co-requisites:
Linear regression; Basic methods in data-analysis

Recommended optional programme components:
-

Recommended or required reading:

Assessment methods and criteria:
Active participation in practicals and final exam. Read more about assessment criteria at the University of Oulu webpage

Grading:
Fail, 1-5

Person responsible:
Mikko Sillanpää

Working life cooperation:
No

Other information:
-

805353A: Statistical Software, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
805340A Statistical Software 4.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
3. year studies. Fall semester. Timing varies.

Learning outcomes:
After successful completion of the course the student can use independently major statistical software needed in data analysis.

Contents:
The course covers R, SAS and IBM SPSS, and their most important tools for data management, statistical computation, graphics and programming will be introduced and proficiency for their fluent use is acquired.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h lectures, exercises and tutoring. 88 h learning tasks and self-study.

Target group:
Major and minor students

Prerequisites and co-requisites:
806112P Basic methods of data-analysis

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Home works

Grading:
Numerical grading 1-5 (or fail)

Person responsible:
Hanna Heikkinen

Working life cooperation:
No

801396A: Introduction to Probability Theory II, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Tuominen, P., , 1993
Opintokohteen kielet: Finnish

ECTS Credits:
4 cr
Language of instruction:
Finnish

Timing:
2. year, Fall semester

Learning outcomes:
On successful completion of this course, the student will be able to
- understand probability theory deeper than before
- apply various stochastic models
- derive the basic results associated with the new concepts introduced

Contents:
The course is a direct continuation for the course Probability Theory I. The new concepts include for instance the moments of a distribution, the probability generating function, the Law of Large Numbers, the Central Limit Theorem as well as two-dimensional distributions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
24h lectures, 12h exercises

Target group:
Major- and minor students. Recommended for students aiming to Master's degree with major in statistics or major in mathematics and computer sciences.

Prerequisites and co-requisites:
801195P Introduction to probability I
802352A Euclidean topology
802353A Series and integrals

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Kenneth Nordström.

H325051: Mathematics orientation module, 0 - 100 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Basic and Intermediate Studies
Laji: Study module
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Compulsory

802335A: Introduction to Real Analysis, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
1st year, 4th period

Learning outcomes:
After completing the course the student is able to
- apply the definition of limit in several different settings
- apply Cauchy criterion
- solve problems related to the topology of the real line
- explain the difference between uniform and pointwise convergence

Contents:
The aim of the course is to deepen the understanding of limits, convergence and approximation. Convergence on the real line and related results are considered in detail. The students understanding of continuity is deepened. Cauchy sequences and completeness form one of the central topics. Finally, function sequences and series are studied as well as uniform and pointwise convergence.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises, 91h independent study

Target group:
Mathematics majors (obligatory for mathematics majors except for subject teacher students)

Prerequisites and co-requisites:
802162P Continuity and Limit
802163P Derivative

Assessment methods and criteria:
Final exam

Grading:
Fail, 1-5

Person responsible:
Pekka Salmi

Working life cooperation:
No

Other information:

802351A: Vector Calculus, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Leikkaavuudet:

<table>
<thead>
<tr>
<th>Course Code</th>
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<td>800328A</td>
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<td>5.0 op</td>
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<td>Analysis II</td>
<td>8.0 op</td>
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**ECTS Credits:**
5 ECTS credits

**Language of instruction:**
Finnish

**Timing:**
1st or 2nd year, 3rd period

**Learning outcomes:**
After completing the course the student is able to - operate functions of several variables - apply derivates of functions of several variables - calculate multiple integrals

**Contents:**
The course concerns calculus of severable variables. The central concepts of the course are partial derivative, gradient, divergence, curl and multiple integral. Integral theorems related to functions of several variables are also presented. The course offers basic tools for further courses in analysis as well as for applications.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
28h lectures, 14h exercises, 91h study a part of which may be guided

**Target group:**
Mathematics major and minor students

**Prerequisites and co-requisites:**
802161P Introduction to Real Functions
802120P Introduction to Matrices

**Recommended optional programme components:**
-

**Recommended or required reading:**
-

**Assessment methods and criteria:**
Final exam

**Grading:**
1-5, fail

**Person responsible:**
Mahmoud Filali

**Working life cooperation:**
No

**Other information:**
-

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802358A: Metric Spaces, 5 op

**Voimassaolo:** 01.06.2015 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
802356A Metric Topology 5.0 op
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd year, 2nd period

Learning outcomes:
After the course the student is able to
- define metric spaces
- give examples of metric spaces
- define elementary topological concepts (open and closed sets, accumulation point, etc)
- apply the definitions from elementary topology in examples and proofs

Contents:
The goal of the courses is to expand student's knowledge and understanding of continuity and to introduce other topological concepts in the setting of metric spaces. Course considers basic topology of n-dimensional Euclidean space and introduces also other metric spaces as examples. Central concepts are open and closed sets, compactness and completeness.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises, 91h independent study

Target group:
Mathematics majors (obligatory for mathematics majors except for subject teacher students)

Prerequisites and co-requisites:
802357A Introduction to Real Analysis

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Final exam
Grading:
Fail, 1-5

Person responsible:
Pekka Salmi

Working life cooperation:
No

Other information:
-

801323A: Seminar, 6 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
800331A Proseminar 10.0 op

ECTS Credits:
6 cr
Language of instruction:
Finnish (also English)

Timing:
2.-3. year of studies

Learning outcomes:
After completing the Bachelor's thesis, student
- is able to form a clear and logical
- is able to concentrate to important and essential details in the subject of thesis
- gain experience presenting mathematical concept and research studies.

Contents:
Proseminar (Bachelor's thesis) is a small mathematical study based on literature. Student is familiarized to write mathematical texts and obtain information using literature. Thesis includes a oral presentation from the subject of the thesis.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Seminars and own work

Target group:
Major students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies.

Recommended optional programme components:
Maturity test is written from the topic of Bachelor's thesis.

Recommended or required reading:
-

Assessment methods and criteria:
Opinnäytetyö
Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Maarit Järvenpää

Working life cooperation:
-

800300A: Maturity test, 0 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
0 cr

Language of instruction:
Finnish/Swedish

Timing:
Third year

Learning outcomes:
Maturity test

Contents:
Students must take a written maturity test to demonstrate their language skills and how well they know the topic of their thesis. The maturity test is taken in the language in which the student has received his or her education in Finland. If the student has received his or her education in a language other than Finnish or Swedish, the degree programme determines the language of the maturity test. In such cases only the contents of the maturity test is evaluated, not the language.

Mode of delivery:
Maturity test written in examination room.

Learning activities and teaching methods:
Maturity test

Target group:
Major students

Prerequisites and co-requisites:
Bachelor's degree (or similar)

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Maturity test
Read more about [assessment criteria](#) at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Supervisor of thesis

Working life cooperation:
-

Electives

**H325035: Optional intermediate studies in mathematics, 0 - 180 op**

Voimassaolo: 01.08.2010 -  
Opiskelumuoto: Intermediate Studies  
Laji: Study module  
Vastuuysikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

**Electives**

**800329A: Topology, 8 op**

Opiskelumuoto: Intermediate Studies  
Laji: Course  
Vastuuysikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Mahmoud Filali  
Opintokohteen oppimateriaali:
Vala K., Suominen K., 1990
Opintokohteen kielet: Finnish

ECTS Credits:
8 cr

Language of instruction:
English (also Finnish)

Timing:
Second year or later. Fall/spring term

Learning outcomes:
On successful completion of this course, the student will be able to follow more advanced topology and analysis.

Contents:
The course presents the very basics of topology that mathematics students should know. It starts with elementary set theory, then it goes on covering metric spaces including Baire's theorem; topological spaces and convergence in topological spaces; separation axioms including Urysohn's lemma and Tietze extension theorem; compact spaces including Tychonoff theorem; and ends with connected spaces.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
56 hours lecture, 28 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics.

Recommended optional programme components:
-

Recommended or required reading:
S. Willard: General Topology;
K. Suominen & K. Vala: Topologia;

Assessment methods and criteria:
Final exam, or mid-term exams
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mahmoud Filali

Working life cooperation:
-

802362A: Introduction to computational inverse problems, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikko Orispää
**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

**802328A: Basics in Number Theory, 5 op**

**Voimassaolo:** 01.06.2011 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Tapani Matala-aho

**Opintokohteen oppimateriaali:**
- Hardy, G. H., , 1979
- Rosen, Kenneth H., , 1993

**ECTS Credits:**
5 cr

**Language of instruction:**
Finnish/English

**Timing:**
2.-3. year of studies. Timing varies.

**Learning outcomes:**
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

**Contents:**
In our lectures we consider arithmetical properties of the common numbers involved in studing mathematics and in particular number theory. Also the methods will get a special interest. Examples of the numbers under the research will be binomials, continued fractions, sums of powers and some numbers sharing a name with the mathematicians Bernoulli, Euler, Fermat, Fibonacci, Heron, Lucas, Mersenne, Neper, Pythagoras, Stirling, Wilson and Wolstenholme. From the tools we mention congruences of rational numbers and polynomials, difference operators, generating series, irrationality considerations, matrix presentations, recurrences and telescopes.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
36h lectures, 18h exercises

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
- 802354A Lukuteoria ja ryhmät,
- 802355A Rings, fields and polynomials
- 802118P Linear algebra I
- 802119P Linear algebra II
- 802352A Euclidean topology
- 802353A Series and integrals
Recommended optional programme components:

Recommended or required reading:
Lecture notes,
G.H. Hardy ja E.M. Wright: An Introduction to the Theory of Numbers;
Kenneth H. Rosen: Elementary number theory and its applications.

Assessment methods and criteria:
Mid-term exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Tapani Matala-aho

Working life cooperation:

802331A: Principles to Mathematical Modelling, 8 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802360A: Introduction to inverse problems, 4 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Sari Lasanen
Opintokohteen kielet: Finnish

ECTS Credits:
4 cr

Language of instruction:
Finnish. Alternatively, a book examination in English.

Learning outcomes:
Upon completion, the student will be able to
- recognise several inverse problems
- describe typical properties of inverse problems
- solve simple inverse problems with accurate and inaccurate data

Contents:
1. Examples of inverse problems and their typical properties
2. Well-posed and ill-posed problems
3. Least squares solutions
4. Tikhonov regularization
5. Statistical inverse problems
Learning activities and teaching methods:
Lectures 4x45 min / week. Exercises 2x45 min /week.

Target group:
Suitable for major and minor students.

Prerequisites and co-requisites:
- 802118P Linear Algebra I
- 802119P Linear Algebra II
Also recommended:
- 800322A Multidimensional Analysis (or Analysis II)
- 801396A Introduction to Probability Theory II
- 802352A Euclidian Topology
- 800345A Differential Equations I

Assessment methods and criteria:
Exam.
Read more about assessment criteria at the University of Oulu webpage.

Other information:
This course does not contain numerical programming tasks. Computer-aided computations are contained in a separate course 802362A Introduction to Computational Inverse Problems.

801396A: Introduction to Probability Theory II, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Tuominen, P., 1993
Opintokohteen kielet: Finnish

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
2. year, Fall semester

Learning outcomes:
On successful completion of this course, the student will be able to
- understand probability theory deeper than before
- apply various stochastic models
- derive the basic results associated with the new concepts introduced

Contents:
The course is a direct continuation for the course Probability Theory I. The new concepts include for instance the moments of a distribution, the probability generating function, the Law of Large Numbers, the Central Limit Theorem as well as two-dimensional distributions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
24h lectures, 12h exercises

Target group:
Major- and minor students. Recommended for students aiming to Master's degree with major in statistics or major in mathematics and computer sciences.
**Prerequisites and co-requisites:**
- 801195P Introduction to probability I
- 802352A Euclidean topology
- 802353A Series and integrals

**Assessment methods and criteria:**
- Final exam
- Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
- 1-5

**Person responsible:**
- Kenneth Nordström.

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**801346A: Introduction to Cryptography, 4 op**

**Opiskelumuoto:** Intermediate Studies

**Laji:** Course

**Vastuuysikkö:** Field of Mathematics

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Tapani Matala-aho

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**

<table>
<thead>
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<th>Code</th>
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<tbody>
<tr>
<td>802336A</td>
<td>Introduction to Cryptography</td>
<td>5.0 op</td>
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**ECTS Credits:**
- 4 cr

**Language of instruction:**
- Finnish

**Timing:**
- 2. year or later, Fall term (1. or 2. period)

**Learning outcomes:**
- After completing the course, student
  - knows the principles of some traditional symmetric key methods
  - knows how public key methods (RSA, discrete logarithm, knapsack) work
  - is familiar with the possibility to use and apply number theory in cryptography

**Contents:**
- The course considers some traditional symmetric key methods (affine system, matrix cryptography) and three public key methods, namely RSA, discrete logarithm and knapsack.

**Mode of delivery:**
- Face-to-face teaching

**Learning activities and teaching methods:**
- 27 h lectures, 15 h exercises

**Target group:**
- Major and minor students

**Prerequisites and co-requisites:**
- Compulsory basic and intermediate studies in mathematics.

**Recommended or required reading:**
- Lecture notes

**Assessment methods and criteria:**
- Final exam
- Read more about [assessment criteria](#) at the University of Oulu webpage.
Grading:
1-5

Person responsible:
Tapani Matala-aho

802364A: Introduction to Mathematical Software, 6 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikko Orispää
Opintokohteen kielet: Finnish

ECTS Credits:
6 cr

Language of instruction:
Lecturing language is Finnish, but the main points can be explained also in English if necessary. The software and the majority of course material is also in English.

Timing:
Autumn semester, period one.

Learning outcomes:
Upon completion of the course, the student
- knows the basics of the use of the most common mathematical software
- is able to use mathematical software in solving mathematical tasks and problems
- is able to independently deepen her knowledge of different mathematical software as necessary.

Contents:
During the course, the student learns the basics of some of commonly used mathematical software which include
- R
- Matlab
- Mathematica
Time permitting, it is also possible to learn other mathematical software depending the interests of the students.

Mode of delivery:
The course is arranged in a computer class as a series of lectures and rehearsals. On the lectures, the students have the possibility to use and try the mathematical software during the lectures. In the rehearsals, different given problems and tasks are solved together.

Learning activities and teaching methods:
Lectures 22h / Rehearsals 22h / Self-study 60h. The self-study contains the independent learning of the software and also the preparation of the final assignments.

Target group:
Anybody interested in mathematical software.

Prerequisites and co-requisites:
The required prerequisite is the completion of following courses (or corresponding knowledge of the subject):
- 802118P Linear Algebra I
- 802119P Linear Algebra II.

Recommended optional programme components:
The course is an independent entity and does not require additional studies carried out at the same time.

Recommended or required reading:
The required and recommended reading consists mainly on free material (manuals/tutorial) found in the internet. More information will be given at the beginning of the course.

**Assessment methods and criteria:**
The course is assessed by final assignments. The student who wish to complete the course at A-level will make two separate assignments of given topics using (at least) two different mathematical software. Those who wish to complete the course in S-level will need to discuss with the lecturer about the extra work needed to pass. For example, it could be possible to do assignments of wider topics, making an assignment(s) with a software not covered in the course, or making an assignment that requires particular skills and knowledge. Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
The course utilizes verbal grading scale “Pass/ fail”.

**Person responsible:**
Mikko Orispää

**Working life cooperation:**
-

**802322A: Basics in mathematical modelling, 5 op**

- **Opiskelumuoto:** Intermediate Studies
- **Laji:** Course
- **Vastuuyksikkö:** Field of Mathematics
- **Arvostelu:** 1 - 5, pass, fail
- **Opettajat:** Erkki Laitinen
- **Opintokohteen kielet:** Finnish

**801329A: Mathematics in Teaching, 3 op**

- **Voimassaolo:** 01.06.2015 -
- **Opiskelumuoto:** Intermediate Studies
- **Laji:** Course
- **Vastuuyksikkö:** Field of Mathematics
- **Arvostelu:** 1 - 5, pass, fail
- **Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
800146P  Introduction to teaching  5.0 op

**ECTS Credits:**
3 cr/ 81 hours of work

**Language of instruction:**
Finnish

**Timing:**
1st year, periods 3 and 4

**Learning outcomes:**
The student can reflect critically on the learning and teaching of mathematics. The student can analyze the connection between mathematics at school and at university.

**Contents:**
Learning and teaching mathematics are thought about and discussed. The course consists of reflective exercises and seminar meetings where the exercises are discussed. A student analyzes the connection between mathematics at school and at university. A student writes a learning journal.

**Mode of delivery:**
Face-to-face teaching
Learning activities and teaching methods:
24 h seminar meetings, 57 h self-study and group work.

Target group:
Mathematics teacher students

Prerequisites and co-requisites:
-

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Active participation, learning journal, group work

Grading:
Pass/Fail

Person responsible:
Riikka Palkki

Working life cooperation:
-

Other information:
-

800104P: Number Systems, 4 op

Voimassaolo: 01.03.2011 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
Autumn semester, period I. Recommended to complete the course at the first or second autumn semester.

Learning outcomes:
Having completed the course, the student is able to
- define and construct the most common number systems
- list and use the basic arithmetic operations in number systems

Contents:
The course considers the basics of arithmetic and algebra in the setting of the most common number systems (natural numbers, integers, rationals and reals). The course begins with the construction of natural numbers and continues, through integers and rational numbers, to the construction of real numbers.
Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 28 h, exercises 14 h, self-study 66 h

Target group:
Major and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction

Recommended optional programme components:
For first year students, recommended to be completed simultaneously with the course "802155P Continuity and Limit".

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam

Grading:
1-5, fail

Person responsible:
Jukka Kauppi

Working life cooperation:

031076P: Differential Equations, 5 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Applied Mathematics and Computational Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
ay031076P Differential Equations (OPEN UNI) 5.0 op
800320A Differential equations 5.0 op
031017P Differential Equations 4.0 op

Ei opintojaksokuvauksia.

806112P: Basic Methods of Data Analysis, 10 op

Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Jari Päkkilä
Opintokohteen oppimateriaali:
Armitage, P. , , 2002
Opintokohteen kielet: Finnish
Leikkaavuudet:
805305A Introduction to Regression and Analysis of Variance 5.0 op
ECTS Credits:
10 cr

Language of instruction:
Finnish

Timing:
The course is held in the autumn semester, during periods 1 and 2.

Learning outcomes:
On successful completion of this course, the student will be able to
- analyze continuous and categorial response in the most common experimental and observational studies
- critically evaluate chosen model
- use some statistical software

Contents:
Skills for performing statistical analyses and inferences on the basis of data obtained in common experimental and observational studies are expanded and deepened. Topics included are e.g. (1) principles of collection, description, and modelling of, and inference on statistical data; (2) basic methods of analysing continuous outcome variables, like comparison of groups, analysis of variance, regression analysis, residuals and model diagnostics, nonparametric methods, treatment of correlated and lifetime (censored) observations; (3) and basic methods of analysing binary, categorical and count data.

Mode of delivery:
Face-to-face teaching.

Learning activities and teaching methods:
56h lectures, 42h exercises, self-study.

Target group:
Major and minor students.

Prerequisites and co-requisites:
For major students:
801195P Introduction to Probability Theory I, 806113P Introduction to statistics, 802118P Linear algebra I,
802154P Elementary functions, 802155P Limits and continuity,
802156P Derivative
For minor students: 806109P Basic Methods in Statistics I

Recommended optional programme components:
To be completed before 805310A Statistical inference I, 806359A Regression modelling and other studies in statistics.

Recommended or required reading:
Lecture notes.

Assessment methods and criteria:
Intermediate (2) or final exam.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
The course utilizes a numerical grading scale 1-5 / fail.

Person responsible:
Jari Pääkkilä

Working life cooperation:
-

H326635: Optional intermediate studies in statistics, 0 - 180 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Electives

805324A: Time series analysis, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C., , 1993
Lütkepohl, Helmut, , 1991
Hamilton, James D., , 1994
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Language of instruction:
Finnish

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply statistical software to fit time series models.

Contents:
1. The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram.
2. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models.
3. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH).
4. Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises.
There are 14 times 2 hour lectures and 7 times 2 hour exercises.

Target group:
Students of mathematical sciences, econometrics and finance students.

Prerequisites and co-requisites:
Basic probability theory.

Recommended optional programme components:
-

Recommended or required reading:
Assessment methods and criteria:
Examination
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1 - 5

Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
Home page of the course is http://cc.oulu.fi/~jklemta/timeseries/
Recommended reading:

805308A: Analysis of longitudinal data, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Peter J. Diggle et al., , 2002
Hsiao, Cheng , , 2003
McCulloch, Charles E. , , 2001
Fitzmaurice, Garrett M. , , 2004
Opintokohteen kielet: Finnish

ECTS Credits:
5/6 cr

Language of instruction:
Finnish

Timing:
Every secon year.

Learning outcomes:
After finishing the course a student can apply pooled ordinary least squares, generalized least squares, random effects methods, and fixed effects methods.

Contents:
1. Introduction: data types, omitted variables.
2. Mathematical tools: conditional expectation, basic asymptotic theory.
4. Estimating systems of equations by ordinary least squares and by generalized least squares, panel data and seemingly unrelated regression as examples, simultaneous exogeneity and strict exogeneity, consistency and asymptotic normality, homoskedasticity and heteroskedasticity.
5. Pooled ordinary least squares for panel data, aggregated time effect, dummy variables, testing serial correlation and heteroskedasticity.
6. Unobserved effects model: random effects and fixed effects.
7. Random effects methods: random effects structure of the covariance matrix.
8. Fixed effects methods: fixed effects transformation, the use of dummy variables, first differencing transformation.
9. Comparison of estimators.

Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
Besides lectures, there are voluntary exercises. There are 14 times 2 hour lectures and 7 times 2 hour exercises.

Target group:
Students of economics and mathematical sciences.

Prerequisites and co-requisites:
Basic Mathematics for Economics 1 and 2, Basic Methods in Statistics 1, Introduction to Econometrics.

Recommended or required reading:

Assessment methods and criteria:
Examination
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1 - 5

Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
The course is organized every two years.
The home page of the course is http://cc.oulu.fi/~jkleme/panel/

805349A: Likelihood Inference, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
805310A Statistical Inference I 10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd or 3rd year of B.Sc. studies, spring term

Learning outcomes:
After successful completion of the course the student can describe the basic principles of likelihood inference, derive likelihood functions of models with few parameters, compute likelihood quantities based on them, and interpret results such obtained.

Contents:
Statistical model and observation data; likelihood function, log-likelihood, score, information; maximum likelihood estimation, relative likelihood, likelihood interval and likelihood region, profile likelihood; normal approximation of log-likelihood; use of R environment in inferential problems.

Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h), and independent work

Target group:
Students having statistics as the major or a minor subject

Prerequisites and co-requisites:
Introduction to Probability Theory I, Basic Methods of Data Analysis

Recommended optional programme components:
Is needed in nearly all intermediate and advanced courses in statistics

Recommended or required reading:

Assessment methods and criteria:
Final exam. Read more about assessment criteria at the University of Oulu webpage.

Grading:
Fail, 1-5

Person responsible:
Esa Läärä

Working life cooperation:
No

Other information:
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805350A: Estimation and Test Theory, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish
Leikkaavuudet:
   805310A  Statistical Inference I  10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd or 3rd year during B.Sc. studies

Learning outcomes:
After successful completion of the course the student can describe the basic principles of frequentist and bayesian statistical inference, compute point and interval estimates, test statistics and P-values based on likelihood function of models with few parameters, and interpret results thus obtained.

Contents:
Statistical model and observational data; construction and properties of point estimators and confidence intervals; likelihood ratio, score and Wald test statistics and their asymptotic sampling distribution; jackknife and bootstrap methods; elements of bayesian inference; use of R environment in inferential problems.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h), and independent work

Target group:
Students having statistics as the major or a minor subject

Prerequisites and co-requisites:
Likelihood inference, Introduction to probability theory I, Basic Methods of Data Analysis

Recommended optional programme components:
Needed in nearly all intermediate and advanced courses of statistics

Recommended or required reading:

Assessment methods and criteria:
Final Exam. Read more about assessment criteria at the University of Oulu webpage

Grading:
Fail, 1-5

Person responsible:
Esa Läärä

Working life cooperation:
No

Other information:

805351A: Linear Regression, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish
Leikkaavuudet:

806359A Regression modelling 10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd or 3rd year during B.Sc. studies

Learning outcomes:
After successful completion of the course the student can describe basic concepts and assumptions in linear models for continuous outcome variables as well as main principles of regression modelling, and can also apply these methods in analysis of experimental and non-experimental observation data.

Contents:
Linear regression models for a continuous outcome variable; formulation of the model, selection of variables and interpretation of parameters; fitting the models, estimation of parameters and prediction using method of least squares; model criticism and diagnostics; use of R environment and SAS software in modelling.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h) and independent work.

Target group:
Students having statistics as the major or a minor subject.

Prerequisites and co-requisites:
Basic Methods of Data Analysis; Core courses in the B.Sc curriculum of mathematical sciences.

Recommended optional programme components:
Prerequisite to the course Generalized Linear Models

Recommended or required reading:

Assessment methods and criteria:
Active participation in practicals and final exam. Read more about assessment criteria at the University of Oulu webpage

Grading:
Fail, 1-5

Person responsible:
Esa Läärää

Working life cooperation:
No

Other information:

805352A: Generalized Linear Models, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikko Sillanpää
Opintokohteen kielet: Finnish
Leikkaavuudet:

805630S Generalized Linear Models 5.0 op
806359A Regression modelling 10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
Learning outcomes:
After successful completion of the course the student can describe the basic concepts and assumptions of generalized linear models as well as main principles of regression modelling, and can also apply these methods in analysis of experimental and observational data.

Contents:
Generalized linear regression models for continuous, binary and count outcomes; formulation of the model, selection of variables and interpretation of parameters; fitting the models, estimating the parameters and prediction by the method of maximum likelihood; model criticism and diagnostics; use of R environment and SAS software in modelling.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h)

Target group:
Students having statistics as the major or a minor subject

Prerequisites and co-requisites:
Linear regression; Basic methods in data-analysis

Recommended optional programme components:

Recommended or required reading:

Assessment methods and criteria:
Active participation in practicals and final exam. Read more about assessment criteria at the University of Oulu webpage

Grading:
Fail, 1-5

Person responsible:
Mikko Sillanpää

Working life cooperation:
No

Other information:

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805353A: Statistical Software, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
805340A Statistical Software 4.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

**Timing:**
3. year studies. Fall semester. Timing varies.

**Learning outcomes:**
After successful completion of the course the student can use independently major statistical software needed in data analysis.

**Contents:**
The course covers R, SAS and IBM SPSS, and their most important tools for data management, statistical computation, graphics and programming will be introduced and proficiency for their fluent use is acquired.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
42 h lectures, exercises and tutoring. 88 h learning tasks and self-study.

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
806112P Basic methods of data-analysis

**Recommended optional programme components:**
-  

**Recommended or required reading:**
Lecture notes

**Assessment methods and criteria:**
Home works

**Grading:**
Numerical grading 1-5 (or fail)

**Person responsible:**
Hanna Heikkinen

**Working life cooperation:**
No

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**801396A: Introduction to Probability Theory II, 5 op**

**Opiskelumuoto:** Intermediate Studies

**Laji:** Course

**Vastuuysikkö:** Field of Mathematics

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen oppimateriaali:**
Tuominen, P., , 1993

**Opintokohteen kielet:** Finnish

**ECTS Credits:**
4 cr

**Language of instruction:**
Finnish

**Timing:**
2. year, Fall semester

**Learning outcomes:**
On successful completion of this course, the student will be able to
- understand probability theory deeper than before
- apply various stochastic models
- derive the basic results associated with the new concepts introduced

**Contents:**
The course is a direct continuation for the course Probability Theory I. The new concepts include for instance the moments of a distribution, the probability generating function, the Law of Large Numbers, the Central Limit Theorem as well as two-dimensional distributions.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
24h lectures, 12h exercises

**Target group:**
Major- and minor students. Recommended for students aiming to Master's degree with major in statistics or major in mathematics and computer sciences.

**Prerequisites and co-requisites:**
801195P Introduction to probability I
802352A Euclidean topology
802353A Series and integrals

**Assessment methods and criteria:**
Final exam
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Kenneth Nordström.

### H326650: Statistics orientation module, 0 - 100 op

**Voimassaolo:** 01.08.2015 -
**Opiskelumuoto:** Basic and Intermediate Studies
**Laji:** Study module
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

**Compulsory**

**802351A: Vector Calculus, 5 op**

**Voimassaolo:** 01.06.2015 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
- 800328A Calculus of several variables 5.0 op
- 800322A Analysis II 8.0 op

**ECTS Credits:**
5 ECTS credits
Language of instruction: Finnish

Timing:
1st or 2nd year, 3rd period

Learning outcomes:
After completing the course the student is able to - operate functions of several variables - apply derivates of functions of several variables - calculate multiple integrals

Contents:
The course concerns calculus of severable variables. The central concepts of the course are partial derivative, gradient, divergence, curl and multiple integral. Integral theorems related to functions of several variables are also presented. The course offers basic tools for further courses in analysis as well as for applications.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h lectures, 14h exercises, 91h study a part of which may be guided

Target group:
Mathematics major and minor students

Prerequisites and co-requisites:
802161P Introduction to Real Functions
802120P Introduction to Matrices

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Final exam

Grading:
1-5, fail

Person responsible:
Mahmoud Filali

Working life cooperation:
No

Other information:
-

806112P: Basic Methods of Data Analysis, 10 op

Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikko: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Jari Pääkkö
Opintokohteen oppimateriaali:
Armitage, P. , , 2002
Opintokohteen kielet: Finnish
Leikkaavuudet:
805305A Introduction to Regression and Analysis of Variance 5.0 op

ECTS Credits:
10 cr

Language of instruction: Finnish

Timing:
The course is held in the autumn semester, during periods 1 and 2.

Learning outcomes:
On successful completion of this course, the student will be able to
- analyze continuous and categorial response in the most common experimental and observational studies
- critically evaluate chosen model
- use some statistical software

Contents:
Skills for performing statistical analyses and inferences on the basis of data obtained in common experimental and observational studies are expanded and deepened. Topics included are e.g. (1) principles of collection, description, and modelling of, and inference on statistical data; (2) basic methods of analysing continuous outcome variables, like comparison of groups, analysis of variance, regression analysis, residuals and model diagnostics, nonparametric methods, treatment of correlated and lifetime (censored) observations; (3) and basic methods of analysing binary, categorical and count data.

Mode of delivery:
Face-to-face teaching.

Learning activities and teaching methods:
56h lectures, 42h exercises, self-study.

Target group:
Major and minor students.

Prerequisites and co-requisites:
For major students:
801195P Introduction to Probability Theory I, 806113P Introduction to statistics, 802118P Linear algebra I, 802154P Elementary functions, 802155P Limits and continuity, 802156P Derivative
For minor students: 806109P Basic Methods in Statistics I

Recommended optional programme components:
To be completed before 805310A Statistical inference I, 806359A Regression modelling and other studies in statistics.

Recommended or required reading:
Lecture notes.

Assessment methods and criteria:
Intermediate (2) or final exam.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
The course utilizes a numerical grading scale 1-5 / fail.

Person responsible:
Jari Päkkilä

Working life cooperation:
- 805331A: Project seminar I, 6 op

Voimassaolo: 23.04.2007 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
6 cr

Language of instruction:
Finnish

Timing:
3. year of studies (fall or spring)

Learning outcomes:
After successful completion of the project seminar the student is able to conduct a small scale statistical investigation and report it both in written form and orally.

Contents:
Under supervision of the leader of the seminar each student conducts a small-scale statistical investigation on a given empirical topic and material, makes a written report from it and presents it orally in seminar sessions. The written report is the B.Sc. thesis, when statistics is the major subject of the student.

Mode of delivery:
Seminars

Learning activities and teaching methods:
Seminar sessions (20 h) and independent work.

Target group:
Major and minor students

Prerequisites and co-requisites:
Basic methods of data-analysis

Recommended optional programme components:
Maturity test is written of the subject of proseminar.

Recommended or required reading:
-

Assessment methods and criteria:
Seminar (written) and presentation

Grading:
Pass/Fail

Person responsible:
Jari Päkkilä

Working life cooperation:
-

800300A: Maturity test, 0 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
0 cr

Language of instruction:
Finnish/Swedish

Timing:
Third year
Learning outcomes:
Maturity test

Contents:
Students must take a written maturity test to demonstrate their language skills and how well they know the topic of their thesis. The maturity test is taken in the language in which the student has received his or her education in Finland. If the student has received his or her education in a language other than Finnish or Swedish, the degree programme determines the language of the maturity test. In such cases only the contents of the maturity test is evaluated, not the language.

Mode of delivery:
Maturity test written in examination room.

Learning activities and teaching methods:
Maturity test

Target group:
Major students

Prerequisites and co-requisites:
Bachelor's degree (or similar)

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Maturity test
Read more about assessment criteria at the University of Oulu webpage.

Grading:
Pass/Fail

Person responsible:
Supervisor of thesis

Working life cooperation:
-

Electives

**H326635: Optional intermediate studies in statistics, 0 - 180 op**

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Study module
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

   Ei opintojaksokuvauksia.

Electives

**805324A: Time series analysis, 5 op**

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen oppimateriaali:
Harvey, Andrew C., 1993
Lütkepohl, Helmut, 1991
Hamilton, James D., 1994
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Language of instruction:
Finnish

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply statistical software to fit time series models.

Contents:
1. The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram.
2. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models.
3. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH).
4. Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises.
There are 14 times 2 hour lectures and 7 times 2 hour exercises.

Target group:
Students of mathematical sciences, econometrics and finance students.

Prerequisites and co-requisites:
Basic probability theory.

Recommended optional programme components:
-

Recommended or required reading:

Assessment methods and criteria:
Examination
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1 - 5

Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
Home page of the course is http://cc.oulu.fi/~jklemela/timeseries/
Recommended reading:
**805308A: Analysis of longitudinal data, 5 op**

**Opiskelumuoto:** Intermediate Studies  
**Laji:** Course  
**Vastuuysikkö:** Field of Mathematics  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen oppimateriaali:**  
Peter J. Diggle et al., 2002  
Hsiao, Cheng, 2003  
McCulloch, Charles E., 2001  
Fitzmaurice, Garrett M., 2004  
**Opintokohteen kielet:** Finnish

**ECTS Credits:**  
5/6 cr

**Language of instruction:**  
Finnish

**Timing:**  
Every second year.

**Learning outcomes:**  
After finishing the course a student can apply pooled ordinary least squares, generalized least squares, random effects methods, and fixed effects methods.

**Contents:**

1. Introduction: data types, omitted variables.  
2. Mathematical tools: conditional expectation, basic asymptotic theory.  
4. Estimating systems of equations by ordinary least squares and by generalized least squares, panel data and seemingly unrelated regression as examples, simultaneous exogeneity and strict exogeneity, consistency and asymptotic normality, homoskedasticity and heteroskedasticity.  
5. Pooled ordinary least squares for panel data, aggregated time effect, dummy variables, testing serial correlation and heteroskedasticity.  
6. Unobserved effects model: random effects and fixed effects.  
7. Random effects methods: random effects structure of the covariance matrix.  
8. Fixed effects methods: fixed effects transformation, the use of dummy variables, first differencing transformation.  
9. Comparison of estimators.

**Mode of delivery:**  
Face-to-face teaching

**Learning activities and teaching methods:**  
Besides lectures, there are voluntary exercises. There are 14 times 2 hour lectures and 7 times 2 hour exercises.

**Target group:**  
Students of economics and mathematical sciences.

**Prerequisites and co-requisites:**  
Basic Mathematics for Economics 1 and 2, Basic Methods in Statistics 1, Introduction to Econometrics.

**Recommended or required reading:**  

**Assessment methods and criteria:**  
Examination  
Read more about assessment criteria at the University of Oulu webpage.

**Grading:**  
1 - 5
Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
The course is organized every two years.
The home page of the course is http://cc.oulu.fi/~jklema/panel/

805349A: Likelihood Inference, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
  805310A Statistical Inference I 10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd or 3rd year of B.Sc. studies, spring term

Learning outcomes:
After successful completion of the course the student can describe the basic principles of likelihood inference, derive likelihood functions of models with few parameters, compute likelihood quantities based on them, and interpret results such obtained.

Contents:
Statistical model and observation data; likelihood function, log-likelihood, score, information; maximum likelihood estimation, relative likelihood, likelihood interval and likelihood region, profile likelihood; normal approximation of log-likelihood; use of R environment in inferential problems.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h), and independent work

Target group:
Students having statistics as the major or a minor subject

Prerequisites and co-requisites:
Introduction to Probability Theory I, Basic Methods of Data Analysis

Recommended optional programme components:
Is needed in nearly all intermediate and advanced courses in statistics

Recommended or required reading:

Assessment methods and criteria:
Final exam. Read more about assessment criteria at the University of Oulu webpage.
Grading:
Fail, 1-5

Person responsible:
Esa Lääärä

Working life cooperation:
No

Other information:
-

805350A: Estimation and Test Theory, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lääärä Esa
Opintokohteen kielet: Finnish
Leikkaavuudet:
  805310A  Statistical Inference I  10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
2nd or 3rd year during B.Sc. studies

Learning outcomes:
After successful completion of the course the student can describe the basic principles of frequentist and bayesian statistical inference, compute point and interval estimates, test statistics and P-values based on likelihood function of models with few parameters, and interpret results thus obtained.

Contents:
Statistical model and observational data; construction and properties of point estimators and confidence intervals; likelihood ratio, score and Wald test statistics and their asymptotic sampling distribution; jackknife and bootstrap methods; elements of bayesian inference; use of R environment in inferential problems.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h), practicals and computer classes (14 h), and independent work

Target group:
Students having statistics as the major or a minor subject

Prerequisites and co-requisites:
Likelihood inference, Introduction to probability theory I, Basic Methods of Data Analysis

Recommended optional programme components:
Needed in nearly all intermediate and advanced courses of statistics

Recommended or required reading:

**Assessment methods and criteria:**
Final Exam. Read more about assessment criteria at the University of Oulu webpage

**Grading:**
Fail, 1-5

**Person responsible:**
Esa Läärä

**Working life cooperation:**
No

**Other information:**
-

805351A: Linear Regression, 5 op

**Voimassaolo:** 01.06.2015 -

**Opiskelumuoto:** Intermediate Studies

**Laji:** Course

**Vastuuyksikkö:** Field of Mathematics

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Läärä Esa

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**

- 806359A Regression modelling 10.0 op

**ECTS Credits:**
5 ECTS credits

**Language of instruction:**
Finnish

**Timing:**
2nd or 3rd year during B.Sc. studies

**Learning outcomes:**
After successful completion of the course the student can describe basic concepts and assumptions in linear models for continuous outcome variables as well as main principles of regression modelling, and can also apply these methods in analysis of experimental and non-experimental observation data.

**Contents:**
Linear regression models for a continuous outcome variable; formulation of the model, selection of variables and interpretation of parameters; fitting the models, estimation of parameters and prediction using method of least squares; model criticism and diagnostics; use of R environment and SAS software in modelling.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
Lectures (28 h), practicals and computer classes (14 h) and independent work.

**Target group:**
Students having statistics as the major or a minor subject.

**Prerequisites and co-requisites:**
Basic Methods of Data Analysis; Core courses in the B.Sc curriculum of mathematical sciences.

**Recommended optional programme components:**
Prerequisite to the course Generalized Linear Models

**Recommended or required reading:**

**Assessment methods and criteria:**
Active participation in practicals and final exam. Read more about assessment criteria at the University of Oulu webpage

**Grading:**
Fail, 1-5

**Person responsible:**
Esa Läärá

**Working life cooperation:**
No

**Other information:**
-

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**805352A: Generalized Linear Models, 5 op**

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikko Sillanpää
Opintokohteen kielet: Finnish
Leikkaavuudet:
- 805630S Generalized Linear Models  5.0 op
- 806359A Regression modelling  10.0 op

**ECTS Credits:**
5 ECTS credits

**Language of instruction:**
Finnish

**Timing:**
2nd or 3rd year of studies in B.Sc. programme

**Learning outcomes:**
After successful completion of the course the student can describe the basic concepts and assumptions of generalized linear models as well as main principles of regression modelling, and can also apply these methods in analysis of experimental and observational data.

**Contents:**
Generalized linear regression models for continuous, binary and count outcomes; formulation of the model, selection of variables and interpretation of parameters; fitting the models, estimating the parameters and prediction by the method of maximum likelihood; model criticism and diagnostics; use of R environment and SAS software in modelling.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
Lectures (28 h), practicals and computer classes (14 h)

**Target group:**
Students having statistics as the major or a minor subject

**Prerequisites and co-requisites:**
Linear regression; Basic methods in data-analysis
Recommended optional programme components:

- 

Recommended or required reading:


Assessment methods and criteria:

Active participation in practicals and final exam. Read more about assessment criteria at the University of Oulu webpage

Grading:

Fail, 1-5

Person responsible:

Mikko Sillanpää

Working life cooperation:

No

Other information:

-

805353A: Statistical Software, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:

805340A Statistical Software 4.0 op

ECTS Credits:

5 ECTS credits

Language of instruction:

Finnish

Timing:

3. year studies. Fall semester. Timing varies.

Learning outcomes:

After successful completion of the course the student can use independently major statistical software needed in data analysis.

Contents:

The course covers R, SAS and IBM SPSS, and their most important tools for data management, statistical computation, graphics and programming will be introduced and proficiency for their fluent use is acquired.

Mode of delivery:

Face-to-face teaching

Learning activities and teaching methods:

42 h lectures, exercises and tutoring. 88 h learning tasks and self-study.

Target group:

Major and minor students

Prerequisites and co-requisites:
80612P Basic methods of data-analysis

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Home works

Grading:
Numerical grading 1-5 (or fail)

Person responsible:
Hanna Heikkinen

Working life cooperation:
No

801396A: Introduction to Probability Theory II, 5 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Tuominen, P., , 1993
Opintokohteen kielet: Finnish

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
2. year, Fall semester

Learning outcomes:
On successful completion of this course, the student will be able to
- understand probability theory deeper than before
- apply various stochastic models
- derive the basic results associated with the new concepts introduced

Contents:
The course is a direct continuation for the course Probability Theory I. The new concepts include for instance the moments of a distribution, the probability generating function, the Law of Large Numbers, the Central Limit Theorem as well as two-dimensional distributions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
24h lectures, 12h exercises

Target group:
Major- and minor students. Recommended for students aiming to Master's degree with major in statistics or major in mathematics and computer sciences.

Prerequisites and co-requisites:
801195P Introduction to probability I
802352A Euclidean topology
802353A Series and integrals

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

**Grading:**
1-5

**Person responsible:**
Kenneth Nordström.

**H325035: Optional intermediate studies in mathematics, 0 - 180 op**

**Voimassaolo:** 01.08.2010 -  
**Opiskelumuoto:** Intermediate Studies  
**Laji:** Study module  
**Vastuuysikkö:** Field of Mathematics  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kiele:** Finnish

Ei opintojaksokuvausia.

**Electives**

**800329A: Topology, 8 op**

**Opiskelumuoto:** Intermediate Studies  
**Laji:** Course  
**Vastuuysikkö:** Field of Mathematics  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Mahmoud Filali  
**Opintokohteen oppimateriaali:**  
Vala K., Suominen K., , 1990  
**Opintokohteen kiele:** Finnish

**ECTS Credits:**
8 cr

**Language of instruction:**
English (also Finnish)

**Timing:**
Second year or later. Fall/spring term

**Learning outcomes:**
On successful completion of this course, the student will be able to follow more advanced topology and analysis.

**Contents:**
The course presents the very basics of topology that mathematics students should know. It starts with elementary set theory, then it goes on covering metric spaces including Baire's theorem; topological spaces and convergence in topological spaces; separation axioms including Urysohn's lemma and Tietze extension theorem; compact spaces including Tyconoff theorem; and ends with connected spaces.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
56 hours lecture, 28 h exercises

**Target group:**
Major and minor students
Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics.

Recommended optional programme components:

Recommended or required reading:
S. Willard: General Topology;
K. Suominen & K. Vala: Topologia;

Assessment methods and criteria:
Final exam, or mid-term exams
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Mahmoud Filali

Working life cooperation:

802362A: Introduction to computational inverse problems, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikko Orispää
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802328A: Basics in Number Theory, 5 op

Voimassaolo: 01.06.2011 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen oppimateriaali:
Hardy, G. H., , 1979
Rosen, Kenneth H., , 1993
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Language of instruction:
Finnish/English

Timing:
2.-3. year of studies. Timing varies.

Learning outcomes:
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; for example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

Contents:
In our lectures we consider arithmetical properties of the common numbers involved in studying mathematics and in particular number theory. Also the methods will get a special interest. Examples of the numbers under the research will be binomials, continued fractions, sums of powers and some numbers sharing a name with the mathematicians Bernoulli, Euler, Fermat, Fibonacci, Heron, Lucas, Mersenne, Neper, Pythagoras, Stirling, Wilson and Wolstenholme. From the tools we mention congruences of rational numbers and polynomials, difference operators, generating series, irrationality considerations, matrix presentations, recurrences and telescopes.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
36h lectures, 18h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
802354A Lukuteoria ja ryhmät,
802355A Rings, fields and polynomials
802118P Linear algebra I
802119P Linear algebra II
802352A Euclidean topology
802353A Series and integrals

Recommended optional programme components:
-

Recommended or required reading:
Lecture notes,
G.H. Hardy ja E.M. Wright: An Introduction to the Theory of Numbers;
Kenneth H. Rosen: Elementary number theory and its applications.

Assessment methods and criteria:
Mid-term exams or final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Tapani Matala-aho

Working life cooperation:
-

802331A: Principles to Mathematical Modelling, 8 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
802360A: Introduction to inverse problems, 4 op

**Voimassaolo:** 01.08.2010 -
**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Sari Lasanen
**Opintokohteen kielet:** Finnish

**ECTS Credits:**
4 cr

**Language of instruction:**
Finnish. Alternatively, a book examination in English.

**Learning outcomes:**
Upon completion, the student will be able to
- recognise several inverse problems
- describe typical properties of inverse problems
- solve simple inverse problems with accurate and inaccurate data

**Contents:**
1. Examples of inverse problems and their typical properties
2. Well-posed and ill-posed problems
3. Least squares solutions
4. Tikhonov regularization
5. Statistical inverse problems

**Learning activities and teaching methods:**
Lectures 4x45 min / week. Exercises 2x45 min /week.

**Target group:**
Suitable for major and minor students.

**Prerequisites and co-requisites:**
- 802118P Linear Algebra I
- 802119P Linear Algebra II
Also recommended:
- 800322A Multidimensional Analysis (or Analysis II)
- 801396A Introduction to Probability Theory II
- 802352A Euclidian Topology
- 800345A Differential Equations I

**Assessment methods and criteria:**
Exam.
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Other information:**
This course does not contain numerical programming tasks. Computer-aided computations are contained in a separate course
802362A Introduction to Computational Inverse Problems.

801396A: Introduction to Probability Theory II, 5 op

**Opiskelumuoto:** Intermediate Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
Opintokohteen oppimateriaali:
Tuominen, P., 1993
Opintokohteen kielet: Finnish

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
2. year, Fall semester

Learning outcomes:
On successful completion of this course, the student will be able to
- understand probability theory deeper than before
- apply various stochastic models
- derive the basic results associated with the new concepts introduced

Contents:
The course is a direct continuation for the course Probability Theory I. The new concepts include for instance the moments of a distribution, the probability generating function, the Law of Large Numbers, the Central Limit Theorem as well as two-dimensional distributions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
24h lectures, 12h exercises

Target group:
Major- and minor students. Recommended for students aiming to Master's degree with major in statistics or major in mathematics and computer sciences.

Prerequisites and co-requisites:
801195P Introduction to probability I
802352A Euclidean topology
802353A Series and integrals

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Kenneth Nordström.

801346A: Introduction to Cryptography, 4 op

Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen kielet: Finnish
Leikkaavuudet:
802336A Introduction to Cryptography 5.0 op

ECTS Credits:
4 cr
Language of instruction: Finnish

Timing: 2. year or later, Fall term (1. or 2. period)

Learning outcomes:
After completing the course, student
- knows the principles of some traditional symmetric key methods
- knows how public key methods (RSA, discrete logarithm, knapsack) work
- is familiar with the possibility to use and apply number theory in cryptography

Contents:
The course considers some traditional symmetric key methods (affine system, matrix cryptography) and three public key methods, namely RSA, discrete logarithm and knapsack.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
27 h lectures, 15 h exercises

Target group:
Major and minor students

Prerequisites and co-requisites:
Compulsory basic and intermediate studies in mathematics.

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Tapani Matala-aho

802364A: Introduction to Mathematical Software, 6 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Mikko Orispää
Opintokohteen kielet: Finnish

ECTS Credits: 6 cr

Language of instruction:
Lecturing language is Finnish, but the main points can be explained also in English if necessary. The software and the majority of course material is also in English.

Timing:
Autumn semester, period one.

Learning outcomes:
Upon completion of the course, the student
- knows the basics of the use of the most common mathematical software
- is able to use mathematical software in solving mathematical tasks and problems
- is able to independently deepen her knowledge of different mathematical software as necessary.

Contents:
During the course, the student learns the basics of some of commonly used mathematical software which include
- R
- Matlab
- Mathematica
Time permitting, it is also possible to learn other mathematical software depending the interests of the students.

Mode of delivery:
The course is arranged in a computer class as a series of lectures and rehearsals. On the lectures, the students have the possibility to use and try the mathematical software during the lectures. In the rehearsals, different given problems and tasks are solved together.

Learning activities and teaching methods:
Lecures 22h / Rehearsals 22h / Self-study 60h. The self-study contains the independent learning of the software and also the preparation of the final assignments.

Target group:
Anybody interested in mathematical software.

Prerequisites and co-requisites:
The required prerequisite is the completion of following courses (or corresponding knowledge of the subject):
- 802118P Linear Algebra I
- 802119P Linear Algebra II.

Recommended optional programme components:
The course is an independent entity and does not require additional studies carried out at the same time.

Recommended or required reading:
The required and recommended reading consists mainly on free material (manuals/tutorial) found in the internet. More information will be given at the beginning of the course.

Assessment methods and criteria:
The course is assessed by final assignments. The student who wish to complete the course at A-level will make two separate assignments of given topics using (at least) two different mathematical software. Those who wish to complete the course in S-level will need to discuss with the lecturer about the extra work needed to pass. For example, it could be possible to do assignments of wider topics, making an assignment(s) with a software not covered in the course, or making an assignment that requires particular skills and knowledge.
Read more about assessment criteria at the University of Oulu webpage.

Grading:
The course utilizes verbal grading scale “Pass/ fail”.

Person responsible:
Mikko Orispää

Working life cooperation:
-
801329A: Mathematics in Teaching, 3 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Intermediate Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:

ECTS Credits:
3 cr/ 81 hours of work

Language of instruction:
Finnish

Timing:
1st year, periods 3 and 4

Learning outcomes:
The student can reflect critically on the learning and teaching of mathematics. The student can analyze the connection between mathematics at school and at university.

Contents:
Learning and teaching mathematics are thought about and discussed. The course consists of reflective exercises and seminar meetings where the exercises are discussed. A student analyzes the connection between mathematics at school and at university. A student writes a learning journal.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
24 h seminar meetings, 57 h self-study and group work.

Target group:
Mathematics teacher students

Prerequisites and co-requisites:
-

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Active participation, learning journal, group work

Grading:
Pass/Fail

Person responsible:
Riikka Palkki

Working life cooperation:
-

Other information:
-

800104P: Number Systems, 4 op

Voimassaolo: 01.03.2011 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:

800347A Number systems 5.0 op

ECTS Credits:
4 cr

Language of instruction:
Finnish

Timing:
Autumn semester, period I. Recommended to complete the course at the first or second autumn semester.

Learning outcomes:
Having completed the course, the student is able to
- define and construct the most common number systems
- list and use the basic arithmetic operations in number systems

Contents:
The course considers the basics of arithmetic and algebra in the setting of the most common number systems (natural numbers, integers, rationals and reals). The course begins with the construction of natural numbers and continues, through integers and rational numbers, to the construction of real numbers.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 28 h, exercises 14 h, self-study 66 h

Target group:
Major and minor students

Prerequisites and co-requisites:
802151P Introduction to mathematical deduction

Recommended optional programme components:
For first year students, recommended to be completed simultaneously with the course "802155P Continuity and Limit".

Recommended or required reading:
Lecture notes

Assessment methods and criteria:
Final exam

Grading:
1-5, fail

Person responsible:
Jukka Kauppi

Working life cooperation:
031076P: Differential Equations, 5 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Applied Mathematics and Computational Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Leikkaavuudet:
ay031076P  Differential Equations (OPEN UNI)  5.0 op
800320A  Differential equations  5.0 op
031017P  Differential Equations  4.0 op

Ei opintojaksokuvauksia.

806112P: Basic Methods of Data Analysis, 10 op

Opiskelumuoto: Basic Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Jari Päkkilä
Opintokohteen oppimateriaali:
Armitage, P. . , 2002
Opintokohteen kielet: Finnish
Leikkaavuudet:
805305A  Introduction to Regression and Analysis of Variance  5.0 op

ECTS Credits:
10 cr
Language of instruction:
Finnish
Timing:
The course is held in the autumn semester, during periods 1 and 2.
Learning outcomes:
On successful completion of this course, the student will be able to
- analyze continuous and categorical response in the most common experimental and observational studies
- critically evaluate chosen model
- use some statistical software

Contents:
Skills for performing statistical analyses and inferences on the basis of data obtained in common experimental and observational studies are expanded and deepened. Topics included are e.g. (1) principles of collection, description, and modelling of, and inference on statistical data; (2) basic methods of analysing continuous outcome variables, like comparison of groups, analysis of variance, regression analysis, residuals and model diagnostics, nonparametric methods, treatment of correlated and lifetime (censored) observations; (3) and basic methods of analysing binary, categorical and count data.

Mode of delivery:
Face-to-face teaching.

Learning activities and teaching methods:
56h lectures, 42h exercises, self-study.

Target group:
Major and minor students.

**Prerequisites and co-requisites:**
For major students:
801195P Introduction to Probability Theory I, 806113P Introduction to statistics, 802118P Linear algebra I,
802154P Elementary functions, 802155P Limits and continuity, 802156P Derivative
For minor students: 806109P Basic Methods in Statistics I

**Recommended optional programme components:**
To be completed before 805310A Statistical inference I, 806359A Regression modelling and other studies in statistics.

**Recommended or required reading:**
Lecture notes.

**Assessment methods and criteria:**
Intermediate (2) or final exam.
Read more about [assessment criteria](#) at the University of Oulu webpage.

**Grading:**
The course utilizes a numerical grading scale 1-5 / fail.

**Person responsible:**
Jari Päkkilä

**Working life cooperation:**

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**800600S: Maturity test, 0 op**

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Field of Mathematics  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish  

Ei opintojaksokuvauksia.

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**800697S: Pro Gradu Thesis, 20 op**

**Opiskelumuoto:** Advanced Studies  
**Laji:** Diploma thesis  
**Vastuuysikkö:** Field of Mathematics  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish  

Ei opintojaksokuvauksia.

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**802639S: Special Course for Teachers of Mathematics: Content Planning, 5 op**

**Voimassaolo:** 01.06.2015 -  
**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Field of Mathematics  
**Arvostelu:** 1 - 5, pass, fail  
**Opintokohteen kielet:** Finnish  

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Leikkaavuudet:

800661S Special course for teachers of mathematics 5.0 op
802632S-01 Special course for teachers of mathematics / Lesson plans for teaching mathematics 4.0 op
802632S-03 Special course for teachers of mathematics / Other training 3.0 op
802632S-02 Special course for teachers of mathematics / Correcting tests in mathematics 3.0 op
802632S Special course for teachers of mathematics 10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
4th or 5th year, 3rd and 4th period

Learning outcomes:
After completing the course the student is able to
- combine a mathematical way of thinking to teaching
- plan teaching content that supports mathematical understanding

Contents:
In this course the students plan and execute teaching samples. In addition we examine research in didactics of mathematics. The students also write reports about their works. Works are discussed in a seminar.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
30h seminar, 103h independent work

Target group:
Mathematics subject teacher students

Prerequisites and co-requisites:
Bachelor degree in mathematics or equivalent

Recommended optional programme components:
-

Recommended or required reading:
-

Assessment methods and criteria:
Active participation, reporting

Grading:
pass/fail

Person responsible:
Pekka Salmi

Working life cooperation:
No

Other information:
-

802640S: Special Course for Teachers of Mathematics: High School Mathematics, 3 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Leikkaavuudet:

802632S-02 Special course for teachers of mathematics / Correcting tests in mathematics 3.0 op
802632S-01 Special course for teachers of mathematics / Lesson plans for teaching mathematics 4.0 op
802632S-03 Special course for teachers of mathematics / Other training 3.0 op
802632S Special course for teachers of mathematics 10.0 op

ECTS Credits:
3 ECTS credits

**Language of instruction:**
Finnish

**Timing:**
4th or 5th year, 3rd and 4th period

**Learning outcomes:**
After completing the course the student is able to
- see the high school mathematics contents from the perspective of the teacher
- connect the mathematics contents to matriculation examination
- mark matriculation exams

**Contents:**
During the course the students review contents from high school mathematics and learn about the principles of marking the matriculation exam.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
28h contact teaching, 52h independent study

**Target group:**
Mathematics subject teacher students

**Prerequisites and co-requisites:**
Bachelor degree in mathematics or equivalent

**Recommended optional programme components:**
-

**Recommended or required reading:**
-

**Assessment methods and criteria:**
Active participation

**Grading:**
Pass/fail

**Person responsible:**
Pekka Salmi

**Working life cooperation:**
No

**Other information:**
-

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**802641S: Special Course for Teachers of Mathematics: Training, 2 - 5 op**

**Voimassaolo:** 01.06.2015 -

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuyksikkö:** Field of Mathematics

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen kielet:** Finnish

**Leikkaavuudet:**
- 802632S-03 Special course for teachers of mathematics / Other training 3.0 op
- 802632S-01 Special course for teachers of mathematics / Lesson plans for teaching mathematics 4.0 op
- 802632S-02 Special course for teachers of mathematics / Correcting tests in mathematics 3.0 op
- 802632S Special course for teachers of mathematics 10.0 op

**ECTS Credits:**
2-5 credits

**Language of instruction:**
Finnish

**Timing:**
4th or 5th year, any period

**Learning outcomes:**
The student is able to apply her/his skills in practice and gains experience in teaching mathematics.

**Contents:**
Teaching practice in mathematics. The practice may include training, preparation of teaching materials and reporting.
Mode of delivery:  
Depends on the practice.

Learning activities and teaching methods:  
53h to 133h work depending on the practice.

Target group:  
Mathematics subject teacher students

Prerequisites and co-requisites:  
Bachelor degree in mathematics or equivalent

Recommended optional programme components:

-  

Recommended or required reading:

-  

Assessment methods and criteria:  
practice, reporting

Grading:  
pass/fail

Person responsible:  
Pekka Salmi

Working life cooperation:  
Yes. The students teach mathematics in real life situations.

Other information:

-  

H325052: Subject teacher's advanced module, 0 - 100 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Advanced studies for subject teacher students

802662S: Supervising advanced problems, 5 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:

5 cr

Language of instruction:

Finnish

Timing:

4-5 year

Learning outcomes:

After completing the course, students are able to
- combine mathematical thinking and teaching
- plan mathematical tasks which support profound mathematical understanding rather than computational procedures.
Contents:
In this course a mathematics tutorial group is planned and implemented.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
28h seminar, 12h teaching, 93h independent and group work

Target group:
Mathematics teacher students

Prerequisites and co-requisites:
B.Sc and teacher pedagogical studies

Assessment methods and criteria:
Participation

Grading:
Pass/fail

Person responsible:
Marko Leinonen

802648S: Mathematical Problem Solving, 10 op

Voimassaolo: 01.01.2011 -
Opiskeluoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

800660S: Group Theory, 10 op

Opiskeluoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Niemenmaa Markku
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802655S: Continued Fractions, 5 op

Voimassaolo: 01.01.2011 -
Opiskeluoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Language of instruction:
FI/EN

Recommended or required reading:
Kenneth H. Rosen: Elementary number theory and its applications.
Lisa Lorentzen and Haakon Waadeland: Continued Fractions with Applications (1992).
Oskar Perron: Die Lehre von den Kettenbruchen (1913).

Course material: http://cc.oulu.fi/~tma/OPETUS.html

802656S: Algebraic numbers, 5 op

Voimassaolo: 01.01.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Language of instruction:
FI/EN

Learning outcomes:
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course. More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding. When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

Contents:
First we revise some basics of rings and fields which are needed to proceed ahead field extensions. In particular, divisibility in an integral domain is carefully studied yielding to applications in the theory of polynomial algebra and algebraic integers. The theory of algebraic numbers is strongly based on polynomial algebra, where the properties of zeros and divisibility of polynomials are considered. The definition of an algebraic number will be generalized to the algebraic elements of field extensions going forward to algebraic fields. Considered as most important algebraic fields we get number fields which are finitely generated subfields of the field $\mathbb{A}$ of all complex algebraic numbers. In particular, we study quadratic number fields. Further, we shall consider the divisibility and factorization of algebraic integers with some applications to Diophantine equations.

Prerequisites and co-requisites:
Algebra I and II, Linear algebra I and II, Basics in Number Theory (Number theory I)

Recommended or required reading:
I.N. Stewart and D.O. Tall: Algebraic number theory.
Daniel Marcus: Number fields.
J.B. Fraleigh: Abstract algebra.
Michael Artin: Algebra.

Course material: http://cc.oulu.fi/~tma/OPETUS.html

802645S: Number Theory A, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho  
Opintokohteen kielet: Finnish  

Ei opintojaksokuvauksia.

802646S: Number Theory B, 5 op  
Voimassaolo: 01.08.2009 -  
Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuysikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Tapani Matala-aho  
Opintokohteen kielet: Finnish  

Ei opintojaksokuvauksia.

802651S: Measure and Integration, 5 op  
Voimassaolo: 01.08.2010 -  
Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuysikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Ville Suomala  
Opintokohteen kielet: Finnish  

Ei opintojaksokuvauksia.

H325053: Mathematics advanced module, 0 - 100 op  
Voimassaolo: 01.08.2015 -  
Opiskelumuoto: Advanced Studies  
Laji: Study module  
Vastuuysikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opintokohteen kielet: Finnish  

Ei opintojaksokuvauksia.

Electives

800660S: Group Theory, 10 op  
Opiskelumuoto: Advanced Studies  
Laji: Course  
Vastuuysikkö: Field of Mathematics  
Arvostelu: 1 - 5, pass, fail  
Opettajat: Niemenmäki Markku  
Opintokohteen kielet: Finnish  

Ei opintojaksokuvauksia.

802655S: Continued Fractions, 5 op
Language of instruction:
FI/EN

Recommended or required reading:
Kenneth H. Rosen: Elementary number theory and its applications.
Lisa Lorentzen and Haakon Waadeland: Continued Fractions with Applications (1992).
Oskar Perron: Die Lehre von den Kettenbruchen (1913).

Course material: http://cc.oulu.fi/~tma/OPETUS.html

802656S: Algebraic numbers, 5 op

Language of instruction:
FI/EN

Learning outcomes:
As usual in my mathematical studies I shall be able to solve problems arising from the subject and to prove essential theorems starting from the given definitions using the tools applied in the course.
More detailed; For example, when I pass the course with the grade 1/5, I shall recognize most definitions and I am able to solve closely related problems. Also I am able to rewrite short proofs with some understanding.
When I pass the course with the grade 5/5, then I shall understand well the given definitions with the proofs of the theorems deduced from them. Further, I am able to solve challenging problems which demand independent deductions with several stages and applications of appropriate tools.

Contents:
First we revise some basics of rings and fields which are needed to proceed ahead field extensions. In particular, divisibility in an integral domain is carefully studied yielding to applications in the theory of polynomial algebra and algebraic integers.
The theory of algebraic numbers is strongly based on polynomial algebra, where the properties of zeros and divisibility of polynomials are considered.
The definition of an algebraic number will be generalized to the algebraic elements of field extensions going forward to algebraic fields. Considered as most important algebraic fields we get number fields which are finitely generated subfields of the field A of all complex algebraic numbers. In particular, we study quadratic number fields.
Further, we shall consider the divisibility and factorization of algebraic integers with some applications to Diophantine equations.

Prerequisites and co-requisites:
Algebra I and II, Linear algebra I and II, Basics in Number Theory (Number theory I)

Recommended or required reading:
I.N. Stewart and D.O. Tall: Algebraic number theory.
Daniel Marcus: Number fields.
J.B. Fraleigh: Abstract algebra.
802645S: Number Theory A, 5 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Tapani Matala-aho
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802651S: Measure and Integration, 5 op

Voimassaolo: 01.08.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Ville Suomala
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802664S: Differential geometry, 10 op

Voimassaolo: 01.06.2014 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: English

802644S: Introduction to Functional Analysis, 10 op

Voimassaolo: 01.08.2009 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Mahmoud Filali
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802647S: Fourier series and the discrete Fourier transform, 10 op

Voimassaolo: 01.01.2010 -
**802635S: Introduction to partial differential equations, 10 op**

**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Field of Mathematics  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Valeriy Serov  
**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

**802665S: Numerical Analysis, 5 op**

**Voimassaolo:** 01.06.2015 -  
**Opiskelumuoto:** Advanced Studies  
**Laji:** Course  
**Vastuuysikkö:** Field of Mathematics  
**Arvostelu:** 1 - 5, pass, fail  
**Opettajat:** Valeriy Serov  
**Opintokohteen kielet:** Finnish

**ECTS Credits:** 5 ECTS credits  
**Language of instruction:** English  
**Timing:** 4th or 5th year of studies  
**Learning outcomes:**  
On successful completion of this course, the student will be able to choose proper numerical methods for solving basic mathematical problems and approximate the errors of numerical results.  
**Contents:**  
The lecture course is focused to numerical methods for solving the most common basic problems in mathematics. For the methods, convergence, stability and suitability for computer arithmetic are considered. The course contains numerical solution methods for the following basic problems: systems of nonlinear equations, systems of linear equations, interpolation, integration, derivation and differential equations.  
**Mode of delivery:**  
Face-to-face teaching  
**Learning activities and teaching methods:**  
Lectures 24 h and exercises 12 h  
**Target group:**  
Major and minor students  
**Prerequisites and co-requisites:**  
Bachelor's degree in mathematics or equivalent studies
Recommended optional programme components:
The course is an independent entity and does not require additional studies carried out at the same time.

Recommended or required reading:
Lecture notes Ward Cheney, David Kincaid: Numerical Mathematics and Computing

Assessment methods and criteria:
Final exam
Grading:
Fail, 1-5

Person responsible:
Erkki Laitinen

Working life cooperation:
No

Other information:

802666S: Linear Optimization, 5 op
Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Erkki Laitinen
Opintokohteen kielet: Finnish
Leikkaavuudet:
800688S Theory of Optimization 10.0 op

Ei opintojaksokuvausia.

802667S: Nonlinear Optimization, 5 op
Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
4th or 5th year of studies

Learning outcomes:
On successful completion of this course, the student will be able to choose the correct methods for solving the nonlinear convex optimization problems and implement the most typical numerical algorithms for solving them.

Contents:
The lecture course is focused to methods, which can apply for solving essential optimization problems of technical and economical sciences. The lectures consist of following topics: Convex optimization problem,
unconstrained convex optimization, constrained convex optimization, dual of convex problem, Karush-Kuhn-Tucker conditions and penalty optimization method. The topics are considered theoretically and also numerical algorithms for problem solution are presented.

**Mode of delivery:**
Face-to-face teaching

**Learning activities and teaching methods:**
Lectures 28 h and exercises 14 h

**Target group:**
Major and minor students

**Prerequisites and co-requisites:**
Bachelor degree in mathematics or equivalent

**Recommended optional programme components:**
The course is an independent entity and does not require additional studies carried out at the same time.

**Recommended or required reading:**
Lecture notes
A. L. Peressini, F.E. Sullivan, J.J. Uhl: The mathematics of Nonlinear Programming David g. Luenberger: Introduction to Linear and Nonlinear Programming

**Assessment methods and criteria:**
Final exam

**Grading:**
Fail, 1-5

**Person responsible:**
Erkki Laitinen

**Working life cooperation:**
No

**Other information:**
-

802633S: Statistical Pattern Recognition, 10 op

**Opiskelumuoto:** Advanced Studies
**Laji:** Course
**Vastuuysikkö:** Field of Mathematics
**Arvostelu:** 1 - 5, pass, fail
**Opettajat:** Lasse Holmström
**Opintokohteen kielet:** Finnish

**ECTS Credits:**
10 cr

**Language of instruction:**
Finnish

**Timing:**
Spring semester, 3rd and 4th periods.

**Learning outcomes:**
Upon completing the course the student will
- be familiar with the most common classifiers used in pattern recognition
- be able to apply pattern recognition methods to practical problems
- be able derive some of the basic mathematical results of pattern recognition theory

**Contents:**
The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction
Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

Recommended or required reading:
Lecture notes.
Optional reading:

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

802636S: Information Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

Ei opintojaksokuvausia.

800600S: Maturity test, 0 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

Ei opintojaksokuvausia.

800698S: Pro gradu thesis, 30 op
Opiskelumuoto: Advanced Studies
Laji: Diploma thesis
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kiele: Finnish

Ei opintojakson kuvaauksia.

H326651: Statistics advanced module, 0 - 100 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kiele: Finnish

Ei opintojakson kuvaauksia.

Compulsory

805642S: Pro gradu thesis, 30 op

Opiskelumuoto: Advanced Studies
Laji: Diploma thesis
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kiele: Finnish

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

805644S: Maturity test, 0 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kiele: Finnish

Ei opintojakson kuvaauksia.

805627S: Theory of Statistical Inference, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kiele: Finnish
Leikkaavuudet:

805611S Mathematical statistics II 10.0 op

Ei opintojakson kuvaauksia.
805620S: Pro Gradu seminar, 8 op

Voimassaolo: 01.09.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Läärä Esa
Opintokohteen kielet: Finnish

Ei opintokokonaisuuksia.

805628S: Probability Distributions, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Leikkaavuudet:

806631S Random variables and distributions 10.0 op

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish

Timing:
3rd or 4th year of studies

Learning outcomes:
After successful completion of the course the student can define the basic concepts and theorems of uni- and multidimensional discrete and continuous probability distributions and can apply this knowledge in other studies in statistics or applied mathematics. After successful completion of the course the student can define the basic concepts and theorems of uni- and multidimensional discrete and continuous probability distributions and can apply this knowledge in other studies in statistics or applied mathematics.

Contents:
Point mass function, density function, cumulative distribution function and quantile function of uni- and multivariate distributions; joint, marginal and conditional distribution; expectation, variance, covariance, correlation coefficient; moment and cumulant generating function; distributions of transformations of random variables and vectors; delta-method; convergence of random variable sequences and limit theorems; main univariate distribution models, multivariate normal distribution, important sampling distributions.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures (28 h) and practicals (14 h)

Target group:
Master's students of statistics, applied mathematics and mathematics

Prerequisites and co-requisites:
Introduction to probability theory I and II, vector analysis (or corresponding)

Recommended optional programme components:
Prerequisite for the course Theory of Statistical Inference

**Recommended or required reading:**

**Assessment methods and criteria:**
Final exam

**Grading:**
Fail, 1-5

**Person responsible:**
Esa Lääärä

**Working life cooperation:**
No

**Other information:**
-

**806624S: Practical training/consulting, 5 - 7 op**

**Opiskelumuoto:** Advanced Studies

**Laaj:** Course

**Vastuuysikkö:** Field of Mathematics

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Jari Päkkilä

**Opintokohteen kielet:** Finnish

**Voidaan suorittaa useasti:** Kyllä

Ei opintojaksokuvauksia.

**H326603: Statistics optional advanced studies, 0 - 120 op**

**Voimassaolo:** 01.08.2010 -

**Opiskelumuoto:** Advanced Studies

**Laaj:** Study module

**Vastuuysikkö:** Field of Mathematics

**Arvostelu:** 1 - 5, pass, fail

**Opintokohteen kielet:** Finnish

Ei opintojaksokuvauksia.

**Electives**

**802633S: Statistical Pattern Recognition, 10 op**

**Opiskelumuoto:** Advanced Studies

**Laaj:** Course

**Vastuuysikkö:** Field of Mathematics

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Lasse Holmström

**Opintokohteen kielet:** Finnish

**ECTS Credits:**
10 cr

**Language of instruction:**
Finnish
Timing:
Spring semester, 3rd and 4th periods.

Learning outcomes:
Upon completing the course the student will
- be familiar with the most common classifiers used in pattern recognition
- be able to apply pattern recognition methods to practical problems
- be able derive some of the basic mathematical results of pattern recognition theory

Contents:
The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

Recommended or required reading:
Lecture notes.
Optional reading:

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

802636S: Information Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

Ei opintojakosokuvauksia.

802629S: Function estimation, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

031051S: Numerical Matrix Analysis, 5 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Applied Mathematics and Computational Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Marko Huhtanen
Opintokohteen kielet: Finnish

ECTS Credits:
5

Language of instruction:
Finnish (English if necessary).

Timing:
1-2

Learning outcomes:
After completing the course the student knows the most efficient and numerically stable methods to solve the basic problems in linear algebra. The student has the capability to solve very large systems with the iterative solutions methods and understands the concept of preconditioning.

Contents:

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 40 h / Group work 20 h.

Target group:
-

Prerequisites and co-requisites:
The recommended prerequisite is the completion of the courses Calculus I and II, Matrix algebra, Numerical Methods.

Recommended optional programme components:
-

Recommended or required reading:
M. Huhtanen, Matrix Computations (opintomoniste), G. Golub and C. van Loan, Matrix Computations.

Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Marko Huhtanen
**806633S: Introduction to Bayesian Statistics, 5 op**

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Leikkaavuudet:
- 805313A Bayesian analysis 5.0 op
- 805665S Bayesian analysis 5.0 op

Ei opintojaksokuvauksia.

**805679S: Time series analysis, 5 op**

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Jussi Klemelä
Opintokohteen kielet: Finnish

ECTS Credits:
5 cr

Language of instruction:
Finnish

Learning outcomes:
After finishing the course, a student can apply linear, nonlinear and nonparametric modeling of time series. A student learns how to choose between alternative time series models and can apply statistical software to fit time series models.

Contents:
1. The course covers basic concepts of time series analysis: stationarity, autocorrelation, spectral distribution and periodogram.
2. Linear time series analysis includes explanation, prediction, parameter estimation and model diagnostics in ARMA models.
3. Nonlinear time series analysis includes threshold models and heteroskedastic time series models (ARCH and GARCH).
4. Furthermore, nonlinear nonparametric smoothing is covered (time space smoothing and state space smoothing) and nonparametric estimation of spectral densities. Nonparametric function estimation includes kernel estimation, local polynomial regression and additive modeling.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Besides lectures, there are voluntary exercises. There are 14 times 2 hour lectures and 7 times 2 hour exercises.

Target group:
Students of mathematical sciences, econometrics and finance students.
Prerequisites and co-requisites:
Basic probability theory.

Recommended optional programme components:
-

Recommended or required reading:

Assessment methods and criteria:
Examination
Read more about assessment criteria at the University of Oulu webpage.

Grading:
1 - 5

Person responsible:
Jussi Klemelä

Working life cooperation:
-

Other information:
Home page of the course is http://cc.oulu.fi/~jklemel/timeseries/
Recommended reading:

H325851: Applied mathematics advanced module, 0 - 100 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

Compulsory Advanced Studies

800698S: Pro gradu thesis, 30 op

Opiskelumuoto: Advanced Studies
Laji: Diploma thesis
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

800600S: Maturity test, 0 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish
Optional Advance Studies

802647S: Fourier series and the discrete Fourier transform, 10 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen kielet: English

Ei opintojaksokuvauksia.

802635S: Introduction to partial differential equations, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

802633S: Statistical Pattern Recognition, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

ECTS Credits:
10 cr
Language of instruction:
Finnish
Timing:
Spring semester, 3rd and 4th periods.
Learning outcomes:
Upon completing the course the student will
-be familiar with the most common classifiers used in pattern recognition
-be able to apply pattern recognition methods to practical problems
-be able derive some of the basic mathematical results of pattern recognition theory
Contents:
The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
42 h of lectures, 28 h of exercises

Target group:
Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

Prerequisites and co-requisites:
Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

Recommended or required reading:
Lecture notes.
Optional reading:

Assessment methods and criteria:
Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

Grading:
The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.

Person responsible:
Lasse Holmström

Working life cooperation:
No

Other information:
No

802636S: Information Theory, 10 op
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

802629S: Function estimation, 10 op
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

Ei opintojaksokuvauksia.

031051S: Numerical Matrix Analysis, 5 op
Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Applied Mathematics and Computational Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Marko Huhtanen
Opintokohteen kielet: Finnish

ECTS Credits:
5
Language of instruction:
Finnish (English if necessary).
Timing:
1-2
Learning outcomes:
After completing the course the student knows the most efficient and numerically stable methods to solve the basic problems in linear algebra. The student has the capability to solve very large systems with the iterative solutions methods and understands the concept of preconditioning.
Contents:
Mode of delivery:
Face-to-face teaching
Learning activities and teaching methods:
Lectures 40 h / Group work 20 h.
Target group:
-
Prerequisites and co-requisites:
The recommended prerequisite is the completion of the courses Calculus I and II, Matrix algebra, Numerical Methods.
Recommended optional programme components:
-
Recommended or required reading:
M. Huhtanen, Matrix Computations (opintomoniste), G. Golub and C. van Loan, Matrix Computations.
Assessment methods and criteria:
Read more about assessment criteria at the University of Oulu webpage.
Grading:
1-5
Person responsible:
Marko Huhtanen
Working life cooperation:
-
Other information:
-

802665S: Numerical Analysis, 5 op
Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits

Language of instruction:
English

Timing:
4th or 5th year of studies

Learning outcomes:
On successful completion of this course, the student will be able to choose proper numerical methods for solving basic mathematical problems and approximate the errors of numerical results.

Contents:
The lecture course is focused to numerical methods for solving the most common basic problems in mathematics. For the methods, convergence, stability and suitability for computer arithmetic are considered. The course contains numerical solution methods for the following basic problems: systems of nonlinear equations, systems of linear equations, interpolation, integration, derivation and differential equations.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 24 h and exercises 12 h

Target group:
Major and minor students

Prerequisites and co-requisites:
Bachelor's degree in mathematics or equivalent studies

Recommended optional programme components:
The course is an independent entity and does not require additional studies carried out at the same time.

Recommended or required reading:
Lecture notes Ward Cheney, David Kincaid: Numerical Mathematics and Computing

Assessment methods and criteria:
Final exam

Grading:
Fail, 1-5

Person responsible:
Erkki Laitinen

Working life cooperation:
No

Other information:
-

802666S: Linear Optimization, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuyksikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Erkki Laitinen
Opintokohteen kielet: Finnish
Leikkaavuudet:
800688S Theory of Optimization 10.0 op
Ei opintojakoksokuvauksia.

802667S: Nonlinear Optimization, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits
Language of instruction:
Finnish
Timing:
4th or 5th year of studies
Learning outcomes:
On successful completion of this course, the student will be able to choose the correct methods for solving the nonlinear convex optimization problems and implement the most typical numerical algorithms for solving them.

Contents:
The lecture course is focused to methods, which can apply for solving essential optimization problems of technical and economical sciences. The lectures consist of following topics: Convex optimization problem, unconstrained convex optimization, constrained convex optimization, dual of convex problem, Karush-Kuhn-Tucker conditions and penalty optimization method. The topics are considered theoretically and also numerical algorithms for problem solution are presented.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 28 h and exercises 14 h

Target group:
Major and minor students

Prerequisites and co-requisites:
Bachelor degree in mathematics or equivalent

Recommended optional programme components:
The course is an independent entity and does not require additional studies carried out at the same time.

Recommended or required reading:
Lecture notes
A. L. Peressini, F.E. Sullivan, J.J. Uhl: The mathematics of Nonlinear Programming
David g. Luenberger: Introduction to Linear and Nonlinear Programming

Assessment methods and criteria:
Final exam

Grading:
Fail, 1-5

Person responsible:
Erkki Laitinen

Working life cooperation:
H325851: Applied mathematics advanced module, 0 - 100 op

Voimassaolo: 01.08.2015 -
Opiskelumuoto: Advanced Studies
Laji: Study module
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Compulsory Advanced Studies

800698S: Pro gradu thesis, 30 op

Opiskelumuoto: Advanced Studies
Laji: Diploma thesis
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

Optional Advance Studies

802647S: Fourier series and the discrete Fourier transform, 10 op

Voimassaolo: 01.01.2010 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Valeriy Serov
Opintokohteen kielet: English

802635S: Introduction to partial differential equations, 10 op

Opiskelumuoto: Advanced Studies
**802633S: Statistical Pattern Recognition, 10 op**

**Opiskelumuoto:** Advanced Studies

**Laji:** Course

**Vastuuysikkö:** Field of Mathematics

**Arvostelu:** 1 - 5, pass, fail

**Opettajat:** Valeriy Serov, Lasse Holmström

**Opintokohteen kielet:** Finnish

**ECTS Credits:**

10 cr

**Language of instruction:**

Finnish

**Timing:**

Spring semester, 3rd and 4th periods.

**Learning outcomes:**

Upon completing the course the student will

- be familiar with the most common classifiers used in pattern recognition
- be able to apply pattern recognition methods to practical problems
- be able derive some of the basic mathematical results of pattern recognition theory

**Contents:**

The course focuses on the theory and practice of pattern recognition with emphasis on classifiers and feature extraction

**Mode of delivery:**

Face-to-face teaching

**Learning activities and teaching methods:**

42 h of lectures, 28 h of exercises

**Target group:**

Mathematics, applied mathematics and statistics majors. Other students with a sufficient mathematical background.

**Prerequisites and co-requisites:**

Calculus in one and several dimensions, linear algebra I and II. Probability theory I. Probability theory II or Random variables and distributions.

**Recommended or required reading:**

Lecture notes.

Optional reading:


**Assessment methods and criteria:**

Final exam. In the first exam following the course the student gets credit for the (possible) homework problems he/she has solved during the course.

**Grading:**

The course utilizes a numerical grading scale 1-5. In the numerical scale zero stands for a fail.
Person responsible: Lasse Holmström
Working life cooperation: No
Other information: No

802636S: Information Theory, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

Ei opintojaksojulkaisuja.

802629S: Function estimation, 10 op

Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Lasse Holmström
Opintokohteen kielet: Finnish

Ei opintojaksojulkaisuja.

031051S: Numerical Matrix Analysis, 5 op

Voimassaolo: 01.08.2012 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Applied Mathematics and Computational Mathematics
Arvostelu: 1 - 5, pass, fail
Opettajat: Marko Huhtanen
Opintokohteen kielet: Finnish

ECTS Credits: 5

Language of instruction: Finnish (English if necessary).

Timing: 1-2

Learning outcomes:
After completing the course the student knows the most efficient and numerically stable methods to solve the basic problems in linear algebra. The student has the capability to solve very large systems with the iterative solutions methods and understands the concept of preconditioning.

Contents:

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 40 h / Group work 20 h.

Target group:
-

Prerequisites and co-requisites:
The recommended prerequisite is the completion of the courses Calculus I and II, Matrix algebra, Numerical Methods.

Recommended optional programme components:
-

Recommended or required reading:
M. Huhtanen, Matrix Computations (opintomoniste), G. Golub and C. van Loan, Matrix Computations.

Assessment methods and criteria:
Read more about [assessment criteria](#) at the University of Oulu webpage.

Grading:
1-5

Person responsible:
Marko Huhtanen

Working life cooperation:
-

Other information:
-

802665S: Numerical Analysis, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1 - 5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits

Language of instruction:
English

Timing:
4th or 5th year of studies

Learning outcomes:
On successful completion of this course, the student will be able to choose proper numerical methods for solving basic mathematical problems and approximate the errors of numerical results.

Contents:
The lecture course is focused to numerical methods for solving the most common basic problems in mathematics. For the methods, convergence, stability and suitability for computer arithmetic are considered. The course contains numerical solution methods for the following basic problems: systems of nonlinear equations, systems of linear equations, interpolation, integration, derivation and differential equations.
Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 24 h and exercises 12 h

Target group:
Major and minor students

Prerequisites and co-requisites:
Bachelor's degree in mathematics or equivalent studies

Recommended optional programme components:
The course is an independent entity and does not require additional studies carried out at the same time.

Recommended or required reading:
Lecture notes Ward Cheney, David Kincaid: Numerical Mathematics and Computing

Assessment methods and criteria:
Final exam

Grading:
Fail, 1-5

Person responsible:
Erkki Laitinen

Working life cooperation:
No

Other information:
-

802666S: Linear Optimization, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1-5, pass, fail
Opettajat: Erkki Laitinen
Opintokohteen kielet: Finnish
Leikkaavuudet:
800688S Theory of Optimization 10.0 op

Ei opintojakskokuvauksia.

802667S: Nonlinear Optimization, 5 op

Voimassaolo: 01.06.2015 -
Opiskelumuoto: Advanced Studies
Laji: Course
Vastuuysikkö: Field of Mathematics
Arvostelu: 1-5, pass, fail
Opintokohteen kielet: Finnish

ECTS Credits:
5 ECTS credits

Language of instruction:
Finnish
Timing:
4th or 5th year of studies

Learning outcomes:
On successful completion of this course, the student will be able to choose the correct methods for solving the nonlinear convex optimization problems and implement the most typical numerical algorithms for solving them.

Contents:
The lecture course is focused to methods, which can apply for solving essential optimization problems of technical and economical sciences. The lectures consist of following topics: Convex optimization problem, unconstrained convex optimization, constrained convex optimization, dual of convex problem, Karush-Kuhn-Tucker conditions and penalty optimization method. The topics are considered theoretically and also numerical algorithms for problem solution are presented.

Mode of delivery:
Face-to-face teaching

Learning activities and teaching methods:
Lectures 28 h and exercises 14 h

Target group:
Major and minor students

Prerequisites and co-requisites:
Bachelor degree in mathematics or equivalent

Recommended optional programme components:
The course is an independent entity and does not require additional studies carried out at the same time.

Recommended or required reading:
Lecture notes
A. L. Peressini, F.E. Sullivan, J.J. Uhl: The mathematics of Nonlinear Programming
David g. Luenberger: Introduction to Linear and Nonlinear Programming

Assessment methods and criteria:
Final exam

Grading:
Fail, 1-5

Person responsible:
Erkki Laitinen

Working life cooperation:
No

Other information:
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